| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | :--- |
| 1 | $\operatorname{Var}(P s)=\frac{0.3(1-0.3)}{120}(=0.00175)$ | M1 | Attempt correct values in correct formula |
|  | $0.3 \pm z \sqrt{40.00175 "}$ | M1 | must be a $z$-value, not a prob |
|  | $z=1.645$ | B1 |  |
|  | $\mathrm{CI}=0.231$ to $0.369(3 \mathrm{sf})$ | A1 |  |
|  |  | $\mathbf{4}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 2(i) | $\left(\mathrm{H}_{1}\right): \mu \neq 6.4$ | B1 |  |
|  | Total: | 1 |  |
| 2(ii) | $\text { comp } 2.43 \text { with a } z \text {-value }$ $z=2.576 \text { AND }$ | M1 | oe valid comparison |
|  | No evidence that $\mu$ is not 6.4 or do not reject $\mu=6.4$ | A1 | Allow "Accept $\mu=6.4$ " <br> Must mention $\mu$, not just " $\mathrm{H}_{0}$ " or " $\mathrm{H}_{1}$ " |
|  | Total: | 2 |  |
| 2(iii) | Testing for an increase in $\mu$, or for a decrease in $\mu$, rather than a change | B1 | Any equiv statement |
|  | Total: | 1 |  |


| Question |  | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: | :---: |
| 3(i) | $\frac{53-52}{6.1+\sqrt{75}}$ | ( $=1.420$ ) | M1 |  |
|  | $\frac{51-52}{6.1+\sqrt{75}}$ | $(=-1.420)$ | M1 | or -"1.420" seen |
|  | $\Phi$ ("1.4 | ("-1.420") | M1 |  |
|  | $=0.844$ |  | A1 |  |
|  |  | Total: | 4 |  |
| 3(ii) | Need to assume $\bar{X}$ (approx.) normally distributed |  | B1 | or $X$ not stated to be normally distributed |
|  |  | Total: | 1 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 4(i) | ( $\lambda=$ ) 4.5 | B1 |  |
|  | $\mathrm{e}^{-4.5}\left(1+4.5+\frac{4.5{ }^{2}}{2!}\right)$ | M1 | Allow any $\lambda$. Allow one end error |
|  | $=0.174$ | A1 |  |
|  | Total: | 3 |  |
| 4(ii) | Accept reduction in mean no. of missed appts although untrue | B1 | or Mean is 0.9 (or 4.5 ) but $<3$ missed appts. In context |
|  | Total: | 1 |  |
| 4(iii) | $\mathrm{P}(X \geqslant 3)$ | M1 | Attempted |
|  | $=1-\mathrm{e}^{-1}\left(1+1+\frac{1^{2}}{2!}\right)$ | M1 | Allow any $\lambda$ except 4.5 or 0.9 , Allow one end error |
|  | $=0.0803(3 \mathrm{sfs})$ | A1 |  |
|  | Total: | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 5(a)(i) | $k=1$ | B1 |  |
|  | Total: | 1 |  |
| 5(a)(ii) | $\mathrm{f}_{2}:$ area $>1(\operatorname{area} \neq 1)$ | B1 | oe |
|  | $f_{3}$ : includes negative values of $f_{3}$ | B1 | oe |
|  | Total: | 2 |  |
| 5(b)(i) | $6 \int_{-a}^{a}\left(a^{2}-x^{2}\right) \mathrm{d} x=1$ | M1 | Integ $\mathrm{f}(x)=1$, ignore limits |
|  | $6\left[a^{2} x-\frac{x^{3}}{3}\right]{ }_{-a}^{a}=1$ | A1 | Correct integral and limits |
|  | $\begin{align*} & 6\left(2 a^{3}-\frac{2 a^{3}}{3}\right)=1 \\ & \frac{24 a^{3}}{3}=1 \text { or } 8 a^{3}=1 \\ & a=1 / 2 \end{align*}$ | A1 | Correctly obtained. No errors seen. (SR Verification scores M1A1 only max 2/3) |
