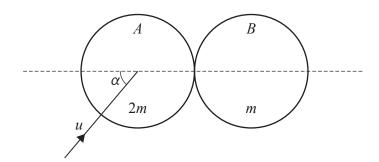


A fixed smooth solid sphere has centre O and radius a. A particle of mass m is projected downwards with speed $\sqrt{\frac{1}{6}ag}$ from the point A on the surface of the sphere, where OA makes an angle α with the upward vertical through O (see diagram). The particle moves in part of a vertical circle on the surface of the sphere. It loses contact with the sphere at the point B, where OB makes an angle β with the upward vertical through O.

Given that $\cos \alpha = \frac{2}{3}$, find the value of $\cos \beta$.	[5]
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Two uniform smooth spheres A and B of equal radii have masses 2m and m respectively. Sphere B is at rest on a smooth horizontal surface. Sphere A is moving on the surface with speed u and collides with B. Immediately before the collision, the direction of motion of A makes an angle α with the line of centres of the spheres, where $\tan \alpha = \frac{4}{3}$ (see diagram). The coefficient of restitution between the spheres is $\frac{1}{3}$.

Find the speed of A after the collision.	[5]
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(a)	Find the distance of the centre of mass of the object from the end of the cylinder that is not attack to the cone.

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Show that the object can reshorizontal surface.				[3
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A particle P of mass m is moving in a horizontal circle with angular speed ω on the smooth inner surface of a hemispherical shell of radius r. The angle between the vertical and the normal reaction of the surface on P is θ .

Show that $\cos \theta = \frac{g}{\omega^2 r}$.	[3
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The plane of the circular motion is at a height x above the lowest point of the shell. When the angular speed is doubled, the plane of the motion is at a height 4x above the lowest point of the shell.

- A particle P is projected with speed u m s⁻¹ at an angle of θ above the horizontal from a point O on a horizontal plane and moves freely under gravity. The horizontal and vertical displacements of P from O at a subsequent time ts are denoted by x m and y m respectively.
 - (a) Starting from the equation of the trajectory given in the List of formulae (MF19), show that

$y = x \tan \theta - \frac{8}{2}$	$\frac{gx^2}{2u^2}(1+\tan^2\theta).$		
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sses through the point winnor value of θ for which B		b). e point with coordinates (18
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One end of a light elastic string, of natural length a and modulus of elasticity k , is attached of mass m . The other end of the string is attached to a fixed point Q . The particle vertically upwards from Q . When P is moving upwards and at a distance $\frac{4}{3}a$ directly a speed $\sqrt{2ga}$. At this point, its acceleration is $\frac{7}{3}g$ downwards.	e P is projected
Show that $k = 4mg$ and find in terms of a the greatest height above Q reached by P.	[8]
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A pa mkv The	article P of mass $m \log m \log n$ moves in a horizontal straight line again $^2 N$, where $v m s^{-1}$ is the speed of P after it has moved a distance initial speed of P is $u m s^{-1}$.	enst a resistive force of magnitude ex m and k is a positive constant.
(a)	Show that $x = \frac{1}{k} \ln 2$ when $v = \frac{1}{2}u$.	[4]

Beginning at the instant when the speed of P is $\frac{1}{2}u$, an additional force acts on P. This force has magnitude $\frac{5m}{v}$ N and acts in the direction of increasing x.

(b)	Show that when the speed of P has increased again to $u \mathrm{ms^{-1}}$, the total distance travelled by P is
	given by an expression of the form

 $\frac{1}{3k}\ln\left(\frac{A-ku^3}{B-ku^3}\right)$ stating the values of the constants A and B. [7]