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1	$0.6 = 1.2 \omega$ $\omega = 0.5 \text{ rads}^{-1}$	M1 A1 [2]	Uses $v = r \omega$ [2]
2 (i)	$(9 + 11)OG =$ $+/-[9 \times 0.7/(\pi/2) - 11 \times (2 \times 0.7)/3\pi/2]$ $OG = 0.0371 \text{ m}$ AG	M1 A1 A1 [3]	Table of value idea with signs either way round. Accept -ve answer
(ii)	$\tan \theta = 0.0371(36..)/0.7$ $\theta = 3.0^\circ$ Lamina	M1 A1 B1 [3]	 [6]
3 (i)	$F + F \cos 60 = mg$ $F = 10m/1.5$ $F \sin 60 = mv^2/0.6$ $v = 1.86 \text{ ms}^{-1}$	M1 A1 M1 A1 [4]	Resolves vertically for S May be implied by later work $10m/1.5 = mv^2/0.6$
(ii)	$F \cos 60 = 10m$ $F \sin 60 = m \omega^2/0.6$ $\omega = 5.37 \text{ rads}^{-1}$	B1 M1 A1 [3]	May be implied by later work [7]
4 (i)	$EE = 21(\sqrt{1.2^2 + 1.6^2} - 1.2)^2/(2 \times 1.2)$ $m12^2/2 = mg \times 1.6 +$ $2 \times 21(\sqrt{1.2^2 + 1.6^2} - 1.2)^2/(2 \times 1.2)$ $m = 0.2$	B1 M1 A1 A1 [4]	Use of EE formula (= 5.6J) KE/EE/PE conservation
(ii)	$T = 21(\sqrt{1.2^2 + 0.5^2} - 1.2)/1.2$ $ma = 2 \times 21(\sqrt{1.2^2 + 0.5^2} - 1.2)/1.2 \times \frac{0.5}{1.3}$ $- mg$ $a = (-)3.27 \text{ ms}^{-2}$	B1 M1 A1 A1 [4]	Newton's Second Law with component of T or reversed signs [8]

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<p>5 (i) $0.4v\frac{dv}{dx} = 0.4g\sin 30 - 0.6x$</p> <p>$\int v\,dv = \int (5 - 1.5x)\,dx$</p> <p>$v^2/2 = 5x - 1.5x^2/2 (+ c)$</p> <p>$0.4g\sin 30 - 0.6x = 0$</p> <p>$x = 3\frac{1}{3}$</p> <p>$v^2/2 = 5 \times 10/3 - 1.5 \times (10/3)^2/2$</p> <p>$v = 4.08\text{ ms}^{-1}$</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1 [7]</p>	<p>Newton's Second Law, – sign essential</p> <p>Accept uncancelled integration</p> <p>Accept omission of c</p> <p>Maximum speed when acceleration = 0</p> <p>Accept 10/3</p>	
<p>(ii) $0 = 5x - 1.5x^2/2$</p> <p>$x = 6\frac{2}{3} = 6.67$</p>	<p>M1</p> <p>A1 [2]</p>	<p>Uses $v = 0$ appropriately</p> <p>Not 20/3</p>	[9]
<p>6 (i)</p> <p>$1.5 \times 0.4 \times 0.2 + 1 \times 1 \times 0.9$ $= (1 \times 1 + 1.5 \times 0.4)d$ or $0.5 \times 0.4 \times 0.2 + 1 \times 1.4 \times 0.7$ $= (0.5 \times 0.4 + 1 \times 1.4)d$ or $1.5 \times 1.4 \times 0.7 - 1 \times 0.5 \times 0.9$ $= (1.5 \times 1.4 - 1 \times 0.5)d$</p> <p>$d = 0.6375$</p>	<p>M1</p> <p>A1</p> <p>A1 [3]</p>	<p>Table of moments idea</p> <p>Uses area or any weight/m² value</p> <p>Accept 0.637 or 0.638</p>	
<p>(ii) $F \times 1.5 = 120 \times 0.6375$</p> <p>$F = 51$</p> <p>$F \times 1.5 = 120 \times (0.6375 - 0.4)$</p> <p>$F = 19$</p> <p>$51 > F > 19$</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1 [6]</p>	<p>Moments about O</p> <p>Candidates consider both cases ✓ [cv(two values of F)] accept ></p>	[9]

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7 (i)	$x = (15\cos 41)t$	B1	
	$y = (15\sin 41)t - gt^2/2$	B1	
	$y = (15\sin 41)x/(15\cos 41) - 5 [x/(15\cos 41)]^2$	M1	
	$y = 0.869x - 0.0390x^2$	A1 [4]	$y = 0.86928..x - 0.03901..x^2$
(ii)	$H = 0.869 \times 1.5 - 0.039 \times 1.5^2 + 1.6$	M1	Must add height of O
	$H = 2.82\text{ m}$	A1	
	$0.039x^2 - 0.869x - 1.6 = 0$	M1	Uses $y = -1.6$ and tries to solve
	$D = 23.99 - 1.5$	DM1	Solve a 3 term quadratic equation and minus 1.5
	$D = 22.5\text{ m}$	A1 [5]	Accept 22.4

[9]