

| Question | Answer                                                                                                                                        | Marks     | Guidance                                                                        |
|----------|-----------------------------------------------------------------------------------------------------------------------------------------------|-----------|---------------------------------------------------------------------------------|
| 1        | $x' = 24\cos 30 (= 12\sqrt{3})$                                                                                                               | <b>B1</b> | Use horizontal motion                                                           |
|          | $y' = 24\sin 30 - 4g (= -28)$                                                                                                                 | <b>B1</b> | Use vertical motion                                                             |
|          | $V^2 = (24\cos 30)^2 + (24\sin 30 - 4g)^2 = (12\sqrt{3})^2 + (-28)^2$<br>OR $\tan \alpha = (24\sin 30 - 4g)/(24\cos 30) = -28/(12\sqrt{3})^2$ | <b>M1</b> | Where V is the required speed<br>and $\alpha$ is the angle below the horizontal |
|          | $V = 34.9 \text{ m s}^{-1}$                                                                                                                   | <b>A1</b> |                                                                                 |
|          | $\alpha = 53.4^\circ$ below the horizontal                                                                                                    | <b>A1</b> |                                                                                 |
|          |                                                                                                                                               | <b>5</b>  |                                                                                 |

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|----------|------------------------------------------------------------------------------|-----------|-----------------------------------------|
| 2(i)     | Total volume $(= 27 + 8 + 1) = 36$                                           | <b>B1</b> |                                         |
|          | $36x = 27 \times 1.5 + 8 \times 4 + 1 \times 5.5$                            | <b>M1</b> | Take moments about base of largest cube |
|          | $x (= 13/6) = 2.17 \text{ m}$                                                | <b>A1</b> |                                         |
|          |                                                                              | <b>3</b>  |                                         |
| 2(ii)    | Mass of new cube $= 35 + m$                                                  | <b>B1</b> | Where m is the mass of the new cube     |
|          | $(35 + m) \times 3 = 27 \times 1.5 + 8 \times 4 + 5.5m$ (leads to $m = 13$ ) | <b>M1</b> | Take moments about base of largest cube |
|          | 13:1 or 1:13                                                                 | <b>A1</b> | Accept 13                               |
|          |                                                                              | <b>3</b>  |                                         |

| Question | Answer                                                                    | Marks     | Guidance                                                            |
|----------|---------------------------------------------------------------------------|-----------|---------------------------------------------------------------------|
| 3(i)     | $x = 4t$ and $y = 6t - 5t^2$                                              | <b>M1</b> | Use horizontal and vertical motion and attempt to eliminate t       |
|          | $y [= 6x/4 - 5(x/4)^2] = 1.5x - 5x^2/16$ or $1.5x - 0.3125x^2$            | <b>A1</b> |                                                                     |
|          |                                                                           | <b>2</b>  |                                                                     |
| 3(ii)    | $\tan\theta = 1.5$                                                        | <b>M1</b> | Use the trajectory equation from the formula sheet                  |
|          | $\theta = 56.3^\circ$                                                     | <b>A1</b> |                                                                     |
|          | $V^2 \cos^2 56.3 = 16$                                                    | <b>M1</b> | Again use the trajectory equation                                   |
|          | $V = 7.21 \text{ m s}^{-1}$                                               | <b>A1</b> |                                                                     |
|          | OR                                                                        |           |                                                                     |
|          | $V \cos\theta = 4$ and $V \sin\theta = 6$                                 | <b>M1</b> | Initial horizontal and vertical velocities                          |
|          | $V^2 \cos^2 \theta + V^2 \sin^2 \theta = 4^2 + 6^2$ OR $\tan\theta = 6/4$ | <b>M1</b> | Use Pythagoras's theorem or trigonometry of a right angled triangle |
|          | $V = 7.21 \text{ m s}^{-1}$                                               | <b>A1</b> |                                                                     |
|          | $\theta = 56.3^\circ$                                                     | <b>A1</b> |                                                                     |
|          | <b>4</b>                                                                  |           |                                                                     |

| Question | Answer                                  | Marks | Guidance              |
|----------|-----------------------------------------|-------|-----------------------|
| 4        | $T\cos 60 = 0.3g$                       | M1    | Resolve vertically    |
|          | $T = 6 \text{ N}$                       | A1    |                       |
|          | $T = 16e/0.8 (= 6)$ leads to $e = 0.3$  | M1    | Use $T = \lambda x/L$ |
|          | $r = (0.8 + 0.3)\sin 60 (= 1.1\sin 60)$ | A1    |                       |
|          | $T\sin 60 = 0.3 v^2 / (1.1\sin 60)$     | M1    | Use N2L horizontally  |
|          | $v = 4.06 \text{ m s}^{-1}$             | A1    |                       |
|          |                                         | 6     |                       |

