

| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| $2(\mathrm{i})$ | $1 \mathrm{~L}:{ }^{6} \mathrm{C}_{2}=15$ | $\mathbf{B 1}$ |  |
|  |  | $\mathbf{1}$ |  |
| $2(\mathrm{ii})$ | $\mathrm{No} \mathrm{L:}{ }^{6} \mathrm{C}_{3}=20$ <br> $\left(1 \mathrm{~L}:{ }^{6} \mathrm{C}_{2}=15\right)$ | $\mathbf{M 1}$ | Either 0L or 2L correct unsimplified |
|  | $2 \mathrm{~L}:{ }^{6} \mathrm{C}_{1}=6$ | $\mathbf{M 1}$ | Summing the 3 correct scenarios |
|  | Total $=41$ | $\mathbf{A 1}$ |  |
|  |  | $\mathbf{3}$ |  |


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| :---: | :---: | :---: | :---: |
| 3(i) | $(10 / 160=) 1 / 16,0.0625$ | B1 | OE |
|  |  | 1 |  |
| 3(ii) | $(90 / 160)=9 / 16,0.5625$ | B1 | OE |
|  |  | 1 |  |
| 3(iii) | $\begin{aligned} \mathrm{P}(\text { red } / \text { hatchback }) & =\mathrm{P}(\text { red hatchback }) / \mathrm{P}(\text { hatchback }) \\ & =40 / 160 / 90 / 160 \end{aligned}$ | M1 | Appropriate probabilities in a fraction |
|  | $=4 / 9$ | A1 | OE <br> Altn method: Direct from table M1 for 40/a or $\mathrm{b} / 90, \mathrm{a} \neq 160$ Al for 40/90 oe |
|  |  | 2 |  |


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| 3(iv) | EITHER: $\mathrm{P}(\text { red }) \times \mathrm{P}(\text { hatchback })=\frac{72}{160} \times \frac{90}{160} \neq \frac{40}{160}$ | (M1 | Use correct approach with appropriate probabilities substituted |
|  | Not independent | A1) | Numerical comparison and conclusion stated |
|  | OR: $\mathrm{P}(\mathrm{red} / \text { hatchback })=40 / 90 \text { and } \frac{40}{90} \neq \frac{72}{160}$ | (M1 | Use correct approach with appropriate probabilities substituted |
|  | Not independent | A1) | Numerical comparison and conclusion stated |
|  |  | 2 |  |


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| 4(i) | $\Sigma p=1: 0.2+0.1+p+0.1+q=1: \quad p+q=0.6$ | M1 | Unsimplified sum of probabilities equated to 1 |
|  | $\Sigma p x=1.7:-0.4+0+p+0.3+4 q=1.7:$ | M1 | Unsimplified Sum of $p x$ equated to 1.7 |
|  | $p+4 q=1.8$ | M1 | Solve simult. equations to find expression in $p$ or $q$ |
|  | $p=0.2, q=0.4$ | A1 |  |
|  |  | 4 |  |
| 4(ii) | $\begin{aligned} & \operatorname{Var}(X)=\Sigma p x^{2}-1.7^{2}=4 \mathrm{x} 0.2+1 p+9 \mathrm{x} 0.1+16 q-1.7^{2} \\ & =8.3-2.89 \end{aligned}$ | M1 | Use correct unsimplified expression for variance |
|  | $=5.41$ | A1 |  |
|  |  | 2 |  |


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| 5(i) | $24.25 n-20 n=136$ <br> Or $\frac{136}{n}+20=24.25$ | M1 | Unsimplified correct equation |
|  | $n=32$ | A1 |  |
|  |  | 2 |  |
| 5(ii) | Using coded information: $\text { Variance }=\frac{2888}{32}-\left(\frac{136}{32}\right)^{2}$ | M1 | unsimplified expression for variance |
|  | $=72.1875=72.19$ | A1 | accept answers 72.2 SOI |
|  | Using uncoded information: $\text { Variance }=\frac{\sum x^{2}}{32}-24.25^{2}$ <br> Equate with 72.1875 to give | M1 | Equate two expressions for variance and solve |
|  | $\sum x^{2}=21128$ | A1 |  |
|  |  | 4 |  |


