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1 (i)	$80(x^4), -32(x^5)$	B1B1 [2]	Fully simplified
(ii)	$(-32 + 80p)(x^5) = 0$ $p = 2/5$ or $32/80$ oe	M1 A1 ^h [2]	Attempt to mult. relevant terms & put = 0
2	$y = \frac{3x^3}{3} - \frac{2x^{-2}}{-2} (+c)$ $3 = -1 + 1 + c$ $y = x^3 + x^{-2} + 3$	B1B1 M1 A1 [4]	Sub $x = -1, y = 3$. c must be present Accept $c = 3$ www
3	$a + 11d = 17$ $\frac{31}{2}(2a + 30d) = 1023$ Solve simultaneous equations $d = 4, a = -27$ 31st term = 93	B1 B1 M1 A1 A1 [5]	At least one correct
4 (a)	$3x = -\sqrt{3}/2$ $x = \frac{-\sqrt{3}}{6}$ oe	M1 A1 [2]	Accept -0.866 at this stage Or $\frac{-3}{6\sqrt{3}}$ or $\frac{-1}{2\sqrt{3}}$
(b)	$(2 \cos \theta - 1)(\sin \theta - 1) = 0$ $\cos \theta = 1/2$ or $\sin \theta = 1$ $\theta = \pi/3$ or $\pi/2$	M1 A1 A1A1 [4]	Reasonable attempt to factorise and solve Award B1B1 www Allow 1.05, 1.57. SCA1 for both $60^\circ, 90^\circ$
5 (i)	Mid-point of $AB = (7, 3)$ soi Grad. of $AB = -2 \rightarrow$ grad of perp. bisector = $1/2$ soi Eqn of perp. bisector is $y - 3 = \frac{1}{2}(x - 7)$	B1 M1 A1 [3]	Use of $m_1 m_2 = -1$
(ii)	Eqn of CX is $y - 2 = -2(x - 1)$ $\frac{1}{2}x - \frac{1}{2} = -2x + 4$ $x = 9/5, y = 2/5$ $BX^2 = 7.2^2 + 1.4^2$ soi $BX = 7.33$	M1 DM1 A1 M1 A1 [5]	Using their original gradient and (1,2) Solve simultaneously dependent on both previous M's

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6 (i)	$A = 2\pi r^2 + 2\pi rh$ $\pi r^2 h = 1000 \rightarrow h = \frac{1000}{\pi r^2}$ $\text{Sub for } h \text{ into } A \rightarrow A = 2\pi r^2 + \frac{2000}{r} \text{ AG}$	B1 M1 A1 [3]	
(ii)	$\frac{dA}{dr} = 0 \Rightarrow 4\pi r - \frac{2000}{r^2} = 0$ $r = 5.4$ $\frac{d^2A}{dr^2} = 4\pi + \frac{4000}{r^3}$ $> 0 \text{ hence MIN hence MOST EFFICIENT AG}$	M1A1 DM1 A1 B1 [5]	Attempt differentiation & set = 0 Reasonable attempt to solve to $r^3 =$ Or convincing alternative method
7 (i)	$CP = \frac{3}{5}CA \text{ soi}$ $CP = \frac{3}{5}(4i - 3k) = 2.4i - 1.8k \text{ AG}$	M1 A1 [2]	
(ii)	$OP = 2.4i + 1.2k$ $BP = 2.4i - 2.4j + 1.2k$	B1 B1 [2]	
(iii)	$BP \cdot CP = 5.76 - 2.16 = 3.6$ $ BP CP = \sqrt{2.4^2 + 2.4^2 + 1.2^2} \sqrt{2.4^2 + 1.8^2}$ $\cos BPC = \frac{3.6}{\sqrt{12.96} \sqrt{9}} \left(= \frac{1}{3} \right)$ $\text{Angle } BPC = 70.5^\circ \text{ (or 1.23 rads) cao}$	M1 M1 M1 A1 [4]	Use of $x_1x_2 + y_1y_2 + z_1z_2$ Product of moduli All linked correctly
