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	<b>GCE AS/A LEVEL – May/June 2012</b>	<b>9709</b>	<b>72</b>

Note: “(3 sfs)” means “answer which rounds to ... to 3 sfs”. If correct ans seen to  $\geq 3$ sfs, ISW for later rounding. Penalise  $< 3$  sfs only once in paper.

<b>1 (i)</b>	$H_0$ : Pop mean = 3 $H_1$ : Pop mean > 3	B1 [1]	Allow $\mu$ or $\lambda$ , but not just ‘mean’
<b>(ii)</b>	0.0683 > 0.05 No evidence that pop mean increased	M1 A1ft [2]	For inequality stated or clearly shown on dig. Allow ‘No increase in mean’
<b>[Total: 3]</b>			
<b>2 (i)</b>	$7, \sqrt[3]{\sqrt{n}}$	B1, B1 [2]	oe
<b>(ii) (a)</b>	Pop is normal	B1 [1]	Allow $X$ is normal
<b>(b)</b>	Large sample	B1 [1]	or large $n$ (can be implied by $n \geq 30$ )
<b>[Total: 4]</b>			
<b>3 (i)</b>	$p = \frac{18}{50}$ or 0.36 oe $z = 2.326$ $0.36 \pm z \sqrt{\frac{0.36 \times (1-0.36)}{50}}$ = 0.202 to 0.518 (3 sfs)	B1 B1 M1 A1 [4]	Allow any $z$ ( $\neq 0$ or 1) Allow any brackets or none
<b>(ii)</b>	Sample random	B1 [1]	oe
<b>[Total: 5]</b>			
<b>4 (i)</b>	$\lambda = 8 \times 0.32 + 12 \times 0.45$ (= 7.96) $1 - e^{-7.96} \left( 1 + 7.96 + \frac{7.96^2}{2} \right)$ = 0.986 (3 sfs)	M1 M1 A1 [3]	$1 - P(X \leq 2)$ , any $\lambda$ allow one end error
<b>(ii)</b>	$\lambda = 155 \times 0.32 = 49.6$ $N(49.6, 49.6)$ $\frac{34.5 - 49.6}{\sqrt{49.6}}$ (= -2.144) $\Phi(-2.144) = 1 - \Phi(2.144)$ = 0.016(0)	B1 M1 M1 M1 A1 [5]	$N(\lambda, \lambda)$ any $\lambda$ . May be implied Allow no or wrong cc & no $\sqrt{\quad}$ Correct area consistent with their working
<b>[Total: 8]</b>			
<b>5 (i)</b>	$F + J \sim N(24, 2.8^2 + 2.6^2)$ $\frac{30-24}{\sqrt{14.6}}$ (= 1.570) $P(F + J < 30) = \Phi(1.570)$ 0.942 (3 sfs)	B1 M1 M1 A1 [4]	or $N(24, 14.6)$ for correct mean and variance Allow without $\sqrt{\quad}$ (ignore false cc) Correct area consistent with their working

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<b>(ii)</b>	$F - 2J \sim N(-11.4, 2.8^2 + 4 \times 2.6^2)$ $\frac{0 - (-11.4)}{\sqrt{34.88}} (= 1.930)$ $P(F - 2J) > 0$ $= 1 - \Phi(1.930)$ $= 0.0268$ (3 sfs)	B1 M1 M1 A1 [4]	or $N(-11.4, 34.88)$ for correct mean and variance Allow without $\sqrt{\quad}$ (ignore false cc) Correct area consistent with their working or similar scheme using $2J - F$
<b>[Total: 8]</b>			
<b>6 (i)</b>	$\int_4^{25} kx^{-\frac{1}{2}} dx = 1$ $\left[ \frac{kx^{\frac{1}{2}}}{\frac{1}{2}} \right]_4^{25} = 1$ $2k(5 - 2) = 1$ $(k = \frac{1}{6} \text{ AG})$	M1 A1 [2]	Attempt integrate & = 1. Ignore limits or equiv correct subst of correct limits
<b>(ii)</b>	$\frac{1}{6} \int_4^{25} x^{\frac{1}{2}} dx$ $= \frac{1}{6} \left[ \frac{x^{\frac{3}{2}}}{\frac{3}{2}} \right]_4^{25} (= \frac{1}{9} (125 - 8))$ $= 13$	M1 A1 A1 [3]	Attempt integ $xf(x)$ . Ignore limits Correct integrand and limits Or 117/9
<b>(iii)</b>	$\frac{1}{6} \int_{20}^{25} x^{-\frac{1}{2}} dx$ $(= \frac{1}{6} \left[ \frac{x^{\frac{1}{2}}}{\frac{1}{2}} \right]_{20}^{25} = \frac{1}{3} (5 - \sqrt{20}))$ $= 0.176$ (3 sfs)	M1 A1 [2]	Attempt integ $f(x)$ from 20 to 25 Or $1 - \int_4^{20}$
<b>(iv)</b>	Wkly demand may be $> 25$ (or $< 4$ )	B1 [1]	or other sensible
<b>[Total: 8]</b>			
<b>7 (i)</b>	$H_0: \mu = 2.0 \quad H_1: \mu \neq 2.0$ $\bar{x} = \frac{430}{200} = 2.15$ $s^2 = \frac{200}{199} \left( \frac{1290}{200} - \left( \frac{430}{200} \right)^2 \right)$ $= 1.8366834$ $\frac{2.15 - 2.0}{\sqrt{\frac{1.8366834}{200}}} (= 1.565)$ $z = 1.645$ No evidence that $\mu \neq 2.0$	B1 B1 B1 M1 M1 A1 [6]	For $\bar{x}$ Correct subst in $s^2$ formula For $s^2$ correct (or $s = 1.35524$ ) For standardising (need 200) accept sd/var mixes For correct comparison of z values or areas Cwo (condone biased variance for last 3 marks)

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<b>(ii) (a)</b>	Concluding $\mu = 2.0$ although not true	B1 [1]	Not concluding $\mu \neq 2.0$ although this is true
<b>(b)</b>	$\frac{\bar{x}-2.0}{\sqrt{\frac{1.85}{200}}} = 1.645$ $\bar{x} = 2 + 0.1582$ Rejection region is $\bar{x} < 1.8418 \text{ and } \bar{x} > 2.1582$ $\frac{2.1582-2.12}{\sqrt{\frac{1.85}{200}}} \quad (= 0.397)$ $P(\bar{x} < 2.1582 \mid \mu = 2.12) = \Phi('0.397')$ $= 0.6543$ $\frac{1.8418-2.12}{\sqrt{\frac{1.85}{200}}} \quad (= -2.893)$ $P(\bar{x} < -2.893 \mid \mu = 2.12) = 1 - \Phi('2.893')$ $(= 0.0019)$ $\Rightarrow P(1.8418 < \bar{x} < 2.1582 \mid \mu = 2.12)$ $= 0.6543 - 0.0019$ $= 0.6524$ $P(\text{Type II error}) = 0.652 \text{ (3 sfs)}$	M1  A1  M1  M1  M1  M1  A1 [7]	Attempt at finding rejection region              Using only RH tail (ans 0.654) scores max M1A0M1M1M0M0A0 SR If zero scored allow SC M1 for one standardisation attempt with den $\sqrt{(1.85 / 200)}$
<b>[Total: 14]</b>			