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1	$z = 1.452$ $1.452 = \frac{20 - \mu}{\mu/5}$ $\mu = 15.5$	B1 B1 B1	[3]	Rounding to ± 1.45 $\frac{20 - \mu}{\mu/5}$ or $\frac{20 - 5\sigma}{\sigma}$ seen oe rounding to correct answer
2	$\bar{x} = 50 + 81.4/22 = 53.7$ $\text{var} = 671/22 - 3.7^2 = 16.81(16.8)$ $16.81 = \Sigma x^2/22 - 53.7^2$ $= 63811(63800)$ OR $\Sigma x - 22 \times 50 = 81.4$ ($\Sigma x = 1181.4$) $\Sigma x^2 - 100 \Sigma x + 22 \times 50^2 = 671$ $\Sigma x^2 = 671 + 118140 - 55000 = 63811$ $\text{Var} = \Sigma x^2/22 - (\Sigma x/22)^2 = 16.81$	M1 A1 M1 A1 M1 M1 A1 A1	[4]	Attempt to find variance using coding in both, correct formula Correct answer using their var and their mean with uncoded formula for both correct answer expanded eqn with 22×50 seen expanded eqn with 2 or 3 terms correct correct answer correct answer
3	(i) $P(x < 440)$ $= P\left(z < \frac{440 - 445}{3.6}\right) = 1 - \Phi(1.389)$ $= 1 - 0.9176$ $\text{Ans} = 0.0824$ (ii) $z = 1.881$ $\frac{c}{3.6} = 1.881$ $c = 6.77$	M1 M1 A1 M1 M1 A1	[3]	Standardising no cc no sq or sq rt Correct area ($1 - \Phi$) oe (indep) Rounding to correct answer accept 0.0825 ± 1.88 or 1.881 or 1.882 or 1.555 seen \pm Equation with $\pm c/3.6$ or $2c/3.6$ only = z or prob (can be implied) Correct answer accept 6.78
4	(i) $p = 4/9$ or $5/9$ $P(\text{at least } 2) = 1 - P(0, 1)$ $= 1 - (5/9)^5 - (4/9)(5/9)^4 {}_5C_1$ $= 0.735$ (ii) $np = 96$ $npq = 32$ $p = P(\leq k)$ $p = 2/3$ $q = 1/3$ $n = 144$ $k = 6$ $n = 144$	B1 M1 A1 M1 A1 A1ft A1	[3]	Binomial term ${}_5C_x p^x (1-p)^{5-x}$ seen Correct answer Using $np = 96$ $npq = 32$ to obtain eqn in 1 variable $1/3$ or $2/3$ seen or implied Correct k ft $k = 9p$ correct n

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5	(i)	Stem leaf	B1		Correct stem condone a space under the 1	
		0 1 4 6 8				
		1 0 3 4 4 4 5 5 5 6 6 6 6 7 8 8	B1		Correct leaves must be single digits and one line for each stem value or 2 lines each stem value	
		2 0 1 5 7 8				
		3 1				
		4 5				
		5 7				
		Key 1 4 represents \$140	B1ft	[3]	Correct key must have \$, ft 2 special cases	
	(ii)	Median = 160 LQ = 140 UQ = 210 IQ range = UQ - LQ = 70	B1 M1 A1	[3]	Subt their LQ from their UQ Correct answer cwo	
	(iii)	1.5 × IQ range = 105 Lower outlier is below 35 Upper outlier is above 315 Outliers 10, 450, 570	M1 A1ft A1	[3]	Mult their IQ range by 1.5 can be implied Correct limits ft their IQ range and quartiles Correct outliers	
6	(i)	H J O				
		1. 28 2 = 4C2 × 9C8 × 2C2 = 54	M1		Mult 3 combs, 2C2 may be implied	
		3 7 2 = 4C3 × 9C7 × 2C2 = 144	M1		4Cx × 9Cy × 2Cz	
		4 6 2 = 4C4 × 9C6 × 2C2 = 84	A1		Summing 2 or 3 three-factor options	
		Total = 282 ways	A1	[4]	2 options correct unsimplified Correct answer	
	(ii)	4! × 6! × 2! × 3! = 207360 (207000)	M1 M1 A1	[3]	4! × 6! × 2! oe seen multiplied by int ≥ 1 3! seen mult by int ≥ 1 Correct answer	
	(iii)	8 J and O trees in 8! = 40320 ways 9 gaps × 8 × 7 × 6 = 121,927,680 (122,000,000)	B1 M1 A1	[3]	8! seen mult by int ≥ 1 no division 9P4 oe or 7P4 or 8P4 seen mult by int ≥ 1 no division Correct answer	
	(i)	SR 4C2 × 9C2 × 2C2 × 9C6	M1			
	(ii)	SR $\frac{4! \times 6! \times 2!}{4! \times 6! \times 2!}$ or 3! or both	M1			

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	(iii)	SR1 $12! - 9! 4!$	M1										
		SR2 $\frac{9P4}{4!}$ or $\frac{8!}{6!2!}$ or both	M1										
7	(i)	$P(T,B) = \frac{5}{12} \times \frac{2}{10} = \frac{1}{12}$ (0.0833)	M1 A1	[2]	Mult their $P(T)$ by $2/9$ or $2/10$ only Correct answer								
	(ii)	$P(C_S \cap C_A) = \frac{7}{12} \times \frac{4}{10} = \frac{28}{120}$ (0.2333)	M1		Mult their $P(C_S)$ by $3/9$ or $4/10$ seen as num or denom of a fraction								
		$P(C_A) = \frac{7}{12} \times \frac{4}{10} + \frac{5}{12} \times \frac{3}{10} = \frac{43}{120}$ (0.3583)	M1	Summing 2 two-factor products to find $P(C_A)$ seen anywhere									
		$P(C_S C_A) = \frac{P(C \cap C)}{P(C_A)} = \frac{28/120}{43/120}$	A1	Correct unsimplified $P(C_A)$ seen as num or denom of a fraction									
		$= \frac{28}{43}$ (0.651)	A1	[4] Correct answer									
	(iii)	<table border="1" style="margin-left: 20px;"> <tr> <td>x</td> <td>0</td> <td>1</td> <td>2</td> </tr> <tr> <td>Prob</td> <td>7/24</td> <td>19/40</td> <td>7/30</td> </tr> </table>	x	0	1	2	Prob	7/24	19/40	7/30	B1		$x = 0, 1, 2$, can be implied from table or working
	x	0	1	2									
	Prob	7/24	19/40	7/30									
		$P(X = 0) = P(T, B) + P(T, T)$	M1		1 or 2 two-factor products, denoms 12 and 10 or 12 and 9, implied if ans is correct								
		$= \frac{5}{12} \times \frac{2}{10} + \frac{5}{12} \times \frac{5}{10} = \frac{7}{24}$ (0.292)	A1		One correct unsimplified								
	$P(X = 2) = P(C, C) = \frac{7}{12} \times \frac{4}{10} = \frac{28}{120}$ (0.233)	B1		One other correct unsimplified									
	$P(X = 1) = 1 - 7/24 - 28/120 = \frac{19}{40}$ (0.475)	B1ft	[5]	Third correct ft $1 - P(2 \text{ of their probs})$									