8 (i)	$2a + 4b = 8$ $2a^2 + 3a + 4b = 14$ $2a^2 + 3a + (8 - 2a) = 14 \rightarrow (a + 2)(2a - 3) = 0$ $a = -2 \text{ or } 3/2$ $b = 3 \text{ or } 5/4$	M1 A1 M1 A1 A1 [5]	Substitute in -2 and -3 Sub linear into quadratic & attempt solution If A0A0 scored allow SCA1 for either $(-2, 3)$ or $(3/2, 5/4)$
(ii)	$y = \left(x - \frac{1}{2}\right)^2 - \frac{13}{4} \text{ Attempt completing of square}$ $x - \frac{1}{2} = (\pm) \sqrt{y + \frac{13}{4}} \text{ oe}$ $f^{-1}(x) = \frac{1}{2} \pm \sqrt{x + \frac{13}{4}} \text{ oe}$ $\text{Domain of } f^{-1} \text{ is } (x) \geq -13/4$	M1A1 DM1 A1 B1 [5]	Allow with x/y transposed Allow with x/y transposed Allow $y = \dots$ Must be a function of x Allow $>$, $-13/4 \leq x \leq \infty$, $\left[-\frac{13}{4}, \infty\right)$ etc

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9 (a) (i)	$BAO = OBA = \frac{\pi}{2} - \alpha$ $AOB = \pi - \left(\frac{\pi}{2} - \alpha\right) - \left(\frac{\pi}{2} - \alpha\right) = 2\alpha \text{ AG}$	M1A1 [2]	Allow use of 90° or 180° Or other valid reasoning
(ii)	$\frac{1}{2}r^2(2\alpha) - \frac{1}{2}r^2 \sin 2\alpha \text{ oe}$	B2,1,0 [2]	SCB1 for reversed subtraction
(b)	<p>Use of $\alpha = \frac{\pi}{6}$, $r = 4$</p> <p>1 segment $S = \left(\frac{1}{2}\right)4^2\left(\frac{\pi}{3}\right) - \left(\frac{1}{2}\right)4^2 \sin \frac{\pi}{3}$</p> $= \left(\frac{8\pi}{3} - 4\sqrt{3}\right)$ <p>Area ABC $T = \left(\frac{1}{2}\right)4^2 \sin \frac{\pi}{3} \quad (= 4\sqrt{3})$</p> $T - 3S = \left(\frac{1}{2}\right)4^2 \sin \frac{\pi}{3} - 3$ $\left[\left(\frac{1}{2}\right)4^2\left(\frac{\pi}{3}\right) - \left(\frac{1}{2}\right)4^2 \sin \frac{\pi}{3}\right]$ <p>$16\sqrt{3} - 8\pi \text{ cao}$</p>	B1B1 M1 B1 M1 A1 [6]	<p>Ft <i>their</i> (ii), α, r</p> <p>OR $AXB = \frac{T}{3} = 4 \tan \frac{\pi}{6}$ or</p> $\frac{1}{2}\left(\frac{4}{\sqrt{3}}\right)^2 \sin \frac{2\pi}{3} \left(= \frac{4\sqrt{3}}{3}\right)$ <p>OR $3\left[\frac{T}{3} - S\right] = 3\left[\frac{4\sqrt{3}}{3} - \left(\frac{8\pi}{3} - 4\sqrt{3}\right)\right]$</p>
10 (i)	$x = 1/3$	B1 [1]	
(ii)	$\frac{dy}{dx} = \left[\frac{2}{16}(3x-1)\right] [3]$ <p>When $x = 3$ $\frac{dy}{dx} = 3$ soi</p> <p>Equation of QR is $y - 4 = 3(x - 3)$</p> <p>When $y = 0$ $x = 5/3$</p>	B1B1 M1 M1 A1 [5]	
(iii)	<p>Area under curve = $\left[\frac{1}{16 \times 3}(3x-1)^3\right] \left[\times \frac{1}{3}\right]$</p> $\frac{1}{16 \times 9} [8^3 - 0] = \frac{32}{9}$ <p>Area of $\Delta = 8/3$</p> <p>Shaded area = $\frac{32}{9} - \frac{8}{3} = \frac{8}{9}$ (or 0.889)</p>	B1B1 M1A1 B1 A1 [6]	Apply limits: <i>their</i> $\frac{1}{3}$ and 3