

Question	Answer	Marks	Guidance
1(i)	Use law for the logarithm of a product or quotient	M1	
	Use $\log_{10} 100 = 2$ or $10^2 = 100$	M1	
	Obtain $x^2 - 4x - 100 = 0$ , or equivalent	A1	
		3	
1(ii)	Solve a 3-term quadratic equation	M1	
	Obtain answer 12.2 only	A1	
		2	

Question	Answer	Marks	Guidance
2(i)	Use the iterative formula correctly at least once	M1	
	Obtain answer 1.3195	A1	
	Show sufficient iterations to 6 d.p. to justify 1.3195 to 4 d.p., or show there is a sign change in (1.31945, 1.31955)	A1	
		3	
2(ii)	State $x = \frac{2x^6 + 12x}{3x^5 + 8}$ , or equivalent	B1	
	State answer $\sqrt[5]{4}$ , or exact equivalent	B1	
		2	

Question	Answer	Marks	Guidance
3(i)	Use trig formulae and obtain an equation in $\sin \theta$ and $\cos \theta$	M1	
	Obtain a correct equation in any form	A1	
	Substitute exact trig ratios and obtain an expression for $\tan \theta$	M1	
	Obtain answer $\tan \theta = \frac{2\sqrt{2}-1}{1-\sqrt{6}}$ , or equivalent	A1	
		4	
3(ii)	State answer, e.g. $\theta = 128.4^\circ$	B1	
	State second answer, e.g. $\theta = 308.4^\circ$	B1 ft	
		2	

Question	Answer	Marks	Guidance
4	Integrate by parts and reach $ax^{-\frac{1}{2}} \ln x + b \int x^{-\frac{1}{2}} \cdot \frac{1}{x} dx$	M1*	
	Obtain $-2x^{-\frac{1}{2}} \ln x + 2 \int x^{-\frac{1}{2}} \cdot \frac{1}{x} dx$ , or equivalent	A1	
	Complete the integration, obtaining $-2x^{-\frac{1}{2}} \ln x - 4x^{-\frac{1}{2}}$ , or equivalent	A1	
	Substitute limits correctly, having integrated twice	M1(dep*)	
	Obtain the given answer following full and correct working	A1	
		5	

Question	Answer	Marks	Guidance
5	State $\cos y \frac{dy}{dx}$ as derivative of $\sin y$	<b>B1</b>	
	State correct derivative in terms of $x$ and $y$ , e.g. $\sec^2 x / \cos y$	<b>B1</b>	
	State correct derivative in terms of $x$ , e.g. $\frac{\sec^2 x}{\sqrt{1 - \tan^2 x}}$	<b>B1</b>	
	Use double angle formula	<b>M1</b>	
	Obtain the given answer correctly	<b>A1</b>	
		<b>5</b>	

Question	Answer	Marks	Guidance
6	Separate variables correctly and attempt integration of at least one side	B1	
	Obtain term $-\frac{1}{2y^2}$ , or equivalent	B1	
	Obtain term $-k e^{-x}$	B1	
	Use a pair of limits, e.g. $x = 0, y = 1$ to obtain an equation in $k$ and an arbitrary constant $c$	M1	
	Use a second pair of limits, e.g. $x = 1, y = \sqrt{e}$ , to obtain a second equation and solve for $k$ or for $c$	M1	
	Obtain $k = \frac{1}{2}$ and $c = 0$	A1	
	Obtain final answer $y = e^{\frac{1}{2}x}$ , or equivalent	A1	
		7	

Question	Answer	Marks	Guidance
7(a)	Use quadratic formula to solve for $z$	<b>M1</b>	
	Use $i^2 = -1$ throughout	<b>M1</b>	
	Obtain correct answer in any form	<b>A1</b>	
	Multiply numerator and denominator by $1 - i$ , or equivalent	<b>M1</b>	
	Obtain final answer, e.g. $1 - i$	<b>A1</b>	
	Obtain second final answer, e.g. $\frac{5}{2} + \frac{1}{2}i$	<b>A1</b>	
		<b>6</b>	
7(b)	Show the point representing $u$ in relatively correct position	<b>B1</b>	
	Show the horizontal line through $z = i$	<b>B1</b>	
	Show correct half-lines from $u$ , one of gradient 1 and the other vertical	<b>B1ft</b>	
	Shade the correct region	<b>B1</b>	
		<b>4</b>	

Question	Answer	Marks	Guidance
8(i)	State or imply the form $A + \frac{B}{2+x} + \frac{C}{3-2x}$	<b>B1</b>	
	Use a correct method for finding a constant	<b>M1</b>	
	Obtain one of $A = 2$ , $B = -4$ and $C = 6$	<b>A1</b>	
	Obtain a second value	<b>A1</b>	
	Obtain the third value	<b>A1</b>	
		<b>5</b>	
8(ii)	Use correct method to find the first two terms of the expansion of $(2+x)^{-1}$ or $(3-2x)^{-1}$ , or equivalent	<b>M1</b>	
	Obtain correct unsimplified expansions up to the term in $x^2$ of each partial fraction	<b>A1ft + A1ft</b>	The ft is on $B$ and $C$
	Add the value of $A$ to the sum of the expansions	<b>M1</b>	
	Obtain final answer $2 + \frac{7}{3}x + \frac{7}{18}x^2$	<b>A1</b>	
		<b>5</b>	

