| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 1(a) | Make a recognisable sketch graph of $y=\|x-2\|$ | B1 |  |
|  |  | 1 |  |
| 1(b) | Find $x$-coordinate of intersection with $y=3 x-4$ | M1 |  |
|  | Obtain $x=\frac{3}{2}$ | A1 |  |
|  | State final answer $x>\frac{3}{2}$ only | A1 |  |
|  | Alternative method for question 1(b) |  |  |
|  | Solve the linear inequality $3 x-4>2-x$, or corresponding equation | M1 |  |
|  | Obtain critical value $x=\frac{3}{2}$ | A1 |  |
|  | State final answer $x>\frac{3}{2}$ only | A1 |  |
|  | Alternative method for question 1(b) |  |  |
|  | Solve the quadratic inequality $(x-2)^{2}<(3 x-4)^{2}$, or corresponding equation | M1 |  |
|  | Obtain critical value $x=\frac{3}{2}$ | A1 |  |
|  | State final answer $x>\frac{3}{2}$ only | A1 |  |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| 2 | Use law of logarithm of a power and sum and remove logarithms | M1 |  |
|  | Obtain a correct equation in any form, e.g. $3(2 x+5)=(x+2)^{2}$ | A1 |  |
|  | Use correct method to solve a 3-term quadratic, obtaining at least one root | M1 |  |
|  | Obtain final answer $x=1+2 \sqrt{3}$ or $1+\sqrt{12}$ only | A1 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 3(a) | Sketch the graph $y=\sec x$ | M1 |  |
|  | Sketch the graph $y=2-\frac{1}{2} x$, and justify the given statement | A1 |  |
|  |  | 2 |  |
| 3(b) | Calculate the values of a relevant expression or pair of expressions at $x=0.8$ and $x=1$ | M1 |  |
|  | Complete the argument correctly with correct calculated values | A1 |  |
|  |  | 2 |  |
| 3(c) | Use the iterative formula correctly at least once | M1 |  |
|  | Obtain final answer 0.88 | A1 |  |
|  | Show sufficient iterations to $4 \mathrm{~d} . \mathrm{p}$. to justify 0.88 to $2 \mathrm{~d} . \mathrm{p}$., or show there is a sign change in the interval $(0.875,0.885)$ | A1 |  |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 4 | Integrate by parts and reach $a x \tan x+b \int \tan x \mathrm{~d} x$ | M1* |  |
|  | Obtain $x \tan x-\int \tan x \mathrm{~d} x$ | A1 |  |
|  | Complete the integration, obtaining a term $\pm \ln \cos x$, or equivalent | M1 |  |
|  | Obtain integral $x \tan x+\ln \cos x$, or equivalent | A1 |  |
|  | Substitute limits correctly, having integrated twice | DM1 |  |
|  | Use a law of logarithms | M1 |  |
|  | Obtain answer $\frac{5}{18} \sqrt{3} \pi-\frac{1}{2} \ln 3$, or exact simplified equivalent | A1 |  |
|  |  | 7 |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| $5(\mathrm{a})$ | Express LHS correctly as a single fraction | B1 |  |
|  | Use $\cos (A \pm B)$ formula to simplify the numerator | M1 |  |
|  | Use $\sin 2 A$ formula to simplify the denominator | M1 |  |
|  | Obtain the given result. | A1 |  |
|  |  | $\mathbf{4}$ |  |


| Question | Answer | Marks |  |
| :---: | :--- | ---: | ---: |
|  | Obtain an equation in $\tan 2 x$ and use correct method to solve for $x$ | M1 |  |
|  | Obtain answer, e.g. 0.232 | $\mathbf{A 1}$ |  |
|  | Obtain second answer, e.g. 1.80 | A1 | Ignore answers outside the given interval. |
|  |  | $\mathbf{3}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 6(a) | Separate variables correctly and attempt integration of at least one side | B1 |  |
|  | Obtain term of the form $a \tan ^{-1}(2 y)$ | M1 |  |
|  | Obtain term $\frac{1}{2} \tan ^{-1}(2 y)$ | A1 |  |
|  | Obtain term $-\mathrm{e}^{-x}$ | B1 |  |
|  | Use $x=1, y=0$ to evaluate a constant or as limits in a solution containing terms of the form $a \tan ^{-1}(b y)$ and $c \mathrm{e}^{ \pm x}$ | M1 |  |
|  | Obtain correct answer in any form | A1 |  |
