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<p>1 c of m of arc = $20\sin(\pi/2)/(\pi/2)$</p> <p>$(2 + 0.9)\bar{x} = 2 \times 20\sin(\pi/2)/(\pi/2)$</p> <p>Distance is 8.78cm</p>	<p>B1 M1 A1 A1 [4]</p>	<p>For attempting to take moments about the diameter</p>
<p>2 (i)</p> <p>$\tan 35^\circ = r/7.5$</p> <p>$r = 5.25$</p>	<p>M1 A1ft A1 [3]</p>	<p>For using the idea that the c.m. is vertically above the lowest point of contact ft using their c of m from the base</p>
<p>(ii) [$\mu mg \cos 35^\circ > mg \sin 35^\circ$]</p> <p>$\mu > \tan 35^\circ \rightarrow$ Coefficient is greater than 0.7</p>	<p>M1 A1 [2]</p>	<p>For using 'no sliding $\rightarrow \mu R >$ weight component' Do not allow $\mu \geq 0.7$ AG</p>
<p>3 (i) $mg = T \cos \theta$</p> <p>$ma = T \sin \theta$</p> <p>$\tan \theta = a/g = 0.75$</p> <p>$T = 0.24 \times 10 / \cos \theta = 3$</p>	<p>B1 B1 B1 B1 [4]</p>	<p>SR B1 not B2 for $\tan \theta = v^2/gr$ or a/g used AG For using $T \cos \theta = mg$ to find T</p>
<p>(ii) [$v^2 = 7.5 \times 2 \sin \theta$]</p> <p>Speed is 3ms^{-1}</p>	<p>M1 A1 [2]</p>	<p>For using $v^2 = ar$ to find v</p>
<p>4 Weight split is 9N:6N</p> <p>For lamina $9 \times 0.75 + 6 \times 0.5$</p> <p>$= T \times 1.5 \sin 30^\circ$</p> <p>Tension is 13N</p> <p>Alternatively</p> <p>$[(1.5^2 + \frac{1}{2} 1.5 \times 2)\bar{x} = 1.5^2 \times 0.75 + \frac{1}{2} 1.5 \times 2 \times 0.5]$</p> <p>$\bar{x} = 0.65$</p> <p>$15 \times 0.65 = T \times 1.5 \sin 30^\circ$</p> <p>Tension is 13N</p>	<p>B1 M1 A1ft A1 A1 [5]</p> <p>M1 A1 M1 A1ft A1 [5]</p>	<p>For taking moments about A</p> <p>For using $A\bar{x} = A_1x_1 + A_2x_2$</p> <p>For taking moments about A</p>

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<p>5 (i) $7 = 16\tan\theta - 10 \times 16^2 / (2 \times 20^2) \cos^2\theta$ $[7 = 16T - 3.2(1 + T^2)]$</p> <p>$3.2T^2 - 16T + 10.2 = 0$ $T = \frac{3}{4}, 17/4$</p>	<p>B1 M1 A1 A1 [4]</p>	<p>For using $\cos\theta = 1/\sec\theta$ and the given identity to obtain a quadratic in $T(\tan\theta)$ AEF AG</p>
<p>(ii) $[x = \tan\theta \cos^2\theta / 0.0125 \text{ or } x = 20^2 \sin 2\theta / g]$</p> <p>For $\tan\theta = 0.75$, distance is 38.4 m For $\tan\theta = 4.25$, distance is 17.8 m</p>	<p>M1 A1 A1 [3]</p>	<p>For solving $y = 0$ for x or for using $R = V^2 \sin 2\theta / g$</p>
<p>(iii) For sketching two parabolic arcs which intersect once, both starting at the origin, each with $y \geq 0$ throughout, and each returning to the x-axis, the arc for which the angle of projection is smaller having the greater range. The ranges appear significantly greater than x at the intersection, and slightly greater, respectively.</p>	<p>B1 B1 [2]</p>	
<p>6 (i) $[0.35g = 2T\{0.7 / (2.4^2 + 0.7^2)^{1/2}\}]$ Tension is 6.25N $[6.25 = \lambda \times \frac{1}{4}]$ Modulus is 25N</p>	<p>M1 A1 M1 A1 [4]</p>	<p>For resolving forces on P vertically For using $T = \lambda x / L$ AG</p>
<p>(ii) EE on release = $25 \times 2^2 / (2 \times 4)$ EE when P is at M = $25 \times 0.8^2 / (2 \times 4)$</p> <p>$25 \times 2^2 / (2 \times 4) = 0.35g \times 1.8 + 25 \times 0.8^2 / (2 \times 4) + \frac{1}{2} 0.35v^2$ Speed is 4.90ms^{-1}</p>	<p>M1 A1 A1 M1 A1 A1 [6]</p>	<p>For using $EE = \lambda x^2 / 2L$ For using $EE \text{ on release} = mgh + EE$ when P is at M + $\frac{1}{2} mv^2$</p>
<p>7 (i) $[0.25v(dv/dx) = -(5 - x)]$</p> <p>$[\int v dv = 4 \int (x - 5) dx]$</p> <p>$v^2/2 = 4(x - 5)^2/2 (+ A)$</p> <p>$v^2 = 4(x - 5)^2$ Selects correct square root to obtain $v = 10 - 2x$</p>	<p>B1 M1 A1 M1 A1 A1 [6]</p>	<p>For using Newton's second law and $a = v(dv/dx)$ For separating variables and attempting to integrate For using $v(0) = 10$ Any correct expression in x AG</p>
<p>(ii) $[\int \frac{dx}{10 - 2x} = \int dt]$</p> <p>$-\frac{1}{2} \ln(10 - 2x) = t(-\frac{1}{2} \ln B)$ B = 10 (or equivalent) $x = 5(1 - e^{-2t})$ $0 < e^{-2t} < 1$ for all $t \rightarrow x < 5$ for all t</p>	<p>M1 A1 A1 B1ft B1 [5]</p>	<p>For using $v = dx/dt$ and separating variables ft $x = (B/2)(1 - e^{-2t})$ AG</p>