Question	Answer	Marks	Guidance
9(i)	State or imply a correct normal vector to either plane, e.g. $2\mathbf{i} + 3\mathbf{j} - \mathbf{k}$ , or $\mathbf{i} - 2\mathbf{j} + \mathbf{k}$	<b>B1</b>	
	Carry out correct process for evaluating the scalar product of two normal vectors	<b>M1</b>	
	Using the correct process for the moduli, divide the scalar product of the two normal vectors by the product of their moduli and evaluate the inverse cosine of the result	<b>M1</b>	
	Obtain answer $56.9^\circ$ or $0.994$ radians	<b>A1</b>	
		<b>4</b>	
9(ii)	<i>EITHER:</i> Carry out a complete strategy for finding a point on the line (call the line $l$ )	<b>M1</b>	
	Obtain such a point, e.g. $(1, 1, 4)$	<b>A1</b>	
	<i>EITHER:</i> State a correct equation for a direction vector $a\mathbf{i} + b\mathbf{j} + c\mathbf{k}$ for $l$ , e.g. $2a + 3b - c = 0$	<b>B1</b>	
	State a second equation, e.g. $a - 2b + c = 0$ , and solve for one ratio, e.g. $a : b$	<b>M1</b>	
	Obtain $a : b : c = 1 : -3 : -7$ , or equivalent	<b>A1</b>	
	State a correct answer, e.g. $\mathbf{r} = \mathbf{i} + \mathbf{j} + 4\mathbf{k} + \lambda(\mathbf{i} - 3\mathbf{j} - 7\mathbf{k})$	<b>A1</b>	
	<i>OR1:</i> Attempt to calculate the vector product of the two normal vectors	<b>M1</b>	
	Obtain two correct components	<b>A1</b>	
	Obtain $\mathbf{i} - 3\mathbf{j} - 7\mathbf{k}$ , or equivalent	<b>A1</b>	
	State a correct answer, e.g. $\mathbf{r} = \mathbf{i} + \mathbf{j} + 4\mathbf{k} + \lambda(\mathbf{i} - 3\mathbf{j} - 7\mathbf{k})$ , or equivalent	<b>A1</b>	

Question	Answer	Marks	Guidance
9(ii)	<i>OR2:</i> Obtain a second point on $l$ e.g. (0, 4, 11)	<b>B1</b>	
	Subtract position vectors and obtain a direction vector for $l$	<b>M1</b>	
	Obtain $\mathbf{i} - 3\mathbf{j} - 7\mathbf{k}$ , or equivalent	<b>A1</b>	
	State a correct answer, e.g. $\mathbf{r} = 4\mathbf{j} + 11\mathbf{k} + \mu(\mathbf{i} - 3\mathbf{j} - 7\mathbf{k})$ , or equivalent	<b>A1</b>	
	<i>OR3:</i> Express one variable in terms of a second	<b>M1</b>	
	Obtain a correct simplified expression, e.g. $y = 4 - 3x$	<b>A1</b>	
	Express the third variable in terms of the second	<b>M1</b>	
	Obtain a correct simplified expression, e.g. $z = 11 - 7x$	<b>A1</b>	
	Form a vector equation for the line	<b>M1</b>	
	State a correct answer, e.g. $\mathbf{r} = 4\mathbf{j} + 11\mathbf{k} + \lambda(\mathbf{i} - 3\mathbf{j} - 7\mathbf{k})$ , or equivalent	<b>A1</b>	
		<b>6</b>	



Question	Answer	Marks	Guidance
9(ii)	<i>OR4:</i> Express one variable in terms of a second	<b>M1</b>	
	Obtain a correct simplified expression, e.g. $x = \frac{4}{3} - \frac{y}{3}$	<b>A1</b>	
	Express the same variable in terms of the third	<b>M1</b>	
	Obtain a correct simplified expression, e.g. $x = \frac{11}{7} - \frac{z}{7}$	<b>A1</b>	
	Form a vector equation for the line	<b>M1</b>	
	Obtain a correct answer, e.g. $\mathbf{r} = 4\mathbf{j} + 11\mathbf{k} + \mu(\mathbf{i} - 3\mathbf{j} - 7\mathbf{k})$ , or equivalent	<b>A1</b>	
		<b>6</b>	

Question	Answer	Marks	Guidance
10(i)	State or imply $du = -\sin x \, dx$	<b>B1</b>	
	Using Pythagoras express the integral in terms of $u$	<b>M1</b>	
	Obtain integrand $\pm\sqrt{u}(1-u^2)$	<b>A1</b>	
	Integrate and obtain $-\frac{2}{3}u^{\frac{3}{2}} + \frac{2}{7}u^{\frac{7}{2}}$ , or equivalent	<b>A1</b>	
	Change limits correctly and substitute correctly in an integral of the form $au^{\frac{3}{2}} + bu^{\frac{7}{2}}$	<b>M1</b>	Or substitute original limits correctly in an integral of the form $a(\cos x)^{\frac{3}{2}} + b(\cos x)^{\frac{7}{2}}$
	Obtain answer $\frac{8}{21}$	<b>A1</b>	
		<b>6</b>	
10(ii)	Use product rule and chain rule at least once	<b>M1</b>	
	Obtain correct derivative in any form	<b>A1 + A1</b>	
	Equate derivative to zero and obtain a horizontal equation in integral powers of $\sin x$ and $\cos x$	<b>M1</b>	
	Use correct methods to obtain an equation in one trig function	<b>M1</b>	
	Obtain $\tan^2 x = 6$ , $7\cos^2 x = 1$ or $7\sin^2 x = 6$ , or equivalent, and obtain answer 1.183	<b>A1</b>	
		<b>6</b>	