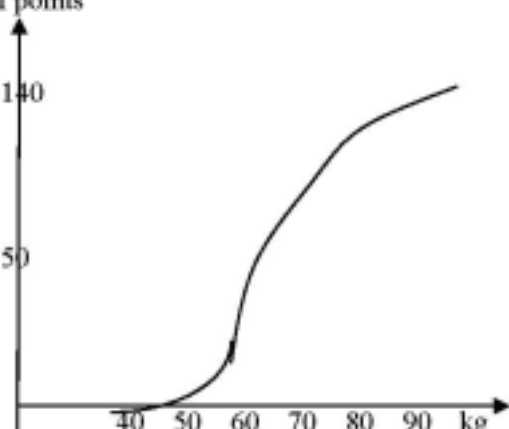


Page 4	Mark Scheme	Syllabus	Paper
	GCE AS/A LEVEL – May/June 2013	9709	63

1 $P(Q) = \frac{4}{36} \text{ or } P(S) = \frac{1}{2}$ $P(Q \cap S) = \frac{2}{36} \text{ or } P(S Q) = \frac{1}{2} \text{ or}$ $P(Q S) = \frac{2}{18}$ $P(Q \cap S) = P(Q) \times P(S) \text{ or}$ $P(S Q) = P(S) \text{ or } P(Q S) = P(Q)$ <p>Independent</p>	B1	oe	
	B1	oe	
	M1	Comparing correct pair of terms $0 \leq$ all probabilities < 1	
	A1	[4]	Correct conclusion must have all probs correct
2 $P(\text{at least } 2) = P(2, 3) \text{ or } 1 - P(0, 1)$ $= \frac{5}{12} \times \frac{4}{11} \times \frac{7}{10} \times {}_3C_2 + \frac{5}{12} \times \frac{4}{11} \times \frac{3}{10}$ $= \frac{4}{11} (0.364)$ <p>OR $\frac{{}_5C_3 + ({}_5C_2 \times {}_7C_1)}{{}_{12}C_3}$</p>	M1	Summing, or 1–, two different three-factor prob expressions, ${}_3C_2$ not needed	
	M1	12, 11, 10 seen or implied in denominator	
	M1	Mult a prob by ${}_3C_2$ or ${}_3C_1$ oe	
	A1	[4]	Correct answer
	M1	${}_5C_3$ seen added in numerator	
	M1	${}_5C_2$ seen mult alone or in numerator	
	M1	${}_{12}C_3$ seen in denom	
A1	Correct answer		
3 (i) $P(\text{tall}) = P\left(z > \frac{70-50}{16}\right) = P(z > 1.25)$ $= 1 - 0.8944$ $= 0.106$ <p>(ii) $P(\text{short}) = (1 - 0.1056)/3$</p> $= 0.2981$ $z = -0.53$ $-0.53 = \frac{x-50}{16}$ $x = 41.5$	M1	+ve/-ve Standardising no cc no sq rt no sq	
	A1	[2]	Correct answer
	M1	Subt their (i) from 1 or their (i) and multiplying by $\frac{1}{3}$ or $\frac{2}{3}$	
	A1 ft	Rounding to 0.298, only ft for $\frac{(1-(i))}{3}$	
	A1	\pm z-value rounding to 0.53, condone ± 0.24	
	M1	Standardising with their z value (not a probability), no cc sq rt etc.	
	A1	[5]	Correct answer

