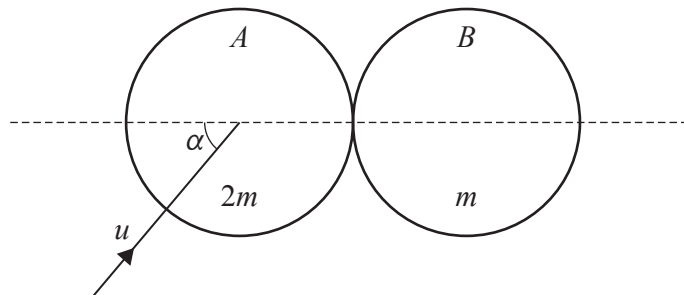


2



Two uniform smooth spheres A and B of equal radii have masses $2m$ and m respectively. Sphere B is at rest on a smooth horizontal surface. Sphere A is moving on the surface with speed u and collides with B . Immediately before the collision, the direction of motion of A makes an angle α with the line of centres of the spheres, where $\tan \alpha = \frac{4}{3}$ (see diagram). The coefficient of restitution between the spheres is $\frac{1}{3}$.

Find the speed of A after the collision. [5]

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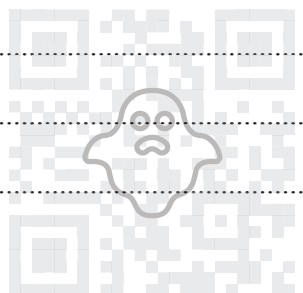
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4 A particle P of mass m is moving in a horizontal circle with angular speed ω on the smooth inner surface of a hemispherical shell of radius r . The angle between the vertical and the normal reaction of the surface on P is θ .

(a) Show that $\cos \theta = \frac{g}{\omega^2 r}$. [3]

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5 A particle P is projected with speed $u \text{ m s}^{-1}$ at an angle of θ above the horizontal from a point O on a horizontal plane and moves freely under gravity. The horizontal and vertical displacements of P from O at a subsequent time t s are denoted by x m and y m respectively.

(a) Starting from the equation of the trajectory given in the List of formulae (MF19), show that

$$y = x \tan \theta - \frac{gx^2}{2u^2}(1 + \tan^2 \theta). \quad [1]$$

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When $\theta = \tan^{-1} 2$, P passes through the point with coordinates $(10, 16)$.

(b) Show that there is no value of θ for which P can pass through the point with coordinates $(18, 30)$. [6]

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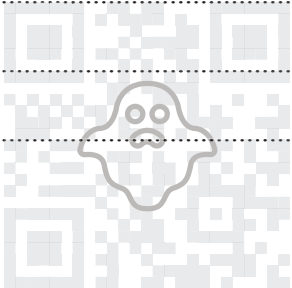
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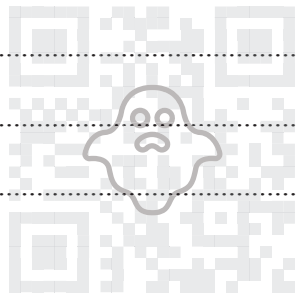
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Handwriting practice area consisting of 25 horizontal dotted lines.



Handwriting practice area consisting of 25 horizontal dotted lines.



Beginning at the instant when the speed of P is $\frac{1}{2}u$, an additional force acts on P . This force has magnitude $\frac{5m}{v}$ N and acts in the direction of increasing x .

- (b) Show that when the speed of P has increased again to u ms^{-1} , the total distance travelled by P is given by an expression of the form

$$\frac{1}{3k} \ln\left(\frac{A - ku^3}{B - ku^3}\right),$$

stating the values of the constants A and B .

[7]

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