

Question	Answer	Marks	Guidance
1	$f'(x) = [-(3x+2)^{-2}] \times [3] + [2x]$	<b>B2, 1, 0</b>	
	$< 0$ hence decreasing	<b>B1</b>	Dependent on at least B1 for $f'(x)$ and must include $< 0$ or 'always neg'
		<b>3</b>	

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2	[Stretch] [factor 2, $x$ direction (or $y$ -axis invariant)]	<b>*B1 DB1</b>	
	[Translation or Shift] [1 unit in $y$ direction] <b>or</b> [Translation/Shift] $\begin{bmatrix} 0 \\ 1 \end{bmatrix}$	<b>B1B1</b>	Accept transformations in either order. Allow (0, 1) for the vector
		<b>4</b>	

Question	Answer	Marks	Guidance
3	$(\pi) \int (y-1) dy$	<b>*M1</b>	SOI Attempt to integrate $x^2$ or $(y-1)$
	$(\pi) \left[ \frac{y^2}{2} - y \right]$	<b>A1</b>	
	$(\pi) \left[ \left( \frac{25}{2} - 5 \right) - \left( \frac{1}{2} - 1 \right) \right]$	<b>DM1</b>	Apply limits $1 \rightarrow 5$ to an integrated expression
	$8\pi$ or AWRT 25.1	<b>A1</b>	
		<b>4</b>	

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4	$\frac{dy}{dx} = 2x - 2$	<b>B1</b>	
	$\frac{dy}{dx} = \frac{4}{6}$	<b>B1</b>	OE, SOI
	<i>their</i> $(2x - 2) = \textit{their} \frac{4}{6}$	<b>M1</b>	LHS and RHS must be <i>their</i> $\frac{dy}{dx}$ expression and value
	$x = \frac{4}{3}$ oe	<b>A1</b>	
		<b>4</b>	

Question	Answer	Marks	Guidance
5	$2 \tan \theta - 6 \sin \theta + 2 = \tan \theta + 3 \sin \theta + 2 \rightarrow \tan \theta - 9 \sin \theta (= 0)$	<b>M1</b>	Multiply by denominator and simplify
	$\sin \theta - 9 \sin \theta \cos \theta (= 0)$	<b>M1</b>	Multiply by $\cos \theta$
	$\sin \theta(1 - 9 \cos \theta) (= 0) \rightarrow \sin \theta = 0, \cos \theta = \frac{1}{9}$	<b>M1</b>	Factorise and attempt to solve at least one of the factors = 0
	$\theta = 0$ or $83.6^\circ$ (only answers in the given range)	<b>A1A1</b>	
		<b>5</b>	

Question	Answer	Marks	Guidance
6(a)	$5C2 [2(x)]^3 \left[ \frac{a}{(x^2)} \right]^2$	<b>B1</b>	SOI Can include correct $x$ 's
	$10 \times 8 \times a^2 \left( \frac{x^3}{x^4} \right) = 720 \left( \frac{1}{x} \right)$	<b>B1</b>	SOI Can include correct $x$ 's
	$a = \pm 3$	<b>B1</b>	
		<b>3</b>	
6(b)	$5C4 [2(x)] \left[ \frac{\text{their } a}{(x^2)} \right]^4$	<b>B1</b>	SOI <i>Their a</i> can be just <u>one</u> of their values (e.g. just 3). Can gain mark from within an expansion but must use <i>their</i> value of $a$
	810 identified	<b>B1</b>	Allow with $x^{-7}$
		<b>2</b>	

Question	Answer	Marks	Guidance
7	$OC = 6\cos 0.8 = 4.18(0)$	<b>M1A1</b>	SOI
	Area sector $OCD = \frac{1}{2}(\text{their } 4.18)^2 \times 0.8$	<b>*M1</b>	OE
	$\Delta OCA = \frac{1}{2} \times 6 \times \text{their } 4.18 \times \sin 0.8$	<b>M1</b>	OE
	Required area = <i>their</i> $\Delta OCA - \text{their sector } OCD$	<b>DM1</b>	SOI. If not seen <i>their</i> areas of sector and triangle must be seen
	2.01	<b>A1</b>	CWO. Allow or better e.g. 2.0064
		<b>6</b>	