Page 5	Mark Scheme	Syllabus	Paper
	GCE AS/A LEVEL – May/June 2013	9709	63

<p>4 (i) $(0.8)^n < 0.001$</p> <p>$n > 30.9$ $n = 31$</p> <p>(ii) $\mu = 120 \times 0.2 = 24$ $\sigma^2 = 120 \times 0.2 \times 0.8 = 19.2$</p> $P(x < 33) = P\left(z < \frac{32.5 - 24}{\sqrt{19.2}}\right)$ $= P(z < 1.9398)$ $= 0.974$	<p>M1</p> <p>M1</p> <p>A1 [3]</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>A1 [4]</p>	<p>Eqn or inequ involving 0.8^n or 0.2^n and 0.001 or 0.999</p> <p>Trial and error or logs (can be implied)</p> <p>Correct answer MR 0.01, max available M1M1A0</p> <p>24 and 19.2 or $\sqrt{19.2}$ seen</p> <p>Standardising with or without cc, must have sq rt in denom</p> <p>Continuity correction 32.5 or 33.5</p> <p>Correct answer</p>
<p>5 (a) $P(W_2) = P(W_1W_2) + P(L_1W_2)$ $= 0.3 \times 0.6 + 0.7 \times 0.15$ $= 0.285$</p> $P(W_1 W_2) = \frac{P(W_1 \cap W_2)}{P(W_2)} = \frac{0.18}{0.285}$ $= 0.632, \frac{12}{19}$ <p>(b) $x + 4$ oe seen</p> $\frac{10}{15} \times \frac{7}{x+4} = \frac{7}{18}$ <p>$x = 8$</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>A1 [4]</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>A1 [4]</p>	<p>0.3×0.6 alone as num or denom of a fraction</p> <p>Attempt at $P(W_2)$ as sum of two 2-factor options seen anywhere</p> <p>Correct unsimplified $P(W_2)$ as num or denom of a fraction</p> <p>Correct answer</p> <p>Seen anywhere</p> <p>Mult two probabilities, one containing x and equating to $\frac{7}{18}$</p> <p>Correct unsimplified equation</p> <p>Correct answer</p>
<p>6 (i) (40, 0), (50, 12) etc. up to (90, 144)</p> <p>cf points</p>  <p>(ii) 80 weigh less than 67.2 kg $c = 67.2$</p>	<p>B1</p> <p>B1 [2]</p> <p>M1</p> <p>A1 ft [2]</p>	<p>Axes, (cf) and labels (kg), uniform scales from at least 0–140 and 40.5–69.5 either way round</p> <p>All points correct, sensible scale (not 12), polygon or smooth curve</p> <p>Subt 64 from 144</p> <p>Accept anything between 67 and 68 ft from incorrect graph</p>

Page 6	Mark Scheme	Syllabus	Paper
	GCE AS/A LEVEL – May/June 2013	9709	63

<p>(iii) freqs 12, 22, 30, 28, 52</p> <p>mean wt = $(45 \times 12 + 55 \times 22 + 62.5 \times 30 + 67.5 \times 28 + 80 \times 52) / 144$</p> <p>= 9675 / 144</p> <p>= 67.2 kg</p> <p>Var $(45^2 \times 12 + 55^2 \times 22 + 62.5^2 \times 30 + 67.5^2 \times 28 + 80^2 \times 52) / 144$</p> <p>– $(9675/144)^2 = 127.59$</p> <p>sd = 11.3, allow 11.2</p>	<p>M1 A1 M1 A1 M1 A1</p> <p>[6]</p>	<p>frequencies attempt not cf Correct freqs</p> <p>Using mid points attempt, i.e. 44.5, 45, 45.5, in correct mean formula, unsimplified, no cfs, condone 1 error.</p> <p>Correct mean</p> <p>Substituting their mid-pts squared (may be class widths, lower or upper bound) in correct var formula even with cfs with their mean²</p> <p>Correct answer</p>
<p>7 (i)</p> <p>S(10) R(14) P(6)</p> <p>1 2 4 = $10C1 \times 14C2 \times 6C4 = 13650$</p> <p>1 3 3 = $10C1 \times 14C3 \times 6C3 = 72800$</p> <p>2 2 3 = $10C2 \times 14C2 \times 6C3 = 81900$</p> <p>Total = 168350 or 168000</p> <p>(ii) $2! \times 2! \times 5!$</p> <p>= 480</p> <p>If M0 earned $\frac{2! \times 2!}{2! \times 2!}$ or $\frac{5!}{3!}$ or both, seen mult by an integer ≥ 1 Or $2! \times 2! \times 5!$ divided by a value</p> <p>(iii) spaniels and retrievers in 4! ways gaps in $5P3$ or $5 \times 4 \times 3$ ways = 1440</p> <p>If M0 earned $\frac{4!}{2! \times 2!}$ or $\frac{{}_5P_3}{3!}$ or both, seen multiplied by an integer > 1 or $7! - 5! \times 3!$ – $\{(4! \times 2 \times 4 \times 3!) + (4! \times 3 \times 4 \times 3!)\}$ = 1440</p> <p>If M0 earned $3! \times 2! \times 2!$ used as a denominator in all 4 terms</p>	<p>M1 M1 B1 A1</p> <p>[4]</p> <p>M1 M1 A1</p> <p>[3]</p> <p>M1 M1 A1</p> <p>SCM1</p> <p>M1 M1 A1</p> <p>SCM1</p>	<p>Summing 2 or more 3-factor options perms or combs</p> <p>Mult 3 combs or 4 combs with $\Sigma r=7$</p> <p>2 options correct, unsimplified</p> <p>Correct answer</p> <p>$2! \times 2!$ oe, seen mult by an integer ≥ 1, no division</p> <p>Mult by 5!, or 5! alone, seen mult by an integer ≥ 1 no division</p> <p>Correct answer</p> <p>4! seen multiplied by an integer > 1</p> <p>Mult by $5P3$ oe</p> <p>Correct answer</p> <p>${}_5C_3$ oe</p> <p>oe</p> <p>oe, e.g. $6 \times 5 \times 4 \times 4!$</p> <p>Marks cannot be earned from both methods.</p>