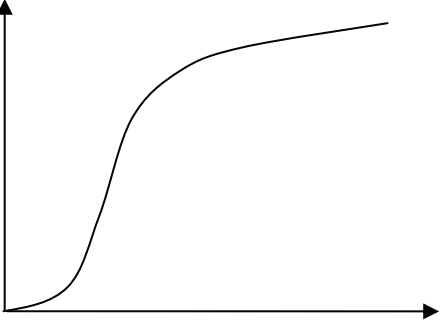


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<p>1 $18p = 2.7$ $p = 0.15$ $P(2, 3, 4) =$ ${}^{18}C_2 \times (0.15)^2(0.85)^{16} + {}^{18}C_3(0.15)^3(0.85)^{15}$ $+ {}^{18}C_4(0.15)^4(0.85)^{14}$ $= 0.655$</p>	<p>B1 M1 A1 A1 [4]</p>	<p>Correct value for p Summing 3 binomial probs o.e Correct unsimplified answer Correct answer</p>
<p>2 $P(\text{pencil case} \mid \text{find}) =$ $\frac{P(\text{pencilcase and find})}{P(\text{find})} = \frac{0.7 \times 1}{0.7 + 0.3 \times 0.2}$ $= 0.921$</p>	<p>M1 A1 A1 A1 [4]</p>	<p>Attempt to use cond prob formula, must be quotient Correct num of a fraction Correct denominator Correct answer</p>
<p>3 (i) $P(\text{any other number}) = 9/70$ $P(X < 2) = 27/70 + 1/10$ $= 34/70$ (17/35) (0.486)</p> <hr/> <p>(ii) $E(X) = 108/70$ (54/35) (1.543) $\text{Var}(X) = ((-2)^2 + \dots + 5^2) \times 9 / 70 - (54/35)^2$ $= 5.33$</p> <hr/> <p>(iii) $a = 1$</p>	<p>B1 B1 ft [2] M1 M1 A1 [3] B1 [1]</p>	<p>9/70 Seen Ft their probs if < 1 Valid attempt at $E(X)$ (needn't be accurate) Using a variance formula correctly with mean² subtracted numerically, no extra division Correct final answer</p>
<p>4 (i) Options 5 bat 5 bl 1 Wk in ${}^{10}C_5 \times {}^9C_5 \times {}^2C_1 = 63504$ ways or 5 bat 4 bl 2 Wk in ${}^{10}C_5 \times {}^9C_4 \times {}^2C_2 = 31752$ ways or 6 bat 4 bl 1 Wk in ${}^{10}C_6 \times {}^9C_4 \times {}^2C_1 = 52920$ ways Total = 148176 (148000)</p> <hr/> <p>(ii) $\frac{11!}{5!4!2!} = 6930$</p> <hr/> <p>(iii) Omit a pen $\frac{10!}{4!4!2!} = 3150$ Omit a diary $\frac{10!}{5!3!2!} = 2520$ Omit a notebook $\frac{10!}{5!4!} = 1260$ Total = 6930</p>	<p>M1 M1 A1 A1 [4] B1 [1] M1 B1 A1 [3]</p>	<p>Multiplying three combinations together Summing more than one sensible option Two options correct unsimplified Correct final answer Correct answer evaluated Summing three options One option correct Correct final answer</p>

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<p>5 (a) $z > \frac{2\mu - \mu}{\sigma} = \frac{\mu}{\sigma} = \frac{7\sigma^2}{3\sigma}$</p> $\frac{7\sigma}{3} = 1.272$ $\sigma = 0.545$ $\mu = 0.693$	<p>M1</p> <p>M1</p> <p>B1</p> <p>A1</p> <p>[4]</p>	<p>Standardising attempt resulting in $z > \text{some } \mu/\sigma$</p> <p>Substituting to eliminate μ or σ</p> <p>1.272 seen</p> <p>Both answers correct</p>
<p>(b) $P(X < a + 33) = 0.75$</p> $z = 0.674$ $\frac{a + 33 - 33}{\sqrt{21}} = 0.674$ $a = 3.09$	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>[4]</p>	<p>Using 0.75 oe</p> <p>± 0.674 seen</p> <p>Standardising, no cc, must have sq rt</p> <p>Correct answer</p>
<p>6 (i)</p>  <p>Median 270</p>	<p>M1</p> <p>M1 (Indpt)</p> <p>A1</p> <p>[3]</p>	<p>Sensible attempt at graph using u.c.b.</p> <p>2500 seen in median attempt on a CF graph</p> <p>Can be implied</p> <p>Correct answer + or – 5</p>
<p>(ii) 20% less than 160</p>	<p>M1</p> <p>A1</p> <p>[2]</p>	<p>Using 20%</p> <p>Correct answer + or – 5</p>
<p>(iii) $2100 - 1600 = 500$</p>	<p>B1</p> <p>[1]</p>	
<p>(iv) $(50.5 \times 200 + 125.5 \times 600 + 175.5 \times 800 + 225.5 \times 500 + 300.5 \times 2000 + 400.5 \times 600 + 525.5 \times 300) / 5000$</p> $= 268$	<p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>[4]</p>	<p>Using an attempt at mid-points</p> <p>Using an attempt at frequencies</p> <p>Correct mid-points or frequencies</p> <p>Correct answer only</p>
<p>7 (a) (i) $P(\text{at least one 3}) = 1 - P(\text{no 3s})$</p> $= 1 - (5/6)^9$ $= 0.806$	<p>M1</p> <p>A1</p> <p>[2]</p>	<p>Using $1 - \text{none}$</p> <p>Correct answer</p>
<p>(ii) $P(\text{at least 1 three}) = 1 - (5/6)^n$</p> $1 - (5/6)^n > 0.9$ $n > 12.6$ $n = 13$	<p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>[4]</p>	<p>Equation or inequality involving n and 0.9</p> <p>Solving attempt of sensible equation, can be trial</p> <p>Correct answer</p>
<p>(b) $P(\text{R wins his 1st ball}) = P(\text{GY})$</p> $= 15/56 (0.268)$ $P(\text{R wins 2nd ball}) = P(\text{GGGY}) = 3/28$ $P(\text{R wins 3rd ball}) = P(\text{GGGGY})$ $\frac{5}{8} \times \frac{4}{7} \times \frac{3}{6} \times \frac{2}{5} \times \frac{1}{4} \times \frac{3}{3} = 1/56$ $P(\text{R wins}) = 11/28 (0.393)$	<p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>[4]</p>	<p>Using $P(\text{GY})$</p> <p>Attempt to find $P(\text{GGGY})$ or $P(\text{GGGGY})$</p> <p>Adding three options</p> <p>Correct answer</p>