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<p>1 $\tan^2 \theta - \sin^2 \theta = \tan^2 \theta \sin^2 \theta$</p> <p>(i) $\frac{s^2}{c^2} - s^2$ $\rightarrow \frac{s^2 - s^2 c^2}{c^2} = \frac{s^2(1 - c^2)}{c^2}$ $\rightarrow t^2 s^2$</p> <p>(ii) RHS > 0 $\rightarrow \tan^2 \theta > \sin^2 \theta$ QED $\tan \theta > \sin \theta$ if θ acute.</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>[3]</p> <p>B1</p> <p>[1]</p>	<p>Use of $s \div c = t$</p> <p>Use of $s^2 + c^2 = 1$</p> <p>All ok</p> <p>Realises RHS > 0</p>
<p>2 $\vec{OA} = \begin{pmatrix} 2 \\ -1 \\ 4 \end{pmatrix}, \vec{OB} = \begin{pmatrix} 4 \\ 2 \\ -2 \end{pmatrix}, \vec{OC} = \begin{pmatrix} 1 \\ 3 \\ p \end{pmatrix}$.</p> <p>(i) $\vec{AB} = \begin{pmatrix} 2 \\ 3 \\ -6 \end{pmatrix}$ Modulus = $\sqrt{(4+9+36)}$</p> <p>Unit Vector = $\frac{1}{7} \begin{pmatrix} 2 \\ 3 \\ -6 \end{pmatrix}$</p> <p>(ii) $\vec{OB} \cdot \vec{OC} = 4 + 6 - 2p$ $= 0 \rightarrow p = 5$</p>	<p>B1 M1</p> <p>A1✓</p> <p>[3]</p> <p>M1A1</p> <p>[2]</p>	<p>co. Correct method for modulus</p> <p>co for his vector AB.</p> <p>Dot product = 0. co</p>
<p>3 $(1 - 2x)^2(1 + ax)^6$</p> <p>Coeff of x in $(1 + ax)^6 = 6ax$</p> <p>Coeff of x^2 in $(1 + ax)^6 = 15a^2x^2$</p> <p>Multiplies by $(1 - 4x + 4x^2)$</p> <p>2 terms in x $6a - 4 = -1$ $\rightarrow a = \frac{1}{2}$</p> <p>3 terms in x^2 $15a^2 - 24a + 4 = b$ $\rightarrow b = -4\frac{1}{4}$</p>	<p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>[6]</p>	<p>6C1 needs removing (here or later)</p> <p>6C2 needs removing (here or later)</p> <p>Needs to consider 2 terms in equation</p> <p>Co</p> <p>Needs to consider 3 terms in equation</p>
<p>4 $\sin 2x + 3 \cos 2x = 0$</p> <p>(i) $\rightarrow \tan 2x = -3$ $2x = 180 - 71.6$ or $360 - 71.6$ $x = 54.2^\circ$ or 144.2° Also 234.2° and 324.2°</p> <p>(ii) 12 answers.</p>	<p>M1</p> <p>M1</p> <p>A1A1✓</p> <p>A1✓</p> <p>[5]</p> <p>B1✓</p> <p>[1]</p>	<p>Uses $\tan 2x = k$ and works with "2x".</p> <p>Finds "2x" before $\div 2$</p> <p>co. co✓ (both of these need 2nd M)</p> <p>for 180° + his answer(s)</p> <p>for 3 times the number of solns to (i).</p>