|  | Total: | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 5(b)(ii) | 0 | B1 |  |
|  | Total: | 1 |  |
| 5(b)(iii) | $\begin{aligned} & 6 \int_{-0.5}^{0.5}\left(\frac{x^{2}}{4}-x^{4}\right) \mathrm{d} x \\ & \left(=6\left[\frac{x^{3}}{12}-\frac{x^{5}}{5}\right]_{-0.5}^{0.5}=0.05\right) \\ & \operatorname{Var}=0.05-0^{2} \end{aligned}$ | M1 | attempt int $x^{2} \mathrm{f}(x) \&$ correct limits |
|  | $=0.05 \mathrm{oe}$ | A1 | cao; allow omission of $-0^{2}$ |
|  | Total: | 2 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 6 (i) | Assume cartons are random sample(s) | B1 | or masses of cartons are independent of each other oe |
|  | $\begin{aligned} & \mathrm{E}(T)=816.4 \\ & \operatorname{Var}(T)=1570.08 \end{aligned}$ | B1 | Both |
|  | $z=\frac{900-816.44^{\prime \prime}}{\sqrt{" 15750.08^{\prime \prime}}} \quad(=2.110)$ | M1 |  |
|  | $1-\Phi($ "2.110") | M1 |  |
|  | $=0.0174=1.74 \%(3 \mathrm{sfs})$ | A1 | $\%$ only (accept $1.7 \%$ if 0.0174 seen) |
|  | Total: | 5 |  |
| 6(ii) | $\mathrm{P}(F-S>0)$ stated or implied | M1 | $\mathrm{P}(S-F<0)$ |
|  | $\begin{array}{ll} 62.0-78.8 & (=-16.8) \\ \& 10.0^{2}+12.6^{2} & (=258.76) \end{array}$ | B1 | $\begin{array}{ll} 78.8-62.0 & (=16.8) \\ \& 12.6^{2}+10.0^{2} & (=258.76) \end{array}$ |
|  | $z=\frac{0-\left("-16.8^{\prime \prime}\right)}{\sqrt{\prime 255.76^{\prime \prime}}}(=1.044)$ | M1 | $z=\frac{0-116.8^{\prime \prime}}{\sqrt{" 258.76^{\prime}}}(=-1.044)$ |
|  | $1-\Phi(" 1.044$ ") | M1 | $\Phi("-1.044 ")=1-\Phi\left({ }^{(1.044 ")}\right.$ |
|  | $\begin{aligned} & (=1-0.8517) \\ & =0.148(3 \mathrm{sfs}) \end{aligned}$ | A1 |  |
|  | Total: | 5 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 7(i) | Planes arrive at constant mean rate | B1 |  |
|  | Planes arrive at random | B1 | or Planes arrive independently Must be in context |
|  | Total: | 2 |  |
| 7(ii)(a) | ( $\lambda=$ ) $5.2 \div 4$ | M1 |  |
|  | $\mathrm{e}^{-1.3}\left(\frac{1.3{ }^{2}}{2}+\frac{1.3^{3}}{3!}\right)$ | M1 | Allow any $\lambda$, allow one end error |
|  | $=0.330$ (3 sfs) | A1 | Accept 0.33 |
|  | Total: | 3 |  |
| 7(ii)(b) | $1-\mathrm{e}^{-3.467} \times\left(1+3.467+\frac{3.467^{2}}{2!}+\frac{3.467^{3}}{3!}\right)$ | M1 | Allow any $\lambda$ except 5.2 or 1.3 , allow one end error |
|  | $=0.456$ (3 sfs) | A1 |  |
|  | Total: | 2 |  |
| 7(iii) | $\mathrm{N}(52,52)$ stated or implied | B1 |  |
|  | $\frac{60.5-52}{\sqrt{52}}(=1.179)$ | M1 | ft their mean and var. <br> Allow wrong or no cc or no $\sqrt{ }$ |
|  | Ф("1.179") | M1 |  |
|  | $=0.881$ ( 3 sf ) | A1 |  |
|  | Total: | 4 |  |

