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Note: "(3 sfs)" means "answer which rounds to ... to 3 sfs". If correct ans seen to \geq 3sfs, ISW for later rounding. Penalise < 3 sfs only once in paper

1	$z = 2.326$ $494 \pm z \times \frac{23}{\sqrt{150}}$ $= 490 \text{ to } 498 \text{ (3 sfs)}$	B1 M1 A1 [3]	seen Any z
2	$(0.75 \times 54.8 + 0.25 \times 82.4 =) 61.7$ $0.75^2 \times 16.0^2 + 0.25^2 \times 4.8^2$ $(= 145.44)$ $\text{sd} = 12.1 \text{ (3 sfs)}$	B1 M1 A1 [3]	No need for $\sqrt{\quad}$ for M1
3	$H_0: p = 0.15$ $H_1: p > 0.15$ $(N(300 \times 0.15, 300 \times 0.15 \times 0.85))$ $= N(45, 38.25)$ $\frac{59.5 - '45'}{\sqrt{38.25}} (= 2.345)$ Allow wrong or no cc $z = 1.96 \quad 2.345 > 1.96$ Evidence prop is higher for new plan	B1 B1 M1 M1 A1 [5]	or H_0 : Approval rate same for new as for old H_1 : Approval rate for new > for old $(N(0.15, \frac{0.15 \times 0.85}{300}))$ $= N(0.15, 0.000425)$ or $\frac{59}{300} + \frac{0.5}{300} - '0.15'$ $\sqrt{0.000425} (= 2.345)$ Allow wrong or no cc comparison (or area comparison) cwo
4 (i)	$\int_0^1 \frac{k}{(x+1)^2} dx = 1$ $-\left[\frac{k}{x+1}\right]_0^1 = 1$ $-k\left(\frac{1}{2} - 1\right) = 1$ $(k = 2 \text{ AG})$	M1 A1 [2]	Any attempt integ $f(x)$ & = 1. Ignore limits oe, with limits inserted correctly
(ii)	$\int_0^a \frac{2}{(x+1)^2} dx = \frac{1}{5}$ $-\left[\frac{2}{x+1}\right]_0^a = \frac{1}{5}$ $-\left(\frac{2}{a+1} - 2\right) = \frac{1}{5}$ $a = \frac{1}{9}$	M1 A1 A1 [3]	Attempt integ $f(x)$ & = $\frac{1}{5}$ (oe), ignore limits oe, with correct limits inserted correctly
(iii)	Area below $x = 0.5$ is greater than 0.5 $m < 0.5$	B1 B1dep [2]	oe, eg More area at left hand end

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5	(i) (a)	$P(X \geq 3) = 1 - e^{-3.2} \left(1 + 3.2 + \frac{3.2^2}{2!} \right)$ $= 0.62(0)$ (3 sf)	M1 A1 [2]	Allow one end error																	
	(b)	$P(X = 3) = e^{-3.2} \left(\frac{3.2^3}{3} \right)$ (= 0.22262) $\left(\frac{P(X=3 \cap X \geq 3)}{P(X \geq 3)} = \frac{P(X=3)}{P(X \geq 3)} \right)$ $= \frac{0.22262}{0.62010}$ $= 0.359$ (3 sf)	M1 M1 A1 [3]	May be implied Their $P(X=3)$ Their $P(X \geq 3)$																	
5	(ii) (a)	(Approx) normal with mean 3.2 variance = $\frac{3.2}{120}$ or $\frac{2}{75}$ or 0.0267 (3 sfs) oe	B1 B1 [2]	or sd = $\sqrt{\frac{3.2}{120}}$ or 0.163 (3 sfs) oe																	
	(b)	$\frac{3.3-3.2}{\sqrt{\frac{3.2}{120}}}$ (= 0.612) Φ ("0.612") $= 0.730$ (3 sfs)	M1 M1 A1 [3]	Allow with cc attempted Accept 0.73																	
6	(i)	$\bar{x} = 1.96$ ($\Sigma x^2 f = 254$) $S^2 = \frac{50}{49} x \left(\frac{254}{50} - 1.96^2 \right)$ $= \frac{1548}{1225}$ or 1.2637	B1 M1 A1 [3]	Correct sub in S^2 formula																	
	(ii)	H_0 : Pop mean = 1.66 H_1 : Pop mean \neq 1.66 $\frac{1.96-1.66}{\sqrt{\frac{1.2637}{50}}}$ $= 1.887$ $z = 1.96$ 1.887 < 1.96 No evidence that mean has changed	B1 M1 A1 M1 A1 _{ft} [5]	<table border="0"> <tr> <td></td> <td>H_0: Pop mean = 1.66</td> <td></td> </tr> <tr> <td></td> <td>H_1: Pop mean > 1.66</td> <td>B0</td> </tr> <tr> <td></td> <td>$\frac{1.96-1.66}{\sqrt{\frac{1.2637}{50}}}$</td> <td>M1</td> </tr> <tr> <td></td> <td>= 1.887</td> <td>A1</td> </tr> <tr> <td></td> <td>$z = 1.645$</td> <td>M1</td> </tr> <tr> <td>In context</td> <td>Evidence mean has changed</td> <td>A1_{ft}</td> </tr> </table>		H_0 : Pop mean = 1.66			H_1 : Pop mean > 1.66	B0		$\frac{1.96-1.66}{\sqrt{\frac{1.2637}{50}}}$	M1		= 1.887	A1		$z = 1.645$	M1	In context	Evidence mean has changed
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	= 1.887	A1																			
	$z = 1.645$	M1																			
In context	Evidence mean has changed	A1 _{ft}																			
(iii)	No because H_0 not rejected	B1 _f [1]	If H_0 rejected in (ii): Yes because H_0 rejected																		
(iv)	State mean not changed when it has $-1.96 < \text{test stat} < 1.96$	B1 B1 [2]	<table border="0"> <tr> <td>In context</td> <td>State mean not increased when it has</td> <td>B1</td> </tr> <tr> <td></td> <td>test stat < 1.645</td> <td>B1</td> </tr> </table>	In context	State mean not increased when it has	B1		test stat < 1.645	B1												
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7 (i)	$\lambda = 5$ $1 - e^{-5} \left(1 + 5 + \frac{5^2}{2!} \right)$ $= 0.875$	B1 M1 A1 [3]	Any λ . Allow one end error
(ii)	$X \sim N(120, 120)$ $\frac{109.5-120}{\sqrt{120}} (= -0.9585)$ $1 - \Phi("0.9585")$ $(= 1 - 0.8312)$ $"0.1688"^{*2}$ $= 0.0285 \text{ to } 0.0286$	B1 M1 M1 A1 [4]	May be implied Allow with wrong or no cc or no $\sqrt{\quad}$
(iii)	$\lambda = 15 \times \frac{5}{60} + 0.5$ $= 1.75$ $e^{-1.75} \left(\frac{1.75^3}{3!} + \frac{1.75^4}{4!} + \frac{1.75^5}{5!} \right)$ $= 0.247 \text{ (3 sfs)}$	M1 A1 M1 A1 [4]	Any λ . Allow one end error