

Page 4	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE AS/A LEVEL – May/June 2011	9709	72

1	$E(T) = 9.6$ $\text{Var}(\text{wt of one bag}) = 0.0016$ $\text{Var}(T) = 3 \times 0.0016$ $\text{sd of } T = \sqrt{3 \times 0.0016} = 0.0693$	B1 M1 M1 A1 [4]	May be impl. by $\text{Var}(T) = 0.0048$ or $0.0144$
<b>[Total: 4]</b>			
2	$\bar{X} \sim N\left(3, \frac{9}{60}\right)$ $\frac{2.8-3}{\sqrt{\frac{9}{60}}} (= -1.033)$ $\Phi(-1.033) = 1 - \Phi(1.033)$ $= 0.151$	B2 M1 M1 A1 [5]	B1 for $N$ & $\mu = 3$ ; (oe) B1 for $\frac{9^4}{60}$ or $\frac{3}{80}$ or $0.0375$ (oe) (oe working with totals or proportions) With or without c.c.  With cc of $-\frac{1}{120}$ , $\Phi(-1.076) = 1 - \Phi(1.076) = 0.141$
<b>[Total: 5]</b>			
3	(i) Constant average rate of goals scored Goals random Goals indep	B1 B1 [2]	Any two given in context (SR score B1 for any two not in context) Not Goals scored singly (because this is inherent in the context so it's not a condition)
	(ii) $e^{-1.8} \left( \frac{1.8^3}{3!} + \frac{1.8^4}{4!} + \frac{1.8^5}{5!} \right)$ $= 0.259$	M1 A1 [2]	Poisson probs, $\lambda = 1.8$ . Allow 2, 6 included
	(iii) $1 - e^{-1.8}$ $(1 - e^{-1.8})^{10}$ $= 0.164$	M1 M1 A1 [3]	Any $\lambda$ . Allow end errors.
<b>[Total: 7]</b>			
4	(i) $\bar{x} = 8.4$ $8.4 \pm z \frac{1.3}{\sqrt{15}}$ $z = 2.576$ [7.54, 9.26]	B1 M1 B1 A1 [4]	Accept 2.574 to 2.579 or equiv. Accept 7.53. Accept 9.27
	(ii) No because pop normal so $\bar{X}$ normally distr	B1 B1 [2]	SR If 'Yes' or no conclusion, but 2 correct statements score B1
	(iii) 8 within CI Claim justified	B1√ B1√ [2]	ft (i)
<b>[Total: 8]</b>			

<b>Page 5</b>	<b>Mark Scheme: Teachers' version</b>	<b>Syllabus</b>	<b>Paper</b>
	<b>GCE AS/A LEVEL – May/June 2011</b>	<b>9709</b>	<b>72</b>

<b>5</b>	<b>(i)</b> Po(3.3) $e^{-3.3}(1 + 3.3 + \frac{3.3^2}{2})$  = 0.359	B1 M1  A1 [3]	seen or implied Poisson $P(0) + P(1) + P(2)$ . Allow + $P(3)$ Allow wrong $\lambda$ . Accept equiv method.
	<b>(ii)</b> $X \sim \text{Po}(36)$ $X \sim \text{N}(36, 36)$ $\frac{48.5 - 36}{\sqrt{36}}$ = 2.08(3) comp with 1.96 Evidence to support claim	B1 B1  M1  A1 M1 A1√ [6]	Allow with no or wrong cc or no $\sqrt{\quad}$ 2.08(3) or 0.0186/0.0187 if area comparison Valid comparison Correct conclusion (ft their $z$ )
<b>[Total: 9]</b>			
<b>6</b>	<b>(i)</b> $H_0: P(6) = \frac{1}{6}$ $H_1: P(6) > \frac{1}{6}$	B1 [1]	Condone undefined $p$
	<b>(ii)</b> $\left(\frac{5}{6}\right)^{10} + 10 \times \left(\frac{5}{6}\right)^9 \times \frac{1}{6} + \binom{10}{2} \times \left(\frac{5}{6}\right)^8 \times \frac{1}{6}^2 + \binom{10}{3} \times \left(\frac{5}{6}\right)^7 \times \left(\frac{1}{6}\right)^3$  $1 - \left(\left(\frac{5}{6}\right)^{10} + 10 \times \left(\frac{5}{6}\right)^9 \times \frac{1}{6} + \binom{10}{2} \times \left(\frac{5}{6}\right)^8 \times \left(\frac{1}{6}\right)^2 + \binom{10}{3} \times \left(\frac{5}{6}\right)^7 \times \left(\frac{1}{6}\right)^3\right)$  = 0.0697 (3 sfs)	M1  M1  A1 [3]	(1 –) $P(0,1,2,3)$ o.e. using $B(10,1/6)$ allow end errors  Attempt at fully correct expression for $1 - P(0,1,2,3)$ o.e.  Accept 0.0698
	<b>(iii)</b> Die biased towards a six but result < 4 so no evidence of bias	B1 [1]	or equiv. Must be in context
	<b>(iv)</b> P(0, 1, 2 or 3 sixes) $\left(\frac{1}{2}\right)^{10} + 10 \times \left(\frac{1}{2}\right)^9 \times \frac{1}{2} + \binom{10}{2} \times \left(\frac{1}{2}\right)^8 \times \left(\frac{1}{2}\right)^2 + \binom{10}{3} \times \left(\frac{1}{2}\right)^7 \times \left(\frac{1}{2}\right)^3$ = 0.172 or 11/64	B1  M1  A1 [3]	Stated or attempted. Can be implied  Attempt at $P(0,1,2,3)$ with $p = 1/2$ , allow end errors.
<b>[Total: 8]</b>			

Page 6	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE AS/A LEVEL – May/June 2011	9709	72

7	(i)	$\int_{-1}^1 k(1-x)dx = 1$ $(k[x - \frac{x^2}{2}]_{-1}^1 = 1)$ $2k = 1$ $(k = \frac{1}{2} \quad \text{AG})$	M1  A1 [2]	Attempt integ f(x) = 1 with correct limits
	(ii)	$(\int_{0.5}^1 \frac{1}{2}(1-x)dx = \frac{1}{2}[x - \frac{x^2}{2}]_{0.5}^1)$ $= \frac{1}{16} \text{ or } 0.0625$	B1 [1]	
	(iii)	$\int_{-1}^1 \frac{1}{2}(x-x^2)dx$ $= \frac{1}{2}[\frac{x^2}{2} - \frac{x^3}{3}]_{-1}^1$ $= -\frac{1}{3} \text{ or } -0.333$	M1 A1 A1 [3]	$\int xf(x)dx$ ignore limits Correct integrand and limits
	(iv)	$\int_{-1}^a \frac{1}{2}(1-x)dx = 0.25$ $(\frac{1}{2}[x - \frac{x^2}{2}]_{-1}^a = 0.25)$ $(\frac{1}{2}(a - \frac{a^2}{2} - (-1 - \frac{1}{2})) = 0.25)$ $a^2 - 2a - 2 = 0$ $a = 1 - \sqrt{3} \text{ or } -0.732$	M1  A1 A1 [3]	Correct limits (or integral from a to 1 = 0.75)  any correct QE with “= 0”(or in completed square form $(a-1)^2 = 3$ ) Not $a = 1 \pm \sqrt{3}$ ; Not -0.732 or 2.732
			<b>[Total: 9]</b>	