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1		M1	For using $WD = Fd \cos \alpha$
	$F \times 5 \cos 60^\circ = 75$	A1	
	Magnitude of the force is 30 N	A1	[3]
2	[ $12 = 15 \sin \alpha$ ]	M1	For resolving forces in the direction of the force of magnitude 12 N
	$\alpha = 53.1$	A1	
	[ $F = 15 \cos \alpha$ ]	M1	For resolving forces in the direction of the force of magnitude F N
	$F = 9 \text{ N}$	A1	[4]
2	ALTERNATIVE 1		
	[ $F \sin \alpha = 12 \cos \alpha$ and $F \cos \alpha + 12 \sin \alpha = 15 \rightarrow \sin \alpha \div \cos \alpha = 12 \cos \alpha \div 15 - 12 \sin \alpha$ ]	M1	For resolving forces in the $x$ and $y$ directions and eliminating F from the resultant equations
	$15 \sin \alpha - 12 \sin^2 \alpha = 12 \cos^2 \alpha \rightarrow 15 \sin \alpha = 12 \rightarrow \alpha = 53.1$	A1	
		M1	For substituting into $F \sin \alpha = 12 \cos \alpha$ or $F \cos \alpha + 12 \sin \alpha = 15$
	$F = 9 \text{ N}$	A1	[4]
2	ALTERNATIVE 2		
	[ $\sin \alpha = 12/15$ ]	M1	For using correct triangle of forces to find $\alpha$
	$\alpha = 53.1$	A1	
	[ $F^2 = 15^2 - 12^2$ ]	M1	For using correct triangle of forces to find F
	$F = 9 \text{ N}$	A1	[4]
2	ALTERNATIVE 3		
	[ $12 \div \sin(180 - \alpha) = 15 \div \sin 90 \rightarrow 12 = 15 \sin \alpha$ ]	M1	For using Lami's rule and $\sin(180^\circ - \alpha) = \sin \alpha$
	$\alpha = 53.1$	A1	
	[ $F \div \sin 143.1 = 15 \div \sin 90$ ]	M1	For using Lami's rule and value of $\alpha$ to find F
	$F = 9 \text{ N}$	A1	[4]
<b>SR (max 2/4) For candidates who have sin and cos interchanged.</b>			
Allow B1 for $\alpha = 36.9$ and allow B1 for $F = 9$ following correct work relative to the cos/sin interchange error.			

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3	(i)	M1	For an attempt to find $v(t)$ using integration of $a(t)$
	$v = 1.2t^{5/3} + 2$	A1	
		DM1	For attempting to solve $v(t) = 3$ for $t^{5/3}$ or For confirming $v = 3$ by substituting $t^{5/3} = 5/6$ into the expression found for $v(t)$
	$t^{5/3} = 5/6$	A1	[4] AG
<hr/>			
	(ii)	M1	For integrating and using $s(0) = 0$ (may be implied by absence of +C) to find $s(t)$
	$s = 0.45t^{8/3} + 2t$	A1	
	Distance is 2.13 m	A1	[3]
<hr/>			
4	(i)	M1	For resolving forces horizontally
	Horizontal component is $T\cos 25^\circ$ (0.906T)	A1	
		M1	For resolving forces vertically
	Vertical component is $4g + T\sin 25^\circ$ (40 + 0.423T)	A1	[4]
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	(ii)	M1	For using $F = 0.4R$
	$0.906T = 16 + 0.169T$	A1ft	May be implied by correct answer for T
	$T = 21.7\text{ N}$	A1	[3]
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5	(i)	B1	
	Tension in $S_1$ is 30 N Tension in $S_2$ is 50 N	B1	[2]
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	(ii)	M1	For applying Newton's second law to A or to B
	$3g - T - 1.6 = 3a$ (or $2g + T - 4 = 2a$ )	A1	
	$2g + T - 4 = 2a$ (or $3g - T - 1.6 = 3a$ ) or $(3g + 2g) - (1.6 + 4) = (3 + 2)a$	B1	
	Acceleration is $8.88\text{ ms}^{-2}$	B1	
	Tension is 1.76 N	A1	[5]
<b>SR (max. 1 / 2) for candidates who do not give numerical answers in (i).</b>			
Allow B1 for Tension in $S_1$ is $3g$ and Tension in $S_2$ is $5g$			

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<b>6 (i)</b>	PE gain = $1250 \times 10 \times 400 \times 0.125$	B1	
	WD against resistance is $800 \times 400$ J	B1	
		M1	For using WD by car's engine = Gain in PE + WD against resistance
	WD by car's engine is 945 000 J (945 kJ)	A1	[4]
<b>(ii)</b>			For using $P = Fv \rightarrow$
	$[v_2/6 = 5 \times (1/3)]$	M1	$\frac{v_2}{v_1} = \frac{P_2}{P_1} \times \frac{F_1}{F_2}$
	$v_2 = 10$	A1	
	KE gain = $\frac{1}{2} 1250(10^2 - 6^2)$	B1ft	
	[WD by car's engine = 945 000 + 40 000]	M1	For using WD by car's engine = (Gain in PE + WD against resistance) + KE gain
	WD by car's engine is 985 000 J (985 kJ)	A1ft	[5] ft incorrect ans(i)
<b>Alternative scheme for part (i)</b>			
<b>(i)</b>		M1	For using Newton's second law with $a = 0$
	DF = $1250g \times 0.125 + 800$	A1	
		M1	For using WD = DF $\times$ 400
	WD by car's engine is 945 00 J (945 kJ)	A1	[4]

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7	(i)	$[-0.12 = 0.15a]$	M1	For using Newton's 2 <sup>nd</sup> law
		$a = -0.8 \text{ ms}^{-2}$	A1	
		$[v = 3 - 0.8 \times 2]$	M1	For using $v = u + at$ to find speed of approach
		$v_{\text{approach}} = 1.4$	A1	
		$[\frac{1}{2} 0.15(1.4^2 - v_r^2)]$	M1	For using KE loss = $\frac{1}{2} m(v_a^2 - v_r^2)$
		$v_{\text{return}} = -1$	A1	
			M1	For using $0 = v_{\text{return}} + a(t - 2)$
		$t = 3.25 \text{ s}$ when block comes to rest	A1	
				Alternative for the M1 A1 immediately above. $t_{YZ} = 1.25$ B1 $t = 3.25 \text{ s}$ when block is at rest B1ft
				ft incorrect values of v and t (although $v_{\text{return}}$ must be negative)
		For correct sketch	B1ft	[9]
	(ii)	$[XY = \frac{1}{2} (3 + 1.4) \times 2, YZ = \frac{1}{2} 1.25 \times 1]$	M1	For using area property (or equivalent) to find distances XY and YZ
		$s = 4.4$ at Y and $3.775$ at Z, stated or on graph	A1	(accept 3.77 or 3.78)
		Curve starts at origin, s increases, slope decreases (convex upwards) for $0 < t < 2$ , value of s(2) shown	B1ft	ft incorrect value for s(2)
		Curve starts at (2, 4.4), s decreases, magnitude of slope decreases to zero at (3.25, 3.775)	B1ft	[4] ft incorrect values of s and t