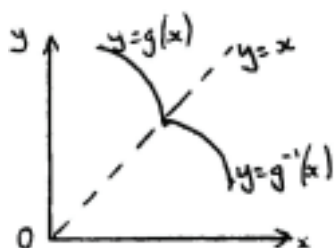
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<p>5 $x = \frac{8}{y^2} - 2$; at $x = 0, y = 2$</p> <p>$\rightarrow x^2 = \frac{64}{y^4} - \frac{32}{y^2} + 4$</p> <p>Integral of $x^2 = \frac{64y^{-3}}{-3} - \frac{32y^{-1}}{-1} + 4y$</p> <p>Uses limits 1 to 2 $\rightarrow 6^{2/3}\pi$</p>	<p>B1</p> <p>B1B1B1</p> <p>M1 A1</p> <p>[6]</p>	<p>co</p> <p>All co.</p> <p>Uses 1 to 2 or 2 to 1. co.</p>
<p>6 (i) Uses S_n</p> <p>$\frac{9}{2}(24 + 8d) = 135 \rightarrow d = \frac{3}{4}$</p> <p>(ii) 9th term of AP = $12 + 8 \times \frac{3}{4} = 18$ GP 1st term 12, 2nd term 18 Common ratio = $r = 18 \div 12 = 1\frac{1}{2}$ 3rd term of GP = $ar^2 = 27$ nth term of AP is $12 + (n - 1)\frac{3}{4}$ $12 + (n - 1)\frac{3}{4} = 27 \rightarrow n = 21$</p>	<p>M1 A1</p> <p>[2]</p> <p>B1[✓]</p> <p>M1 M1</p> <p>M1A1</p> <p>[5]</p>	<p>Uses correct formula co</p> <p>[✓] on “d”</p> <p>Uses “ar” Uses ar^2 or “ar” $\times r$</p> <p>Links AP with GP. co</p>
<p>7 $y = \frac{10}{2x+1} - 2$</p> <p>(i) $\frac{dy}{dx} = \frac{-10}{(2x+1)^2} \times 2$</p> <p>At A, $y = 0, \rightarrow x = 2$</p> <p>m at $x = 2$, is $-\frac{4}{5}$</p> <p>Eqn of tangent is $y = -\frac{4}{5}(x - 2)$ $\rightarrow 5y + 4x = 8$</p> <p>(ii) C (0, 1.6) $d = \sqrt{(1.6^2 + 2^2)} = 2.56$</p>	<p>B1 B1</p> <p>B1</p> <p>M1 A1</p> <p>[5]</p> <p>M1 A1</p> <p>[2]</p>	<p>Without the “$\times 2$”. For the “$\times 2$”.</p> <p>For $x = 2$</p> <p>Must be using differential as m co – answer given.</p> <p>Correct method – needs [✓]. co</p>
<p>8 (i) $OBX = 90^\circ, \cos \theta = \frac{r}{2r}$ $\rightarrow \theta = \frac{1}{3}\pi$.</p> <p>(ii) Arc length $AB = \frac{1}{3}r\pi$ $BX = r \tan(\frac{1}{3}\pi) = r\sqrt{3}$ $P = r + (\frac{1}{3}r\pi + r\sqrt{3})$</p> <p>(iii) Area = $\frac{1}{2}r^2\sqrt{3} - \frac{1}{6}r^2\pi$</p>	<p>M1 A1</p> <p>[2]</p> <p>B1 B1 B1</p> <p>[3]</p> <p>B1[✓] B1</p> <p>[2]</p>	<p>Needs $90^\circ + \cos$ (or Pyth + sin or tan) co ag</p> <p>$r +$ sum of other two</p> <p>[✓] on $\tan(\frac{1}{3}\pi)$. co</p>

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<p>9 $\frac{d^2y}{dx^2} = -4x$</p> <p>(i) $\frac{dy}{dx} = -2x^2 + c$ $\frac{dy}{dx} = 0$ when $x = 2$, $\rightarrow c = 8$ $y = -\frac{2x^3}{3} + 8x (+C)$ Subs (2, 12) $\rightarrow C = \frac{4}{3}$</p> <p>(iii) $\frac{dy}{dt} = \frac{dy}{dx} \times \frac{dx}{dt}$ $= -10 \times 0.05$ \rightarrow decreasing at 0.5 units per second</p>	<p>B1 B1 B1 B1^h M1 A1 [6] M1 A1 [2]</p>	<p>For $-2x^2$ $c = 8$ For each term $-x^h$ on “c” – ignore (+C) Uses (2, 12) to find C. Must use. Enough to see product of gradient and rate. bod over notation.</p>
<p>10 $2y + x = k \quad xy = 6$</p> <p>(i) $2y + x = 8 \rightarrow y(8 - 2y) = 6$ $2y^2 - 8y + 6 = 0$ or $x^2 - 8x + 12 = 0$ $\rightarrow (6, 1)$ and $(2, 3)$</p> <p>Midpoint $M(4, 2)$ $m = -\frac{1}{2}$ Perpendicular $m = 2$ $\rightarrow y - 2 = 2(x - 4)$</p> <p>(ii) $(k - 2y)y = 6$ $\rightarrow 2y^2 - ky + 6 = 0$ or $x^2 - kx + 12 = 0$ Uses $b^2 - 4ac = 0$ $\rightarrow k^2 > 48$ $\rightarrow k < -\sqrt{48}$ and $k > \sqrt{48}$</p>	<p>M1 DM1A1 M1 M1 A1 [6] M1 A1 A1 [3]</p>	<p>Complete elimination of x (or y) DM1 soln of quadratic. co for their 2 points Uses $m_1m_2 = -1$ to find perp. gradient co unsimplified Any use of $b^2 - 4ac$ on a quadratic = 0 For $\sqrt{48}$ on its own All correct.</p>

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<p>11 $f(x) = 8 - (x - 2)^2$,</p> <p>(i) Stationary point at $x = 2$ y - coordinate = 8 Nature Maximum (or $y = -x^2 + 4x + 4$ $-2x + 4 = 0 \rightarrow (2, 8)$ Max)</p> <p>(ii) $k = 2$</p> <p>(iii) $y = 8 - (x - 2)^2$ $\rightarrow (x - 2)^2 + y = 8$ $\rightarrow (x - 2) = \pm\sqrt{8 - y}$ $\rightarrow g^{-1} = 2 + \sqrt{8 - x}$</p> <p>(iv)</p> 	<p>B1 B1 B1</p> <p>[3]</p> <p>B1[✓]</p> <p>[1]</p> <p>M1 M1 A1</p> <p>[3]</p> <p>B1 B1 B1</p> <p>[3]</p>	<p>co co co independent of first two marks</p> <p>✓ on “x-value”</p> <p>Attempt to make x the subject Order of operations correct Must be $f(x)$.</p> <p>B1 arc 1st quad (no tp, no axes) B1 Evidence of symmetry about $y = x$ B1 all correct as shown left</p>
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