

Question	Answer	Marks	Guidance
1	$(\lambda =) \frac{5}{12} = 0.417$ or better	B1	
	$1 - e^{-\frac{5}{12}} (1 + \frac{5}{12})$	M1	1 – P($X = 0$ or 1), by Poisson, using any λ , allow 1 – P($X = 0$ or 1 or 2) for M1
	= 0.0661 or 0.0662 (3 sf)	A1	Final answer SC use of Binomial (from 0.06607...) B1 only
		3	

Question	Answer	Marks	Guidance
2	$2 \times z \times \frac{3.2}{10} = 1.25$	M1	OE Allow without '2 ×'
	$z = 1.953$	A1	SOI
	$\Phi(\text{'their } 1.953\text{'}) (= 0.9746)$	M1	
	$= 1 - 2(1 - \text{'0.9746'})$ $= 0.9492$	M1	OE
	$\alpha = 94.9$ or 95	A1	CWO
		5	

Question	Answer	Marks	Guidance
3(a)	$\text{est } (\mu) = 37.6 \text{ or } \frac{1504}{40} \text{ or } \frac{188}{5}$	B1	
	$\text{est } (\sigma^2) = \frac{40}{39} \left[\frac{57760}{40} - 37.6^2 \right] = 31.0154 = \frac{2016}{65}$	M1	Correct substitution in any correct formula $\frac{1}{39} \left[57760 - \frac{1504^2}{40} \right]$
	$= 31.0(0) \text{ (3 sf)}$	A1	Accept $\frac{2016}{65}$ or $31\frac{1}{65}$
		3	
3(b)	$H_0: \text{Pop mean (or } \mu) = 39.2$ $H_1: \text{Pop mean (or } \mu) < 39.2$	B1	Both. Not just ‘mean’
	$\frac{37.6 - 39.2}{\frac{\sqrt{31.0154}}{\sqrt{40}}}$	M1	Allow use of biased variance (30.2), must have $\sqrt{40}$
	$= -1.817$	A1	SC FT use of biased = -1.840 for A1
	‘1.817’ > 1.645 OE	M1	Valid comparison ‘ <i>their</i> 1.817’ with 1.645 or valid area comparison $0.0346 < 0.05$ OE
	There is evidence that mean time has decreased	A1FT	FT <i>their</i> 1.817; in context, not definite, no contradictions SC For 2 tail test: $H_1: \mu \neq 39.2$ and comp 1.96, max B0M1A1M1A0 (no FT for final mark)
		5	

Question	Answer	Marks	Guidance
4(a)	$\lambda (= 0.4 \times 365 \div 50) = 2.92$	B1	
	$e^{-2.92}(1 + 2.92 + \frac{2.92^2}{2})$	M1	Any λ . Allow one end error
	$= 0.441$ (3 sf)	A1	
		3	
4(b)	$e^{-\lambda} > 0.95$	M1	Allow '=' throughout
	$-\lambda > \ln 0.95$ or $\lambda < 0.051293$ OE	M1	Attempt ln both sides
	'0.051293' $\times 50 \div 0.4 (= 6.411)$	M1	
	Largest n is 6 (3 sf) Allow $n = 6$ or $n \leq 6$ (NOT $n < 6$ or $n \geq 6$ as final answer)	A1	SC Trial and Improvement M1 for $e^{-\lambda} > 0.95$ SOI; M1 for $\lambda = n \times \frac{0.4}{50}$; M1 for use of both $n = 6$ giving 0.9531 and $n = 7$ giving 0.9455; A1 $n = 6$
		4	

Question	Answer	Marks	Guidance
5(a)	$\frac{3}{4000} \int_5^{10} (100 - x^2) dx$ $= \frac{3}{4000} [100x - \frac{x^3}{3}]_5^{10}$	M1	Attempt integration of f(x), ignore limits. Condone omission of $\frac{3}{4000}$
	$= \frac{3}{4000} (1000 - \frac{1000}{3} - 500 + \frac{125}{3})$	M1	Correct limits 5 and 10. OE SOI
	$= 0.156$ (3 sf) or $\frac{5}{32}$	A1	For fully correct working seen including substitution of limits
		3	
5(b)	$\frac{3}{4000} \int_p^{10} (100 - x^2) dx = \frac{1}{4}$	M1	Attempt integration of f(x) with any limits and $= \frac{1}{4}$ or $= \frac{3}{4}$ seen. Condone omission of $\frac{3}{4000}$
	$\frac{3}{4000} [100x - \frac{x^3}{3}]_p^{10} = \frac{1}{4}$	A1	Correct integration with correct limits seen (or implied for limits p and 10) and $= \frac{1}{4}$ OE Condone omission of $\frac{3}{4000}$
	$\frac{3}{4000} (1000 - \frac{1000}{3} - 100p + \frac{p^3}{3}) = \frac{1}{4}$	M1	Attempt substitution correct limits in their integration of f(x). Accept limits 0 to p if clearly seen, accept limits -10 and p. Substitution must be seen.
	e.g. $\frac{2000}{3} - 100p + \frac{p^3}{3} = \frac{1000}{3}$ $p^3 - 300p + 1000 = 0$	A1	AG No errors seen
		4	

Question	Answer	Marks	Guidance
5(c)	Curve is symmetrical about $x = 0$	B1	May be implied by sketch. No contradictions or integrate $f(x)$ between $-q$ and $+q$ and equate to 0.5 leading to $q^3 - 300q + 1000 = 0$ oe
	$q = 3.47$	B1	
		2	

Question	Answer	Marks	Guidance
6(a)	$N(310, 50)$	B1	SOI
	$\frac{300-310}{\sqrt{50}}$ ($= -1.414$)	M1	Standardise using their values
	$\Phi(-1.414) = 1 - \phi(1.414)$	M1	Area consistent with their values
	$= 0.0786$ or 0.0787 (3 sf)	A1	As final answer
		4	

Question	Answer	Marks	Guidance
6(b)	$P(L - 2S > 0)$	M1	OE SOI
	$E(X) = 200 - 2 \times 110$ or $= -20$	B1	OE seen
	$\text{Var} = 30 + 2^2 \times 20$ or $= 110$	B1	Seen
	$N(-20, 110)$ $\frac{0 - (-20)}{\sqrt{110}}$ ($= 1.907$)	M1	Standardising with their values. Mean and variance must come from a combination attempt.
	$1 - \Phi(1.907)$	M1	Correct area consistent with their working
	$= 0.0283$ (3 sf)	A1	Final answer
		6	

Question	Answer	Marks	Guidance
7(a)	$P(X \leq n)$ ($n \leq 20$) attempted, using $B(20, 0.95)$	M1	OE
	$P(X \leq 17)$ or $P(X \leq 16)$ attempted, using $B(20, 0.95)$	M1	OE
	$(P(X \leq 17)) = 0.0755$ and $(P(X \leq 16)) = 0.0159$	A1	OE (0.925 and 0.984) both correct
	Rej region is $X \leq 16$ or $X < 17$	A1	Dependent on M1M1 and previous answers correct to at least 0.075/0.076 and 0.016 or 0.92/0.93 and 0.98 Correct unsupported answers of 0.0755 and 0.0159 OE scores M1 M1 A0
		4	

Question	Answer	Marks	Guidance
7(b)	0.0159	B1	FT <i>their</i> rejection region, from Binomial in a , if $P(X \text{ in rejection region}) < 0.025$
		1	
7(c)	Use of B(20, 0.7)	M1	
	$P(X > 16 \mid p = 0.7)$	M1	Correct method using B(20, 0.7)
	= 0.107	A1	
		3	