| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 1 | EITHER: <br> State or imply non-modular inequality $(5 x+2)^{2}>(4 x+3)^{2}$ or corresponding equation or pair of linear equations | (B1 |  |
|  | Attempt solution of 3-term quadratic equation or of 2 linear equations | M1 |  |
|  | Obtain critical values $-\frac{5}{9}$ and 1 | A1 | And no others |
|  | State answer $x<-\frac{5}{9}, \quad x>1$ | A1) |  |
|  | OR: <br> Obtain critical value $x=1$ from graph, inspection, equation | (B1 |  |
|  | Obtain critical value $x=-\frac{5}{9}$ similarly | B2 |  |
|  | State answer $x<-\frac{5}{9}, \quad x>1$ | B1) |  |
|  |  | 4 |  |


| Question | Answer | Marks |  |
| :---: | :--- | :--- | :--- |
| 2 | Differentiate using product rule | $* \mathbf{M 1}$ | Obtaining form $k_{1} \sin \frac{1}{2} x+k_{2} x \cos \frac{1}{2} x$ |
|  | Obtain correct $4 \sin \frac{1}{2} x+2 x \cos \frac{1}{2} x$ or unsimplified equivalent | A1 |  |
|  | Attempt equation of tangent with numerical value for gradient | DM1 | Dependent on first M1 |
|  | Obtain $y=4 x$ | A1 |  |
|  |  | $\mathbf{4}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| $3(\mathrm{i})$ | Use $y$-values $\ln 2, \ln 4, \ln 6, \ln 8, \ln 10$ | B1 | Or decimal equivalents |
|  | Use correct formula, or equivalent, with $h=2$ and five $y$-values | M1 |  |
|  | Obtain 13.5 | A1 |  |
|  |  | 3 |  |
| 3 (ii) | Recognise integrand as $6 \ln (x+2)$ | B1 |  |
|  | Obtain 81 or 81.0 or 81.1 | B1 |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| $4(\mathrm{i})$ | Substitute $x=-3$ and simplify | M1 |  |
|  | Obtain $-108+36+87-15=0$ or equivalent and conclude | A1 |  |
|  | $4($ ii) | Attempt either division by $x+3$ to reach at least partial quotient $4 x^{2}+k x$ <br> or use of identity $\underline{\text { or inspection }}$ | M1 |
|  |  | A1 |  |
|  |  | A1 |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | :--- | :--- |
| 4 (iii) | Identify $2^{u}=\frac{5}{2}$ | B1 | Ignoring other values at this stage |
|  | Apply logarithms and use power law for $2^{u}=c$ where $c>0$ | $\mathbf{M 1}$ |  |
|  | Obtain $u=1.32$ | A1 | And no other values |
|  |  | $\mathbf{3}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| $5(\mathrm{i})$ | Integrate to obtain $-2 \mathrm{e}^{-2 x}$ | B1 |  |
|  | Apply limits correctly to integral of form $k \mathrm{e}^{-2 x}$ | M1 |  |
|  | Obtain $-2 \mathrm{e}^{-4 a}+2 \mathrm{e}^{2 a}=25$ | A1 |  |
|  | Rearrange to confirm $a=\frac{1}{2} \ln \left(12.5+\mathrm{e}^{-4 a}\right)$ | A1 | AG; necessary detail needed |
|  |  |  | $\mathbf{4}$ |
| $5(\mathrm{ii})$ | Consider sign of $a-\frac{1}{2} \ln \left(12.5+\mathrm{e}^{-4 a}\right)$ or equivalent for 1.0 and 1.5 | M1 |  |
|  | Obtain -0.26 and 0.24 or equivalent and justify conclusion | A1 | AG; necessary detail needed |
|  |  | $\mathbf{2}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| 5 (iii) | Use iterative process correctly at least once | M1 |  |
|  | Obtain final answer 1.263 | A1 |  |
|  | Show sufficient iterations to 6 sf to justify answer or show a sign change <br> in the interval $(1.2625,1.2635)$ | A1 |  |
|  |  | $\mathbf{3}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 6 (i) | Express LHS in terms of $\sin 2 x$ and $\cos 2 x$ and attempt to express in terms of $\sin x$ and $\cos x$ | *M1 |  |
|  | Obtain correct $\frac{1}{2 \sin x \cos x}+\frac{\cos ^{2} x-\sin ^{2} x}{2 \sin x \cos x}$ or equivalent | A1 | Perhaps using $\cos 2 x=2 \cos ^{2} x-1$ immediately |
|  | Simplify as far as single terms involving $x$ in numerator and denominator | DM1 | Dependent on first M mark |
|  | Confirm $\cot x$ | A1 | AG; necessary detail needed |
|  |  | 4 |  |
| 6(ii) | Express in terms of $\sin \frac{1}{6} \pi$ and $\cos \frac{1}{6} \pi$ or $\sin \frac{1}{6} \pi$ and $\tan \frac{1}{6} \pi$ | M1 |  |
|  | Obtain $2+\sqrt{3}$ | A1 |  |
|  |  | 2 |  |


| Question | Answer | Marks |  |
| :---: | :--- | ---: | ---: |
| 6 (iii) | State $\int \sin 2 x \cot 2 x \mathrm{~d} x$ | B1 | Condoning absence of $\mathrm{d} x$ |
|  | State $\int \cos 2 x \mathrm{~d} x$ | B1 | Condoning absence of $\mathrm{d} x$ |
|  | Obtain $\frac{1}{2} \sin 2 x+c$ | B1 |  |
|  |  | $\mathbf{3}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 7(i) | Obtain expression for $\frac{\mathrm{d} y}{\mathrm{~d} x}$ with numerator quadratic, denominator linear | M1 | Or equivalent where separate derivatives evaluated first when $t=3$ |
|  | Obtain $\frac{3 t^{2}-6 t}{2 t+4}$ | A1 |  |
|  | Identify $t=3$ at $P$ | B1 |  |
|  | Obtain $\frac{9}{10}$ or equivalent | A1 |  |
|  |  | 4 |  |
| 7(ii) | Equate first derivative to zero and obtain non-zero value of $t$ | M1 |  |
|  | Obtain $t=2$ | A1 |  |
|  | Substitute to obtain (12, - 4) | A1 |  |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| 7 (iii) | Equate expression for gradient to $m$ and rearrange to confirm <br> $3 t^{2}-(2 m+6) t-4 m=0$ | B1 | AG; necessary detail needed |
|  | Attempt solution of quadratic inequality or equation resulting from <br> discriminant | M1 |  |
|  | Obtain critical values $-\sqrt{72}-9$ and $\sqrt{72}-9$ | A1 | Or exact equivalents |
|  | Conclude $m \leqslant-\sqrt{72}-9, m \geqslant \sqrt{72}-9$ | A1 | Or exact equivalents |
|  |  | $\mathbf{4}$ |  |

