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| $\begin{aligned} & 1 \begin{array}{l} { }^{13} \mathrm{C}_{3} \times{ }^{39} \mathrm{C}_{4} \\ { }^{52} \mathrm{C}_{7} \end{array} \\ & =0.176 \\ & \text { OR P(RRR) }= \\ & \frac{13}{52} \times \frac{12}{51} \times \frac{11}{50} \times \frac{39}{49} \times \frac{38}{48} \times \frac{37}{47} \times \frac{36}{46} \times{ }^{7} \mathrm{C}_{3} \\ & =0.176 \end{aligned}$ | M1 <br> M1 <br> A1 <br> M1 <br> M1 <br> A1 <br> [3] | Using combinations with attempt to evaluate product of 2 in num and only 1 in denom Correct numerator or denominator <br> Correct answer <br> OR Multiplying 3 unequal red probs with 4 unequal non-red probs <br> Multiplying a probability by ${ }^{7} \mathrm{C}_{3}$ <br> Correct answer |
| :---: | :---: | :---: |
| $\begin{aligned} 2 \quad \text { (i) } \quad & \bar{x}=130-287 / 82 \\ = & 126.5(126,127) \mathrm{cm} \end{aligned}$ | M1 <br> A1 <br> [2] | 287/82 seen added or subt to 130 OR 287 seen added or subt to $82 \times 130$ Correct answer |
| (ii) $\frac{\Sigma(x-130)^{2}}{82}-\left(-3.5^{2}\right)=6.9^{2}$ $\Sigma(x-130)^{2}=4908.5 \mathrm{~cm}(4910)$ | M1 <br> A1 <br> [2] | $6.9^{2}+( \pm \text { their coded mean })^{2}$ seen or implied <br> correct answer |
| $\begin{aligned} 3 & \text { (i) } \end{aligned} \begin{aligned} & \mathrm{P}(>5)={ }^{7} \mathrm{C}_{6}(0.6)^{6}(0.4)+(0.6)^{7} \\ & =0.1306+0.02799 \\ & =0.159 \end{aligned}$ | M1 <br> A1 <br> [2] | Summing 2 or 3 binomial probs of the form ${ }^{7} \mathrm{C}_{r}(0.6)^{r}(0.4)^{7-r}$ <br> Correct answer |
| $\text { (ii) } \begin{aligned} & \mathrm{P}(\text { bark })=\mathrm{P}(\text { park, bark })+\mathrm{P}(\text { not park, bark }) \\ = & 0.6 \times 0.35+0.4 \times 0.75 \\ = & 0.51 \end{aligned}$ | M1 <br> A1 <br> [2] | Summing two appropriate 2-factor probabilities Correct answer |
| (iii) Variance (number of times) $=7.2$ | B1 | Correct final answer |


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4 (i) ends cola, $5!/ 2!2!=30$
ends green tea, $5!/ 3!2!=10$
ends orange juice, $5!/ 3!2!=10$
total $=50$ ways
OR $\mathrm{P}($ ends same $)=\frac{3}{7} \times \frac{2}{6}+\frac{2}{7} \times \frac{1}{6}+\frac{2}{7} \times \frac{1}{6}$
$=\frac{5}{21}$
$\frac{5}{21} \times \frac{7!}{3!2!2!}=50$ ways
(ii) colas together, no restrictions, $5!/ 2!2$ !
$=30$ ways
colas together and green tea together, $4!/ 2$ !
$=12$ ways
$30-12=18$ ways.
$\mathbf{O R} \mathbf{1}_{1}$ Attempt to list
$\mathbf{O R}_{2} 3 \times \frac{4 \times 3}{2}=18$
$5 \quad$ (i) $\quad \mathrm{P}(2)=\mathrm{P}(0,2)+\mathrm{P}(2,0)$
$=6 / 10 \times 3 / 7+3 / 10 \times 4 / 7$
$=30 / 70=3 / 7 \mathrm{AG}$
(ii)

| $x$ | 0 | 2 | 4 | 6 |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{P}(X=x)$ | $24 / 70$ | $30 / 70$ | $13 / 70$ | $3 / 70$ |