|  | Obtain final answer $y=\frac{1}{2} \tan \left(2 \mathrm{e}^{-1}-2 \mathrm{e}^{-x}\right)$, or equivalent | A1 |  |
|  |  | 7 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | ---: | :--- |
| $6(\mathrm{~b})$ | State that $y$ approaches $\frac{1}{2} \tan \left(2 \mathrm{e}^{-1}\right)$, or equivalent | B1FT | The FT is on correct work on a solution containing <br> $\mathrm{e}^{-x}$. |
|  |  | $\mathbf{1}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 7(a) | State or imply $3 y^{2}+6 x y \frac{\mathrm{~d} y}{\mathrm{~d} x}$ as derivative of $3 x y^{2}$ | B1 |  |
|  | State or imply $3 y^{2} \frac{\mathrm{~d} y}{\mathrm{~d} x}$ as derivative of $y^{3}$ | B1 |  |
|  | Equate attempted derivative of LHS to zero and solve for $\frac{\mathrm{d} y}{\mathrm{~d} x}$ | M1 | Need to see $\frac{\mathrm{d} y}{\mathrm{~d} x}$ factorised out prior to AG |
|  | Obtain the given answer correctly | A1 | AG |
|  |  | 4 |  |
| 7(b) | Equate denominator to zero | *M1 |  |
|  | Obtain $y=2 x$, or equivalent | A1 |  |
|  | Obtain an equation in $x$ or $y$ | DM1 |  |
|  | Obtain the point (1,2) | A1 |  |
|  | State the point $(\sqrt[3]{5}, 0)$ | B1 | Alternatively (1.71, 0). |
|  |  | 5 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 8(a) | Obtain $\overrightarrow{O M}=2 \mathbf{i}+\mathbf{j}$ | B1 |  |
|  | Use a correct method to find $\overrightarrow{M N}$ | M1 |  |
|  | Obtain $\overrightarrow{M N}=-\mathbf{i}+2 \mathbf{j}+2 \mathbf{k}$ | A1 |  |
|  |  | 3 |  |
| 8(b) | Use a correct method to form an equation for $M N$ | M1 |  |
|  | Obtain $\mathbf{r}=2 \mathbf{i}+\mathbf{j}+\lambda(-\mathbf{i}+2 \mathbf{j}+2 \mathbf{k})$, or equivalent | A1 |  |
|  |  | 2 |  |
| 8(c) | Find $\overrightarrow{D P}$ for a point $P$ on $M N$ with parameter $\lambda$, e.g. $(2-\lambda, 1+2 \lambda,-2+2 \lambda)$ | B1 |  |
|  | Equate scalar product of $\overrightarrow{D P}$ and a direction vector for $M N$ to zero and solve for $\lambda$ | M1 |  |
|  | Obtain $\lambda=\frac{4}{9}$ | A1 |  |
|  | State that the position vector of $P$ is $\frac{14}{9} \mathbf{i}+\frac{17}{9} \mathbf{j}+\frac{8}{9} \mathbf{k}$ | A1 |  |
|  |  | 4 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 9(a) | State or imply the form $\frac{A}{1+2 x}+\frac{B}{1-2 x}+\frac{C}{2+x}$ | B1 |  |
|  | Use a correct method for finding a constant | M1 |  |
|  | Obtain one of $A=-2, B=1$ and $C=4$ | A1 |  |
|  | Obtain a second value | A1 |  |
|  | Obtain the third value | A1 |  |
|  |  | 5 |  |
| 9(b) | Use correct method to find the first two terms of the expansion of $(1+2 x)^{-1}$, $(1-2 x)^{-1},(2+x)^{-1} \text { or }\left(1+\frac{1}{2} x\right)^{-1}$ | M1 |  |
|  | Obtain correct unsimplified expansions up to the term in $x^{2}$ of each partial fraction | $\begin{array}{r} \text { A1FT } \\ + \text { A1FT } \\ + \text { A1FT } \end{array}$ | The FT is on $A, B$ and $C$. |
|  | Obtain final answer $1+5 x-\frac{7}{2} x^{2}$ | A1 |  |
|  |  | 5 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 10(a) | Solve for $v$ or $w$ | M1 |  |
|  | Use $\mathrm{i}^{2}=-1$ | M1 |  |
|  | Obtain $v=-\frac{2 \mathrm{i}}{1+\mathrm{i}}$ or $w=\frac{5+7 \mathrm{i}}{-1+\mathrm{i}}$ | A1 |  |
|  | Multiply numerator and denominator by the conjugate of the denominator | M1 |  |
|  | Obtain $v=-1-\mathrm{i}$ | A1 |  |
|  | Obtain $w=1-6 \mathrm{i}$ | A1 |  |
|  |  | 6 |  |
| 10(b)(i) | Show a circle with centre $2+3 \mathrm{i}$ | B1 |  |
|  | Show a circle with radius 1 and centre not at the origin | B1 |  |
|  |  | 2 |  |
| 10(b)(ii) | Carry out a complete method for finding the least value of $\arg z$ | M1 |  |
|  | Obtain answer $40.2^{\circ}$ or 0.702 radians | A1 |  |
|  |  | 2 |  |

