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- 1 Either: State or imply non-modular inequality  $(x + 3)^2 < (2x + 1)^2$  or corresponding equation or pair of linear equations B1  
 Attempt solution of 3-term quadratic or of 2 linear equations M1  
 Obtain critical values  $-\frac{4}{3}$  and 2 A1  
 State answer  $x < -\frac{4}{3}, x > 2$  A1
- Or: Obtain critical value  $x = 2$  from graphical method, inspection, equation B1  
 Obtain critical value  $x = -\frac{4}{3}$  similarly B2  
 State answer  $x < -\frac{4}{3}, x > 2$  B1 [4]
- 2 (i) State or imply equation in the form  $(5^x)^2 + 5^x - 12 = 0$  B1  
 Attempt solution of quadratic equation for  $5^x$  M1  
 Obtain  $5^x = 3$  only A1 [3]
- (ii) Use logarithms to solve equation of the form  $5^x = k$  where  $k > 0$  M1  
 Obtain 0.683 A1 [2]
- 3 (i) Attempt division, or equivalent, at least as far as quotient  $2x + k$  M1  
 Obtain quotient  $2x - 3$  A1  
 Complete process to confirm remainder is 4 A1 [3]
- (ii) State or imply  $(4x^2 + 4x - 3)$  is a factor B1  
 Obtain  $(2x - 3)(2x - 1)(2x + 3)$  B1 [2]
- 4 (i) State or imply  $R = 15$  B1  
 Use appropriate formula to find  $\alpha$  M1  
 Obtain  $53.13^\circ$  A1 [3]
- (ii) Attempt to find at least one value of  $\theta - \alpha$  M1  
 Obtain one correct value  $68.6^\circ$  of  $\theta$  A1  
 Carry out correct method to find second answer M1  
 Obtain  $217.7^\circ$  and no others in range A1 [4]
- (iii) State 15, following their value of  $R$  from part (i) B1√ [1]
- 5 (i) State  $\frac{dx}{dt} = \frac{1}{t+1}$  B1  
 State  $\frac{dy}{dt} = 2e^{2t} + 2$  B1  
 Attempt expression for  $\frac{dy}{dx}$  M1  
 Obtain  $\frac{dy}{dx} = (2e^{2t} + 2)(t + 1)$  or equivalent A1 [4]
- (ii) Substitute  $t = 0$  and attempt gradient of normal M1  
 Obtain  $-\frac{1}{4}$  following their expression for  $\frac{dy}{dx}$  A1√  
 Attempt to find equation of normal through point (0, 1) M1  
 Obtain  $x + 4y - 4 = 0$  A1 [4]

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- 6 (i) Attempt use of quotient rule or equivalent M1  
 Obtain  $\frac{2(x+2)\cos 2x - \sin 2x}{(x+2)^2}$  or equivalent A1  
 Equate numerator to zero and attempt rearrangement M1  
 Confirm given result  $\tan 2x = 2x + 4$  A1 [4]
- (ii) Consider sign of  $\tan 2x - 2x - 4$  for 0.6 and 0.7 or equivalent M1  
 Obtain -2.63 and 0.40 or equivalents and justify conclusion A1 [2]
- (iii) Use iteration process correctly at least once M1  
 Obtain final answer 0.694 A1  
 Show sufficient iterations to 5 decimal places to justify answer or show a sign change in the interval (0.6935, 0.6945) A1 [3]  
 [0.6  $\rightarrow$  0.69040  $\rightarrow$  0.69352  $\rightarrow$  0.69363  
 0.65  $\rightarrow$  0.69215  $\rightarrow$  0.69358  $\rightarrow$  0.69363  
 0.7  $\rightarrow$  0.69384  $\rightarrow$  0.69364  $\rightarrow$  0.69363]
- 7 (i) Replace  $\tan^2 x$  by  $\sec^2 x - 1$  B1  
 Express  $\cos^2 x$  in the form  $\pm \frac{1}{2} \pm \frac{1}{2} \cos 2x$  M1  
 Obtain given answer  $\sec^2 x + \frac{1}{2} \cos 2x - \frac{1}{2}$  correctly A1  
 Attempt integration of expression M1  
 Obtain  $\tan x + \frac{1}{4} \sin 2x - \frac{1}{2} x$  A1  
 Use limits correctly for integral involving at least  $\tan x$  and  $\sin 2x$  M1  
 Obtain  $\frac{5}{4} - \frac{1}{8} \pi$  or exact equivalent A1 [7]
- (ii) State or imply volume is  $\int \pi(\tan x + \cos x)^2 dx$  B1  
 Attempt expansion and simplification M1  
 Integrate to obtain one term of form  $k \cos x$  M1  
 Obtain  $\pi(\frac{5}{4} - \frac{1}{8} \pi) + \pi(2 - \sqrt{2})$  or equivalent A1 [4]