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<p><b>3 (i)</b> <math>\frac{7!}{3!} \times 2</math> = 1680</p> <p><b>(ii)</b> <math>{}^6C_4 = 15</math></p> <p><b>(iii)</b> 1E in <math>{}^6C_3</math> ways = 20</p> <p><b>(iv)</b> need 2Es in <math>{}^6C_2</math> ways = 15 ways need 3Es in <math>{}^6C_1 = 6</math> ways total = 15 + 20 + 15 + 6 = 56 ways</p>	<p>B1</p> <p>B1 [2]</p> <p>B1 [1]</p> <p>M1</p> <p>A1 [2]</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1ft [4]</p>	<p><math>\frac{7!}{3!}</math> or 840 seen or implied</p> <p>correct answer</p> <p>correct answer</p> <p><math>k \times {}^6C_a</math> or <math>k \times {}^bC_3</math> (<math>k</math> a constant) or <math>{}^6P_d</math> or <math>{}^eP_3</math> seen</p> <p>correct final answer</p> <p>attempt to find ways with 2Es or 3Es <math>{}^6C_2</math> oe and <math>{}^6C_1</math> oe seen</p> <p>summing ways for no Es, 1E, 2Es and 3Es</p> <p>correct final answer, ft on their four answers</p>												
<p><b>4 (i)</b> mean = <math>11/6</math> (<math>1\frac{5}{6}</math>, 1.83)</p> <p>sd = <math>\sqrt{(1+1+1+4+9+9)/6 - (11/6)^2}</math> = <math>\sqrt{29}/6</math> (0.898)</p> <p><b>(ii)</b></p> <table border="1" data-bbox="132 1003 679 1077"> <tr> <td><math>x</math></td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> </tr> <tr> <td>Pr</td> <td>9/36</td> <td>6/36</td> <td>13/36</td> <td>4/36</td> <td>4/36</td> </tr> </table> <p><b>(iii)</b> <math>p = 1/3</math> <math>np = 8</math> <math>n = 24</math></p> <p>Var = <math>24 \times 1/3 \times 2/3 = 16/3</math> (5.33)</p>	$x$	2	3	4	5	6	Pr	9/36	6/36	13/36	4/36	4/36	<p>B1</p> <p>M1</p> <p>A1 [3]</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1 [4]</p> <p>B1</p> <p>M1</p> <p>A1ft [3]</p>	<p>correct answer</p> <p>numerical use of a correct sd/variance formula</p> <p>correct answer</p> <p>all correct <math>x</math> values P(2) and P(6) correct considering more than 1 case for a sum of 3 or 4 or 5 P(3), P(4) and P(5) correct</p> <p>correct <math>p</math> using <math>np = 8</math> to find <math>n</math> or <math>8(1 - p)</math> to find var, <math>0 &lt; p &lt; 1</math></p> <p>correct answer, ft their <math>p</math></p>
$x$	2	3	4	5	6									
Pr	9/36	6/36	13/36	4/36	4/36									

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<b>5 (i)</b>					
	Designer	Not designer	Total		
H-h shoes	2	4	6	B1	one row or column correct
L-h shoes	1	3	4	B1 [2]	all correct
Sports	5	5	10	B1ft [1]	correct answer, ft their table
Total	8	12	20	B1ft [1]	correct answer, ft their table
<b>(ii)</b> 1/20 (0.05)				B1ft [1]	correct final answer, ft their table
<b>(iii)</b> 10/20 (1/2, 0.5)				M1	finding $P(D \cap S)$ and comparing with their $P(D) \times P(S)$
<b>(iv)</b> 2/8 (1/4, 0.25)				A1ft [2]	correct conclusion, ft their table
<b>(v)</b> $P(D) = 8/20$ (0.4) $P(S) = 10/20$ (0.5) $P(D \cap S) = 5/20$ (0.25) Not independent as $P(D) \times P(S) \neq P(D \cap S)$					
[OR <sub>1</sub> $P(D S) = \frac{P(D \cap S)}{P(S)} = \frac{5}{10}$ $P(D) = \frac{8}{20}$ Not independent as $P(D S) \neq P(D)$					finding $P(D S)$ and comparing with their $P(D)$ correct conclusion, ft their table]
[OR <sub>2</sub> $P(S D) = \frac{P(S \cap D)}{P(D)} = \frac{5}{8}$ $P(S) = \frac{10}{20}$ Not independent as $P(S D) \neq P(S)$					finding $P(D S)$ and comparing with their $P(D)$ correct conclusion, ft their table]
<b>(vi)</b> $P(\text{at most } 4) = 1 - {}^7C_5(0.4)^5(0.6)^2 - {}^7C_6(0.4)^6(0.6)^1 - (0.4)^7$ $= 0.904$				M1 M1 A1 [3]	bin probability of form ${}^7C_r p^r (1-p)^{7-r}$ , $r \neq 0$ or 7  bin expression for $1 - P(5, 6, 7)$ or $P(0, 1, 2, 3, 4)$ , any $p$ correct answer

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<p>6 (i) <math>\frac{34.1 - \mu}{\sigma} = 1.751</math>  <math>\frac{26.7 - \mu}{\sigma} = -0.524</math>  <math>\mu = 28.4, \sigma = 3.25</math></p>	<p>B1  B1 M1 M1 A1 [5]</p>	<p><math>\pm 1.751</math> seen  <math>\pm 0.524</math> seen a standardising equation with a z-value, <math>\mu</math> and <math>\sigma</math> valid attempt to eliminate <math>\mu</math> or <math>\sigma</math> correct answers</p>
<p>(ii) <math>\Phi\left(\frac{34.5 - 32.9}{2.4}\right) - \Phi\left(\frac{33.5 - 32.9}{2.4}\right)</math>  <math>= \Phi(0.667) - \Phi(0.25)</math>  <math>= 0.7477 - 0.5987</math>  <math>= 0.149</math></p>	<p>M1  M1 A1 [3]</p>	<p>one numerical standardising expression, no cc, no square root, can have 34  subtracting two areas correct answer</p>
<p>(iii) <math>\Phi\left(\frac{t - 32.9}{2.4}\right) - \Phi\left(\frac{31.8 - 32.9}{2.4}\right) = 0.5</math>  <math>\Phi\left(\frac{t - 32.9}{2.4}\right) - (1 - 0.6765) = 0.5</math>  <math>\Phi\left(\frac{t - 32.9}{2.4}\right) = 0.8235</math>  <math>\frac{t - 32.9}{2.4} = 0.929</math>  <math>t = 35.1</math></p>	<p>M1  M1  M1 A1 [4]</p>	<p>using 2 standardising expressions to give an equation involving subtraction and 0.5, oe  adding their tail to 0.5 oe  solving a standardised equation, must be a z- value from their 0.8235 correct final answer</p>