Question	Answer	Marks	Guidance
8(a)	2%	<b>B1</b>	
		<b>1</b>	
8(b)	Bonus = $600 + 23 \times 100 = 2900$	<b>B1</b>	
	Salary = $30000 \times 1.03^{23}$	<b>M1</b>	Allow $30000 \times 1.03^{24}$ (60984)
	= 59207.60	<b>A1</b>	Allow answers of 3 significant figure accuracy or better
	$\frac{\text{their } 2900}{\text{their } 59200}$	<b>M1</b>	SOI
	4.9(0)%	<b>A1</b>	
		<b>5</b>	

Question	Answer	Marks	Guidance
9(a)	$[2(x+3)^2] [-7]$	<b>B1B1</b>	Stating $a=3, b=-7$ gets B1B1
		<b>2</b>	
9(b)	$y=2(x+3)^2-7 \rightarrow 2(x+3)^2=y+7 \rightarrow (x+3)^2=\frac{y+7}{2}$	<b>M1</b>	First 2 operations correct. Condone sign error or with $x/y$ interchange
	$x+3=(\pm)\sqrt{\frac{y+7}{2}} \rightarrow x=(\pm)\sqrt{\frac{y+7}{2}}-3 \rightarrow f^{-1}(x)=-\sqrt{\frac{x+7}{2}}-3$	<b>A1FT</b>	FT on <i>their</i> $a$ and $b$ . Allow $y = \dots$
	Domain: $x \geq -5$ or $\geq -5$ or $[-5, \infty)$	<b>B1</b>	Do not accept $y = \dots, f(x) = \dots, f^{-1}(x) = \dots$
		<b>3</b>	
9(c)	$fg(x) = 8x^2 - 7$	<b>B1FT</b>	SOI. FT on <i>their</i> $-7$ from part (a)
	$8x^2 - 7 = 193 \rightarrow x^2 = 25 \rightarrow x = -5$ only	<b>B1</b>	
	<b>Alternative method for question 9(c)</b>		
	$g(x) = f^{-1}(193) \rightarrow 2x - 3 = -\sqrt{100} - 3$	<b>M1</b>	FT on <i>their</i> $f^{-1}(x)$
	$x = -5$ only	<b>A1</b>	
		<b>2</b>	
9(d)	(Largest $k$ is) $-\frac{1}{2}$	<b>B1</b>	Accept $-\frac{1}{2}$ or $k \leq -\frac{1}{2}$
		<b>1</b>	

Question	Answer	Marks	Guidance
10(a)	$2(a+3)^{\frac{1}{2}} - a = 0$	<b>M1</b>	SOI. Set $\frac{dy}{dx} = 0$ when $x = a$ . Can be implied by an answer in terms of $a$
	$4(a+3) = a^2 \rightarrow a^2 - 4a - 12 = 0$	<b>M1</b>	Take $a$ to RHS and square. Form 3-term quadratic
	$(a-6)(a+2) \rightarrow a = 6$	<b>A1</b>	Must show factors, or formula or completing square. Ignore $a = -2$ <b>SC</b> If $a$ is never used maximum of M1A1 for $x = 6$ , with visible solution
		<b>3</b>	
10(b)	$\frac{d^2y}{dx^2} = (x+3)^{-\frac{1}{2}} - 1$	<b>B1</b>	
	Sub <i>their</i> $a \rightarrow \frac{d^2y}{dx^2} = \frac{1}{3} - 1 = -\frac{2}{3}$ ( <i>or</i> $< 0$ ) $\rightarrow$ MAX	<b>M1A1</b>	A mark only if completely correct If the second differential is not $-\frac{2}{3}$ correct conclusion must be drawn to award the M1
		<b>3</b>	
10(c)	$(y =) \frac{2(x+3)^{\frac{3}{2}}}{\frac{3}{2}} - \frac{1}{2}x^2 (+c)$	<b>B1B1</b>	
	Sub $x = \textit{their } a$ and $y = 14 \rightarrow 14 = \frac{4}{3}(9)^{\frac{3}{2}} - 18 + c$	<b>M1</b>	Substitute into an integrated expression. $c$ must be present. Expect $c = -4$
	$y = \frac{4}{3}(x+3)^{\frac{3}{2}} - \frac{1}{2}x^2 - 4$	<b>A1</b>	Allow $f(x) = \dots$
		<b>4</b>	