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| 6 (i) | $3!\times \frac{4!}{3!} \times 2$ | M1 | 3 ! oe seen multiplied by integer $\geqslant 1$, no addition |
|  |  | M1 | $4!/ 3$ ! oe seen multiplied by integer $>1$, no addition |
|  | $=48$ | A1 |  |
|  |  | 3 |  |
| 6(ii) | EITHER:$\begin{aligned} \text { Even } & =\text { Total number of arrangements }- \text { Odd numbers } \\ & =7!/ 3!-3 \times \frac{6 \times 5 \times 4 \times 3 \times 2 \times 1}{3!}=(7!/ 3!-6!/ 2!) \\ & =840-360 \end{aligned}$ | B1 | 7!/3! - |
|  |  | B1 | 6!/2! OE |
|  | $=480$ | B1 |  |
|  | OR: <br> No of arrangements ending in $8: \frac{6!}{3!}$ | B1 | No. ending in 8 or no. ending in 6 correct unsimplified |
|  | No ending in 6: $6!/ 2$ ! | B1 | Both correct and added unsimplified |
|  | Total: $\frac{6!}{3!}+6!/ 2=120+360=480$ | B1 |  |
|  |  | 3 |  |


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| 7(i) | $\begin{aligned} & \mathrm{P}(X>410)=225 / 6000=0.0375 \\ & \mathrm{P}\left(Z>\frac{410-400}{\sigma}\right)=0.0375: 0.9625 \end{aligned}$ | M1 | Use $1-225 / 6000=0.9625$ to find $z$ value |
|  | $z$ value $= \pm 1.78$ | A1 | $z$ value: $\pm 1.78$ |
|  | $\frac{10}{\sigma}=1.78$ | M1 | (410-400)/ $\sigma=$ their $z$ (must be a $z$ value) |
|  | $\sigma=5.62$ | A1 |  |
|  |  | 4 |  |
| 7(ii) | We need $\mathrm{P}(Z<-1.5)$ and $\mathrm{P}(Z>1.5)$ | M1 | Attempt at $\mathrm{P}(Z<-1.5)$ or $\mathrm{P}(Z>1.5)$ $1-\Phi(1.5)$ seen |
|  | $\begin{aligned} & \Phi(-1.5)+1-\Phi(1.5) \\ & =2-2 \Phi(1.5) \end{aligned}$ | M1 | Or equivalent expression with values |
|  | $=2-2 \times 0.9332=0.1336(0.134)$ | A1 | Correct to 3sf |
|  | $\begin{aligned} & \text { Number expected }=500 \times 0.1336 \\ & =66.8 \text { : } \\ & 66 \text { or } 67 \text { packets } \end{aligned}$ | B1ft | 0.1336 used or FT their 4 sf probability times 500 , (not 0.9625 or 0.0375 ) rounded or truncated |
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| 8(i) | $\mathrm{P}(4)+\mathrm{P}(5)={ }^{5} \mathrm{C}_{4}\left(\frac{1}{4}\right)^{4}\left(\frac{3}{4}\right)^{1}+{ }^{5} \mathrm{C}_{5}\left(\frac{1}{4}\right)^{5}\left(\frac{3}{4}\right)^{0}$ | M1 | One binomial term, with $p<1, n=5, p+q=1$ |
|  | $=0.014648 . .+0.00097656 .$. | M1 | Add 2 correct unsimplified binomial terms |
|  | $=0.0156 \text { or } \frac{1}{64}$ | A1 |  |
|  |  | 3 |  |
| 8(ii) | $1-\mathrm{P}(0)>0.995: 0.75^{n}<0.005$ | M1 | Equation or inequality involving $0.75^{n}$ and 0.005 or $0.25^{n}$ and 0.995 |
|  | $\begin{aligned} & n \log 0.75<\log 0.005 \\ & n>18.4: \end{aligned}$ | M1 | Attempt to solve their exponential equation using logs, or trial and error May be implied by their answer |
|  | $n=19$ | A1 |  |
|  |  | 3 |  |
| 8(iii) | $\begin{aligned} p=0.25, n=160: & \text { mean }=160 \times 0.25(=40) \\ & \text { variance }=160 \times 0.25 \times 0.75(=30) \end{aligned}$ | B1 | Correct unsimplified mean and variance |
|  | $\mathrm{P}(X<50)=\mathrm{P}\left(Z<\frac{49.5-40}{\sqrt{30}}\right)$ | M1 | Use standardisation formulae must include square root. |
|  | $\sqrt{30}$ | M1 | Use continuity correction $\pm 0.5$ (49.5 or 50.5 ) |
|  | $=\mathrm{P}(\mathrm{Z}<1.734)=0.959$ | A1 | Correct final answer |
|  |  | 4 |  |

