- 1 Let *a* be a positive constant.
  - (a) Sketch the curve with equation  $y = \frac{ax}{x+7}$ .

[2]



**(b)** Sketch the curve with equation  $y = \left| \frac{ax}{x+7} \right|$  and find the set of values of x for which  $\left| \frac{ax}{x+7} \right| > \frac{a}{2}$ . [4]

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	Find a cubic equa	ition whose ro	ots are $\alpha^2$ , $\mu$	$\beta^2, \gamma^2$ .		
					•••••	
		$2 + B^2 + y^2 = $	$2(\alpha + \beta + \gamma)$			
(h)	It is given that $\alpha^2$					
(b)	It is given that $\alpha^2$		2(0   p   7).			
(b)	It is given that $\alpha^2$ (i) Find the value		Σ(α + β + γ).			
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(a)	Find the equations of the asymptotes of <i>C</i> .	
(h)	Find the coordinates of the stationers rejets on C	
(b)	Find the coordinates of the stationary points on <i>C</i> .	
(b)	Find the coordinates of the stationary points on $C$ .	
(b)		

[3]

(c) Sketch C.



4 (a) By first expressing  $\frac{1}{r^2-1}$  in partial fractions, show that

$$\sum_{r=2}^{n} \frac{1}{r^2 - 1} = \frac{3}{4} - \frac{an + b}{2n(n+1)},$$

where $a$ and $b$ are integers to be found.	[5]
(2)	

	Deduce the value of $\sum_{r=2}^{\infty} \frac{1}{r^2 - r^2}$	· I	
		2 <i>n</i>	
F	Find the limit, as $n \to \infty$ , of	$\sum \frac{n}{2}$	
	, , , , , , , , , , , , , , , , , , ,	$r^2 - 1$	
	•		

1)	Find the shortest distance between $l_1$ and $l_2$ .	

The plane  ${\it II}$  contains  $l_1$  and is parallel to the vector  ${\bf i} + {\bf k}$  .

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le between $l_2$	and $\Pi$ .			
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	le between $l_2$	le between $l_2$ and $\Pi$ .	le between $l_2$ and $\Pi$ .	le between $l_2$ and $\Pi$ .

6 Let  $\mathbf{A} = \begin{pmatrix} 2 & 0 \\ 1 & 1 \end{pmatrix}$ .

	The transformation in the <i>x-y</i> plane represented by $\mathbf{A}^-$ triangle of area $d  \mathrm{cm}^2$ .	transforms a triangle of area 30 cm <sup>2</sup>	<sup>2</sup> into a
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Find the value of d. [3]

**(b)** Prove by mathematical induction that, for all positive integers n,

 $\mathbf{A}^n = \begin{pmatrix} 2^n & 0 \\ 2^n - 1 & 1 \end{pmatrix}. \tag{5}$ 

Find the value of $n$ .	

- 7 The curve  $C_1$  has polar equation  $r = \theta \cos \theta$ , for  $0 \le \theta \le \frac{1}{2}\pi$ .
  - (a) The point on  $C_1$  furthest from the line  $\theta = \frac{1}{2}\pi$  is denoted by P. Show that, at P,

 $2\theta \tan \theta - 1 = 0$ 

		20 tan 0 1 -	- 0		
and verify that this	equation has a r	root between 0	.6 and 0.7.		
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curve $C_2$ has polar denoted by $O$ , and a	at another point	t Q.			$C_2$ intersect at
Find the polar coord	linates of $Q$ , given	ving your answ	vers in exact fo	orm.	
		7.42			

[3]

	( - <b>)</b>	01 .4.1. 0	10		11
(	C	Sketch C.	ana C <sub>2</sub>	on the same	diagram.

d)	Find, in terms of $\pi$ , the area of the region bounded by the arc $OQ$ of $C_1$ and the arc $OQ$ of $C_2$ . [7]