

- 1 (a) Give full details of the geometrical transformation in the  $x$ - $y$  plane represented by the matrix  $\begin{pmatrix} 6 & 0 \\ 0 & 6 \end{pmatrix}$ . [1]

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Let  $\mathbf{A} = \begin{pmatrix} 3 & 4 \\ 2 & 2 \end{pmatrix}$ .

- (b) The triangle  $DEF$  in the  $x$ - $y$  plane is transformed by  $\mathbf{A}$  onto triangle  $PQR$ .  
Given that the area of triangle  $DEF$  is  $13 \text{ cm}^2$ , find the area of triangle  $PQR$ . [2]

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- (c) Find the matrix  $\mathbf{B}$  such that  $\mathbf{AB} = \begin{pmatrix} 6 & 0 \\ 0 & 6 \end{pmatrix}$ . [2]

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- (d) Show that the origin is the only invariant point of the transformation in the  $x$ - $y$  plane represented by  $\mathbf{A}$ . [4]

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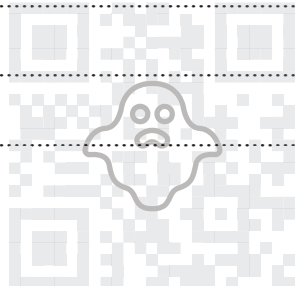
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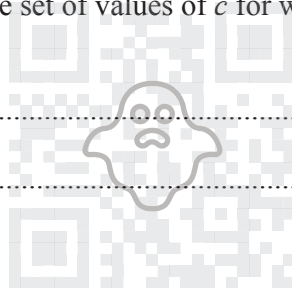


(c) Sketch C.

[2]

(d) (i) Sketch the graphs of  $y = \left| \frac{x^2}{x-3} \right|$  and  $y = |x| - 3$  on a single diagram, stating the coordinates of the intersections with the axes. [4]

(ii) Use your sketch to find the set of values of  $c$  for which  $\left| \frac{x^2}{x-3} \right| \leq |x| + c$  has no solution. [1]



7 The points  $A, B, C$  have position vectors

$$2\mathbf{i} + 2\mathbf{j}, \quad -\mathbf{j} + \mathbf{k} \quad \text{and} \quad 2\mathbf{i} + \mathbf{j} - 7\mathbf{k}$$

respectively, relative to the origin  $O$ .

(a) Find an equation of the plane  $OAB$ , giving your answer in the form  $\mathbf{r} \cdot \mathbf{n} = p$ . [3]

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The plane  $\Pi$  has equation  $x - 3y - 2z = 1$ .

(b) Find the perpendicular distance of  $\Pi$  from the origin. [1]

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