

Page 4	Mark Scheme	Syllabus	Paper
	Cambridge International AS/A Level – March 2016	9709	22
1	Attempt division at least as far as quotient $2x^2 + kx$ Obtain quotient $2x^2 - x + 2$ Obtain remainder 6 Special case: Use of Remainder Theorem to give 6		M1 A1 A1 [3] B1
2	Either State or imply non-modular inequality $(x-5)^2 < (2x+3)^2$ or corresponding pair of linear equations Attempt solution of 3-term quadratic equation or of 2 linear equations Obtain critical values -8 and $\frac{2}{3}$ State answer $x < -8$, $x > \frac{2}{3}$ Or Obtain critical value -8 from graphical method, inspection, equation Obtain critical value $\frac{2}{3}$ similarly State answer $x < -8$, $x > \frac{2}{3}$		B1 M1 A1 A1 B1 B2 B1 [4]
3	Use $2 \ln x = \ln x^2$ Use law for addition or subtraction of logarithms Obtain $x^2 = (3+x)(2-x)$ or equivalent with no logarithms Solve 3-term quadratic equation Obtain $x = \frac{3}{2}$ and no other solutions		B1 M1 A1 M1 A1 [5]
4	(i) Use the iterative formula correctly at least once Obtain final answer 1.516 Show sufficient iterations to justify accuracy to 3 dp or show sign change in interval (1.5155, 1.5165) (ii) State equation $x = \sqrt{\frac{1}{2}x^2 + 4x^{-3}}$ or equivalent Obtain exact value $\sqrt[3]{8}$ or $8^{0.2}$		M1 A1 B1 [3] B1 B1 [2]
5	Obtain integral of form ke^{2x+1} Obtain correct $3e^{2x+1}$ Apply both limits correctly and rearrange at least to $e^{2a+1} = \dots$ Use logarithms correctly to find a Obtain 1.097		M1 A1 M1 M1 A1 [5]

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- 6 (i) Use product rule to obtain expression of form $k_1 e^{-x} \sin 2x + k_2 e^{-x} \cos 2x$ **M1**
 Obtain correct $-3e^{-x} \sin 2x + 6e^{-x} \cos 2x$ **A1**
 Substitute $x = 0$ in first derivative to obtain equation of form $y = mx$ **M1**
 Obtain $y = 6x$ or equivalent with no errors in solution **A1** [4]
- (ii) Equate first derivative to zero and obtain $\tan 2x = k$ **M1***
 Carry out correct process to find value of x **dep M1***
 Obtain $x = 0.554$ **A1**
 Obtain $y = 1.543$ **A1** [4]
- 7 (i) State $3y^2 \frac{dy}{dx}$ as derivative of y^3 **B1**
 Equate derivative of left-hand side to zero and solve for $\frac{dy}{dx}$ **M1**
 Obtain $\frac{dy}{dx} = -\frac{6x^2}{3y^2}$ or equivalent **A1**
 Observe x^2 and y^2 never negative and conclude appropriately **A1** [4]
- (ii) Equate first derivative to -2 and rearrange to $y^2 = x^2$ or equivalent **B1**
 Substitute in original equation to obtain at least one equation in x^3 or y^3 **M1**
 Obtain $3x^3 = 24$ or $x^3 = 24$ or $3y^3 = 24$ or $-y^3 = 24$ **A1**
 Obtain $(2, 2)$ **A1**
 Obtain $(\sqrt[3]{24}, -\sqrt[3]{24})$ or $(2.88, -2.88)$ and no others **A1** [5]
- 8 (i) State $2 \sin x \cos x \cdot \frac{\cos x}{\sin x}$ **B1**
 Simplify to confirm $2 \cos^2 x$ **B1** [2]
- (ii) (a) Use $\cos 2x = 2 \cos^2 x - 1$ **B1**
 Express in terms of $\cos x$ **M1**
 Obtain $16 \cos^2 x + 3$ or equivalent **A1**
 State 3, following their expression of form $a \cos^2 x + b$ **A1** [4]
- (b) Obtain integrand as $\frac{1}{2} \sec^2 2x$ **B1**
 Integrate to obtain form $k \tan 2x$ **M1***
 Obtain correct $\frac{1}{4} \tan 2x$ **A1**
 Apply limits correctly **dep M1***
 Obtain $\frac{1}{4} \sqrt{3} - \frac{1}{4}$ or exact equivalent **A1** [5]