| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| 1 | Use $2 \ln (2 x)=\ln (2 x)^{2}$ | $*$ M1 |  |
|  | Use addition or subtraction property of logarithms | $* \mathbf{M 1}$ |  |
|  | Obtain $4 x^{2}=(x+3)(3 x+5)$ or equivalent without logarithms | A1 |  |
|  | Solve 3-term quadratic equation | DM1 | dep $* \mathrm{M} * \mathrm{M}$ |
|  | Conclude with $x=15$ only | A1 |  |
|  |  | $\mathbf{5}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| 2 (i) | Use identity $\cot \theta=\frac{1}{\tan \theta}$ | B1 |  |
|  | Attempt use of identity for $\tan 2 \theta$ | M1 |  |
|  | Confirm given $\tan ^{2} \theta=\frac{3}{4}$ | A1 |  |
|  |  | Total: | $\mathbf{3}$ |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| 3 (i) | State or imply non-modulus inequality $(2 x-5)^{2}<(x+3)^{2}$ or <br> corresponding equation or pair of linear equations | B1 |  |
|  | Attempt solution of 3-term quadratic inequality or equation <br> or of 2 linear equations | M1 |  |
|  | Obtain critical values $\frac{2}{3}$ and 8 | A1 |  |
|  | State answer $\frac{2}{3}<x<8$ | A1 |  |
|  |  | Total: | $\mathbf{4}$ |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| 3 (ii) | Attempt to find $y$ from $\ln y=$ upper limit of answer to part (i) | M1 |  |
|  | Obtain 2980 | A1 |  |
|  |  | Total: | $\mathbf{2}$ |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| 4 | Use product rule for derivative of $x^{2} \sin y$ | M1 |  |
|  | Obtain $2 x \sin y+x^{2} \cos y \frac{\mathrm{~d} y}{\mathrm{~d} x}$ | A1 |  |
|  | Obtain $-3 \sin 3 y \frac{\mathrm{~d} y}{\mathrm{~d} x}$ as derivative of $\cos 3 y$ | B1 |  |
|  | Obtain $2 x \sin y+x^{2} \cos y \frac{\mathrm{~d} y}{\mathrm{~d} x}-3 \sin 3 y \frac{\mathrm{~d} y}{\mathrm{~d} x}=0$ | A1 |  |
|  | Substitute $x=2, y=\frac{1}{2} \pi$ to find value of $\frac{\mathrm{d} y}{\mathrm{~d} x}$ | M1 | dep $\frac{\mathrm{d} y}{\mathrm{~d} x}$ occurring at least <br> once |
|  | Obtain $-\frac{4}{3}$ | A1 | from correct work only |
|  |  | $\mathbf{6}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| 5 (i) | Integrate to obtain form $k_{1} x+k_{2} x^{2}+k_{3} \mathrm{e}^{3 x}$ for non-zero <br> constants | M1 |  |
|  | Obtain $x+x^{2}+\mathrm{e}^{3 x}$ | A1 |  |
|  | Apply both limits to obtain $a+a^{2}+\mathrm{e}^{3 a}-1=250$ or <br> equivalent | A1 |  |
|  | Apply correct process to reach form without e involved | M1 |  |
|  | Confirm given $a=\frac{1}{3} \ln \left(251-a-a^{2}\right)$ | A1 |  |
|  |  | $\mathbf{5}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| 5 (ii) | Use iterative process correctly at least once | M1 |  |
|  | Obtain final answer 1.835 | A1 |  |
|  | Show sufficient iterations to 6 sf to justify answer or show <br> sign change in interval (1.8345, 1.8355$)$ | A1 |  |
|  |  | Total: | $\mathbf{3}$ |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| 6(i) | Substitute $x=-2$ and equate to zero | M1 |  |
|  | Substitute $x=2$ and equate to 28 | M1 |  |
|  | Obtain $-9 a+4 b+34=0$ and $7 a+4 b-62=0$ or <br> equivalents | A1 |  |
|  | Solve a relevant pair of simultaneous equations for $a$ or $b$ | M1 |  |
|  | Obtain $a=6, b=5$ | A1 |  |
|  |  | Total: | $\mathbf{5}$ |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 7(i) | Use $\cos (A+B)$ identity | M1 |  |
|  | Obtain $2 \cos 2 x\left(\cos 2 x \cdot \frac{1}{2} \sqrt{3}-\sin 2 x \cdot \frac{1}{2}\right)$ | A1 |  |
|  | Attempt identity expressing $\cos ^{2} 2 x$ in terms of $\cos 4 x$ | M1 |  |
|  | Attempt identity expressing $\cos 2 x \sin 2 x$ in terms of $\sin 4 x$ | M1 |  |
|  | Obtain $\frac{1}{2} \sqrt{3}(1+\cos 4 x)-\frac{1}{2} \sin 4 x$ | A1 |  |
|  | Total: | 5 |  |
| 7(ii) | Attempt to find at least one intercept with $x$-axis | M1 |  |
|  | Obtain $x=\frac{1}{6} \pi$ at least | A1 |  |
|  | Integrate to obtain $k_{4} x+k_{5} \sin 4 x+k_{6} \cos 4 x$ | M1 |  |
|  | Obtain $\frac{1}{2} \sqrt{3} x+\frac{1}{8} \sqrt{3} \sin 4 x+\frac{1}{8} \cos 4 x$ | A1 $\sqrt{\text { a }}$ | following their answer to (i) of correct form |
|  | Apply limits 0 and $\frac{1}{6} \pi$ to obtain $\left(\frac{1}{12} \sqrt{3}\right) \pi$ or exact equivalent | A1 | following completely correct work |
|  | Total: | 5 |  |