Question	Answer	Marks	Guidance
11(a)	$(\tan x - 2)(3 \tan x + 1) (= 0)$ . <b>or</b> formula <b>or</b> completing square	<b>M1</b>	Allow reversal of signs in the factors. Must see a method
	$\tan x = 2$ or $-\frac{1}{3}$	<b>A1</b>	
	$x = 63.4^\circ$ (only value in range) or $161.6^\circ$ (only value in range)	<b>B1FT</b> <b>B1FT</b>	
		<b>4</b>	
11(b)	Apply $b^2 - 4ac < 0$	<b>M1</b>	SOI. Expect $25 - 4(3)(k) < 0$ , $\tan x$ must not be in coefficients
	$k > \frac{25}{12}$	<b>A1</b>	Allow $b^2 - 4ac = 0$ leading to correct $k > \frac{25}{12}$ for M1A1
		<b>2</b>	
11(c)	$k = 0$	<b>M1</b>	SOI
	$\tan x = 0$ or $\frac{5}{3}$	<b>A1</b>	
	$x = 0^\circ$ or $180^\circ$ or $59.0^\circ$	<b>A1</b>	All three required
		<b>3</b>	

Question	Answer	Marks	Guidance
12(a)	Centre = (2, -1)	<b>B1</b>	
	$r^2 = [2 - (-3)]^2 + [-1 - (-5)]^2$ or $[2 - 7]^2 + [-1 - 3]^2$ OE	<b>M1</b>	OR $\frac{1}{2} [(-3 - 7)^2 + (-5 - 3)^2]$ OE
	$(x - 2)^2 + (y + 1)^2 = 41$	<b>A1</b>	Must not involve surd form <b>SCB3</b> $(x + 3)(x - 7) + (y + 5)(y - 3) = 0$
		<b>3</b>	
12(b)	Centre = <i>their</i> $(2, -1) + \begin{pmatrix} 8 \\ 4 \end{pmatrix} = (10, 3)$	<b>BIFT</b>	SOI FT on <i>their</i> (2, -1)
	$(x - 10)^2 + (y - 3)^2 = \textit{their} 41$	<b>BIFT</b>	FT on <i>their</i> 41 even if in surd form <b>SCB2</b> $(x - 5)(x - 15) + (y + 1)(y - 7) = 0$
		<b>2</b>	



Question	Answer	Marks	Guidance
12(c)	Gradient $m$ of line joining centres = $\frac{4}{8}$ OE	<b>B1</b>	
	Attempt to find mid-point of line.	<b>M1</b>	Expect (6, 1)
	Equation of $RS$ is $y - 1 = -2(x - 6)$	<b>M1</b>	Through <i>their</i> (6, 1) with gradient $\frac{-1}{m}$
	$y = -2x + 13$	<b>A1</b>	AG
	<b>Alternative method for question 12(c)</b>		
	$(x - 2)^2 + (y + 1)^2 - 41 = (x - 10)^2 + (y - 3)^2 - 41$ OE	<b>M1</b>	
	$x^2 - 4x + 4 + y^2 + 2y + 1 = x^2 - 20x + 100 + y^2 - 6y + 9$ OE	<b>A1</b>	Condone 1 error <b>or</b> errors caused by 1 error in the first line
	$16x + 8y = 104$	<b>A1</b>	
	$y = -2x + 13$	<b>A1</b>	AG
		<b>4</b>	
12(d)	$(x - 10)^2 + (-2x + 13 - 3)^2 = 41$	<b>M1</b>	Or eliminate $y$ between $C_1$ and $C_2$
	$x^2 - 20x + 100 + 4x^2 - 40x + 100 = 41 \rightarrow 5x^2 - 60x + 159 = 0$	<b>A1</b>	AG
		<b>2</b>	