1	Kayla is investigating the lengths of the leaves of a certain type of tree found in two forests X and Y.
	She chooses a random sample of 40 leaves of this type from forest X and records their lengths, x cm.
	She also records the lengths, $y \text{ cm}$, for a random sample of 60 leaves of this type from forest Y . Her
	results are summarised as follows.

$$\Sigma x = 242.0$$
 $\Sigma x^2 = 1587.0$ $\Sigma y = 373.2$ $\Sigma y^2 = 2532.6$

Find a 90% confidence interval for forests X and Y .	[7

		21	10	186	188	208	184	191	215	198	196	
	entist be onnes.	lieves th	at the	e medi	an brea	king stı	ength o	f metal	rods pro	oduced l	by this fa	actory is les
		ilcoxon the scien				t the 5%	% signif	icance l	level, to	test wh	ether the	ere is evide
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(b) (Give a r	eason w	hy a	Wilco	xon sig	gned-rai	ik test i	s pretei	able to	a sign 1	test, whe	en both are

3 Apples are sold in bags of 5. Based on her previous experience, Freya claims that the probability of any apple weighing more than 100 grams is 0.35, independently of other apples in the bag.

The apples in a random sample of 150 bags are checked and the number, x, in each bag weighing more than 100 grams is recorded. The results are shown in the following table.

x	0	1	2	3	4	5
Frequency	12	39	46	37	12	4

Carry out a goodness of fit test at the 5% significance level and hence comment on Freya's claim. [7]

4 Members of the Sprints athletics club have been taking part in an intense training scheme, aimed at reducing their times taken to run 400 m. For a random sample of 9 athletes from the club, the times taken, in seconds, before and after the training scheme are given in the following table.

Athlete	A	В	С	D	E	F	G	Н	I
Time before	48.8	48.2	50.3	49.6	49.4	48.9	47.6	50.3	48.4
Time after	47.9	47.8	49.6	49.1	49.6	48.9	47.7	49.1	48.1

The organiser of the training scheme claims that on average an athlete's time will be reduced by at least 0.3 seconds.

you make.	that [8]

(a)	Find the probability generating function $G_X(t)$ of X .	[1]
oir	ssan has three coins, two of which are biased so that the probability of obtaining a head we is tossed is $\frac{1}{3}$. The corresponding probability for the third coin is $\frac{1}{4}$. The number of heads of Hassan when he tosses these three coins is denoted by Y .	
(b)	Find the probability generating function $G_{\gamma}(t)$ of Y .	[3]
Γhe	e random variable Z is the total number of heads obtained by Keira and Hassan.	
Γhe (c)	e random variable <i>Z</i> is the total number of heads obtained by Keira and Hassan. Find the probability generating function of <i>Z</i> , expressing your answer as a polynomial.	[3]
		[3]
		[3]

6 The continuous random variable X has cumulative distribution function F given by

$$F(x) = \begin{cases} 0 & x < 0, \\ \frac{1}{60}(16x - x^2) & 0 \le x \le 6, \\ 1 & x > 6. \end{cases}$$

(a)	Find the interquartile range of X .	[4]
(b)	Find $E(X^3)$.	Γ/11
(D)	Γ ind $\Sigma(X)$.	[4]

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