| Question | Answer                                                                 | Marks | Guidance                                                                      |
|----------|------------------------------------------------------------------------|-------|-------------------------------------------------------------------------------|
| 5(i)     | $0.3g = 24e/0.6$                                                       | M1    | Note greatest speed occurs at the equilibrium position. Use $T = \lambda x/L$ |
|          | $e = 0.075 \text{ m}$                                                  | A1    | Fall = 0.275 m                                                                |
|          | PE Change = $0.3g \times 0.275$                                        | B1    |                                                                               |
|          | $0.3 v^2 / 2 = 0.3g \times 0.275 - 24 \times 0.075^2 / (2 \times 0.6)$ | M1    | Set up a 3 term energy equation                                               |
|          | $v = 2.18 \text{ m s}^{-1}$                                            | A1    |                                                                               |
|          |                                                                        | 5     |                                                                               |

| Question | Answer                                          | Marks | Guidance                                                         |
|----------|-------------------------------------------------|-------|------------------------------------------------------------------|
| 5(ii)    | $0.3g(0.2 + E) = 24 E^2 / (2 \times 0.6)$       | M1    | Set up an energy equation. Note $v = 0$ at the greatest distance |
|          | $20 E^2 - 3E - 0.6 = 0$                         | M1    | Attempt to solve a 3 term quadratic equation                     |
|          | $E = 0.264$ and so greatest distance is 0.864 m | A1    |                                                                  |
|          |                                                 | 3     |                                                                  |

| Question | Answer                                                             | Marks | Guidance                                               |
|----------|--------------------------------------------------------------------|-------|--------------------------------------------------------|
| 6(i)     | Area of hole = $\pi r^2$ and Area of original circle = $25\pi r^2$ | M1    |                                                        |
|          | Area of cross-section = $24\pi r^2$                                | A1    |                                                        |
|          | $\pi r^2 (2r) = 24\pi r^2 (d)$                                     | M1    | Take moments about the centre of the cylinder          |
|          | $d = r/12$ (= 0.083333...r)                                        | A1    |                                                        |
|          |                                                                    | 4     |                                                        |
| 6(ii)    | $P(2 \times 5r) = W(r/12)\cos 60$                                  | M1    | Take moments about the point of contact with the plane |
|          | $P = W\cos 60/120 = W/240 = 0.00417W$ (= F)                        | A1    |                                                        |
|          | $\mu = (W\cos 60/120)/W$                                           | M1    | Use $F = \mu R$ Note $R = W$ by resolving vertically   |
|          | $\mu = 1/240 = 0.00417$                                            | A1    |                                                        |
|          |                                                                    | 4     |                                                        |

| Question | Answer                                                                               | Marks       | Guidance                       |
|----------|--------------------------------------------------------------------------------------|-------------|--------------------------------|
| 7(i)     | $0.2mg = 0.06 \times 8$                                                              | <b>M1</b>   | Resolve along the plane        |
|          | $m = 0.24 \text{ kg}$ <b>AG</b>                                                      | <b>A1</b>   |                                |
|          |                                                                                      | <b>2</b>    |                                |
| 7(ii)    | $m \frac{dv}{dt} = 0.06t - 0.2mg$ or $0.24 \frac{dv}{dt} = 0.06t - 0.2 \times 0.24g$ | <b>M1</b>   | Use N2L along the plane        |
|          | $\frac{dv}{dt} = 0.25t - 2$ <b>AG</b>                                                | <b>A1</b>   |                                |
|          | $\int dv = \int (0.25t - 2) dt$                                                      | <b>M1</b>   | Attempt to integrate           |
|          | $v = 0.25t^2 / 2 - 2t + c$ , Put $v = 0$ and $t = 4$ ( leads to $c = 6$ )            | <b>M1</b>   | Attempt to find c              |
|          | Initial velocity = $6 \text{ m s}^{-1}$                                              | <b>A1</b>   |                                |
|          |                                                                                      | <b>5</b>    |                                |
| 7(iii)   | $x = \int (0.25t^2 / 2 - 2t + 6) dt$                                                 | <b>M1</b>   | Attempt to integrate           |
|          | $x = 0.25t^3 / 6 - t^2 + 6t (+ k)$                                                   | <b>A1ft</b> | ft candidates c from part (ii) |
|          | Finds or assumes $k = 0$ and substitutes $t = 4$ OR uses limits of 0 and 4           | <b>M1</b>   |                                |
|          | $OP = 32/3 = 10 \frac{2}{3} = 10.7 \text{ m}$                                        | <b>A1</b>   |                                |
|          |                                                                                      | <b>4</b>    |                                |