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1 (i) $(3.6 \times 9 + 64) / 24$ $= 4.02$ years	M1 A1 [2]	Mult by 9, adding 64 then dividing by 24 Correct answer
(ii) $\frac{\Sigma x_A^2}{9} - 3.6^2 = 1.925^2$ $\Sigma x_A^2 = 150$ $\frac{150.0 + 352}{24} - 4.017^2 = 4.780$ $sd = 2.19$	M1 A1 M1 A1 [4]	Attempt to find Σx_A^2 using correct variance formula Correct Σx_A^2 Using 352 + their 150 in correct variance formula Correct answer
2 (i) $4 \times 3 \times 7$ $= 84$	B1 [1]	Correct answer
(ii) $10! - 9! \times 2$ $= 2903040$ (2900000) <i>OR</i> $8! \times 9 \times 8$ $= 2903040$ (2900000)	B1 B1 [2] B1 B1	$10! - k \times 9!$ seen oe Correct answer $8! \times 9 \times l$ seen oe Correct answer
(iii) ${}^9C_1 + {}^9C_2 + \dots + {}^9C_9$ $= 511$ <i>OR</i> $2^9 - 1$ $= 511$	M1 M1 A1 [3] M1 M1 A1	Using combinations Adding 9 combinations Correct answer 2^9 seen Subtracting 1 Correct answer
3 (i) $median_A < 35$ or $20 \leq median_A < 35$ or $median_A = 33.0/33.1/33.5/33.6$ or $median_B \geq 50$ or $50 \leq median_B < 70$ or $median_B = 51.7/51.9/52.2/52.4$ $median_B > median_A$ <i>OR</i> A has 66 cand $50 < mark < 100$, so $med_A < 50$ or B has 156 cand $50 < mark < 100$, so $med_B > 50$ $median_B > median_A$	B1 B1 [2] B1 B1	Correct numerical statement re $median_A$ or $median_B$ Correct numerical statement re other median and a conclusion As before As before
(ii) $159 - 68 = 91$	B1 [1]	Correct final answer
(iii) $mean = \left(\frac{4.5 \times 25 + 14.5 \times 43 + 27 \times 91}{+ \dots + 84.5 \times 40} \right) / 300$ $= 11270 / 300 = 37.6$	M1 M1 M1 A1 [4]	Using an attempt at mid-points, not end points or class widths Using an attempt at frequencies, not cum freqs Sum of 6 prods, correct freqs, divided by 300 Correct answer

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<p>4 (i) (a) $P(\text{final score is } 12) = P(6, 6) = 1/36$</p> <p>(b) $P[(1,5) + (1,4) + (2,3) + (3,2) + (4,1)]$ $= 5/36$</p>	<p>B1 [1]</p> <p>M1</p> <p>M1</p> <p>A1 [3]</p>	<p>Correct answer</p> <p>Considering $P(1, 5)$</p> <p>Considering $P[(1,4) + (2,3) + (3,2) + (4,1)]$</p> <p>Correct answer</p>
<p>(ii) $P(A) = 1/6$ $P(B) = P[(1,5) + (2,4) + (3,3) + (4, 2) + (5,1)]$ $= 5/36$ $P(C) = 1 - P(O, O) = 3/4$</p> <p>$P(A \text{ and } B) = P(1 \text{ and } 5) = 1/36$ $\neq P(A) \times P(B)$ $P(A \text{ and } C) = P[(2,5) + (4,5) + (6,5)] = 3/36$ $\neq P(A) \times P(C)$ $P(B \text{ and } C) = P[(2,4) + (4,2)] = 2/36$ $\neq P(B) \times P(C)$ None are independent.</p>	<p>B1</p> <p>B1</p> <p>M1</p> <p>A1√</p> <p>A1 [5]</p>	<p>Any two of $P(A)$, $P(B)$ and $P(C)$ correct</p> <p>Third probability correct</p> <p>Numerical attempt to compare $P(X \text{ and } Y)$ with $P(X) \times P(Y)$, must be three positive probs</p> <p>One correct comparison and conclusion, ft their probabilities</p> <p>Correct conclusion(s) following legitimate working</p>