(iii) $\mathrm{E}(X)=13 / 7$
$\operatorname{Var}(X)=120 / 70+208 / 70+108 / 70-(13 / 7)^{2}$
$=2.78$
(iv) $\mathrm{P}(\mathrm{A} 2 \mid$ Sum 2$)=\frac{3 / 10 \times 4 / 7}{30 / 70}$
$=0.4$

M1 $\quad$ Considering all three options
A1 Any one option correct
A1 Correct answer

M1 OR Considering all three options

A1 Correct fraction

A1 Correct answer

A1

A1

B1

B1ft
M1
A1

A1

M1A1 $\mathbf{O R}_{\mathbf{1}} 10$ or more, 12 or more correct
M1A1 14 or more, 16 or more correct
A1 18 correct

A1 3 ways for colas and orange juice
M1 Considering green teas not together
A1 $\quad 4 \times 3$ or $(4 \times 3) / 2$
[5]
M1 Summing two 2-factor probabilities

B1 Correct values for rv $X$
[2]
[3]

M1 Correct numerator with a $0<$ denom $<1$
Considering all colas together, or 5 ! seen
Correct answer
Considering all colas tog and all green tea tog, or 4! seen
Correct answer
Correct final answer

Correct final answer

Correct answer legit obtained
[2]

Correct probs

Using variance formula correctly with mean ${ }^{2}$
subtracted numerically, no extra division
Correct final answer

Correct answer

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| 6 (i) for $X$ : Median $=0.825 \mathrm{~cm}$ <br> IQ range $=0.019 \mathrm{~cm}(0.833-0.814)$ | B1 <br> B1 <br> [2] | Correct median Correct IQ range |
| :---: | :---: | :---: |
| (ii) $q=4$ $r=2$ <br> SR $q=0.824$ and $r=0.852$ | B1 | Must be 4 and 2 not 3 and 1 |
| (iii) | B1 <br> B1ft <br> B1ft <br> B1 <br> [4] | Labels $X, Y$ and length $/ \mathrm{cm}$, linear scale from 0.80 to 0.87 and both on one diagram <br> Correct median and quartiles for $X \mathrm{ft}$ theirs must be a box <br> Correct median and quartiles for $Y \mathrm{ft}$ theirs must be a box <br> Whiskers correct no line through middle |
| (iv) $Y$ has longer insects on average Y has larger range | B1 B1 <br> [2] | Correct statement about lengths Correct statement about spreads |
| $\begin{gathered} 7 \text { (i) } 0.431=\frac{135-\mu}{\sigma} \\ \\ -0.842=\frac{127-\mu}{\sigma} \\ \\ \sigma=6.29 \\ \mu=132 \end{gathered}$ | B1 <br> B1 <br> M1 <br> A1 <br> A1 <br> [5] | One $\pm z$-value correct, accept 0.430 <br> A second $\pm z$-value correct <br> Solving two equations relating $\mu, \sigma, 135$, <br> 127 and their $z$-values (must be $z$-values) <br> Correct answer accept 6.28 <br> Correct answer |
| $\text { (ii) } \begin{aligned} & \mathrm{P}(X<145)=\mathrm{P}\left(z<\frac{145-132.3}{6.284}\right) \\ = & \mathrm{P}(z<2.023) \\ & =0.978 \end{aligned}$ | M1 <br> M1 <br> A1 <br> [3] | Standardising no sq rt no cc <br> Correct use of normal tables <br> Answer rounding to 0.978 or 0.979 |
| $\text { (iii) } \begin{aligned} & p=1 / 3 \\ & \mathrm{P}(\text { at least } 2)=1-\mathrm{P}(0,1) \\ &= 1-\left[(2 / 3)^{8}+{ }^{8} \mathrm{C}_{1} \times(1 / 3)^{1}(2 / 3)^{7}\right] \\ &=0.805 \end{aligned}$ | M1 <br> A1 <br> A1 <br> [3] | Binomial expression with powers summing to 8 and ${ }^{8} \mathrm{C}_{\text {something. }}$ (any $p$ ) Correct unsimplified expression <br> Answer rounding to 0.805 |