<p>5 (i) $z = \pm 1.751$ $\pm \frac{20 - \mu}{\mu/4} = 1.751$ $\mu = 13.9$</p>	<p>B1</p> <p>M1</p> <p>A1 [3]</p>	<p>Correct z</p> <p>Standardising no cc, no sqrt, must be a z-value</p> <p>Correct answer</p>
<p>(ii) $P(X < 10) = P(z < \pm \frac{10 - 13.91}{13.91/4})$ $= P(z < -1.124)$ $= 1 - 0.8694$ $= 0.131$ $P(10 < X < 20) = 0.96 - 0.131$ $= 0.829 \text{ or } 0.830$</p>	<p>M1</p> <p>M1</p> <p>A1 [3]</p>	<p>Standardising attempt with 10, their μ and their $\mu/4$, no cc, no sqrt</p> <p>"$\Phi_1 + \Phi_2 - 1$", ft their mean</p> <p>Correct answer</p>
<p>(iii) $\mu = 250 \times 0.96 = 240$ $\sigma^2 = 250 \times 0.96 \times 0.04 = 9.6$ $P(\geq 235) = 1 - \Phi\left(\pm \frac{234.5 - 240}{\sqrt{9.6}}\right)$ $= \Phi(1.775)$ $= 0.962$</p>	<p>B1</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>A1 [5]</p>	<p>240 and 9.6 or sq rt 9.6 seen unsimplified</p> <p>Standardising, with or without cc, must have sq rt in denom</p> <p>Continuity correction 234.5 or 235.5 only</p> <p>Correct region > 0.5, ft their mean</p> <p>Correct answer</p>

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<p>6 (i) $(0.75)^n < 0.06$</p> <p>$n > 9.78$</p> <p>$n = 10$</p>	<p>M1*</p> <p>M1dep*</p> <p>A1 [3]</p>	<p>Equation or inequality with 0.75^n and 0.06 or 0.94 seen</p> <p>Attempt at solving by trial and error (can be implied) or using logarithms correctly</p> <p>Correct answer</p>
<p>(ii) $E(X) = 14 \times 0.75$ or 10.5</p> <p>Try $P(10) = {}^{14}C_{10}(0.75)^{10}(0.25)^4 = 0.220$</p> <p>$P(11) = {}^{14}C_{11}(0.75)^{11}(0.25)^3 = 0.240$</p> <p>(mode is) 11</p> <p>OR</p>	<p>M1</p> <p>M1</p> <p>A1 [3]</p> <p>M1</p> <p>M1</p> <p>A1</p>	<p>Evaluating binomial probability for an integer value directly above or below their mean</p> <p>Evaluating the other binomial probability</p> <p>Correct answer</p> <p>Evaluating binomial $P(n)$ and $P(n + 1)$</p> <p>Evaluating binomial $P(10)$, $P(11)$ and $P(12)$</p> <p>Correct answer</p>
<p>(iii) $P(> 11)$</p> <p>$= {}^{14}C_{12}(0.75)^{12}(0.25)^2 + {}^{14}C_{13}(0.75)^{13}(0.25)^1 + (0.75)^{14}$</p> <p>$= 0.281$</p> <p>$P(3) = {}^5C_3 (0.2811)^3(0.7189)^2$</p> <p>$= 0.115$</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1 [5]</p>	<p>A binomial term of the form ${}^{14}C_n p^n (1 - p)^{14 - n}$ seen, $n \neq 0$ or 14</p> <p>Summing binomial $P(12, 13, 14)$ or $P(11, 12, 13, 14)$</p> <p>Correct answer 0.280 – 0.282</p> <p>A binomial term of the form ${}^5C_3 p^3 (1 - p)^2$ seen, any p</p> <p>Correct answer</p>