## **VENN DIAGRAMS**

[ESTIMATED TIME: 60 minutes]

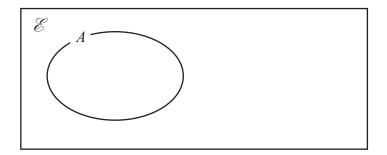


(+ IGCSE) EXAM QUESTION PRACTICE

1. [3 marks]

A, B and C are three sets.

 $A \cap B = \emptyset$  and  $C \subset A$ 



(a) Complete the Venn diagram to show the sets B and C

**(2)** 

(b) On the Venn diagram, shade the region that represents  $A \cap C'$ 

(1)

2. [4 marks]

There are 35 students in a group.

- 18 students play hockey.
- 12 students play both hockey and tennis.
- 15 students play neither hockey nor tennis.

Find the number of students who play tennis.

**Statements** 

 $A \subset B$ 

 $B \subset A$ 

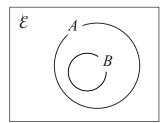
 $A \cup B = \mathcal{E}$ 

 $A \cap B = \emptyset$ 

 $A \cap B = A$ 

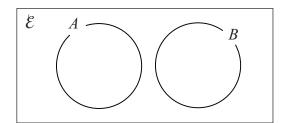
Choose a statement from the box that describes the relationship between sets A and B.

(i)



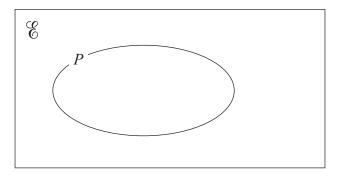
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(ii)



.....

4. [3 marks]



Set *P* is shown on the Venn Diagram. Two sets, *Q* and *R*, are such that

$$R \subset P$$

$$Q \cap R = \emptyset$$

$$P \cup Q = P$$

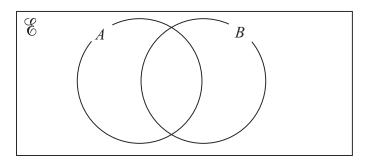
Complete the Venn Diagram to show set Q and set R.

The universal set,  $\mathscr{E} = \{\text{Whole numbers}\}\$ 

 $A = \{\text{Multiples of 5}\}\$ 

 $B = \{\text{Multiples of 3}\}\$ 

Sets A and B are represented by the circles in the Venn diagram.

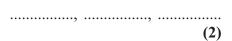


- (a) (i) On the diagram, shade the region that represents the set  $A \cap B'$ .
  - (ii) Write down **three** members of the set  $A \cap B'$ .



 $C = \{\text{Multiples of } 10\}.$ 

- (b) (i) On the diagram draw a circle to represent the set C.
  - (ii) Write down **three** members of the set  $A \cap B \cap C'$



A and B are two sets.

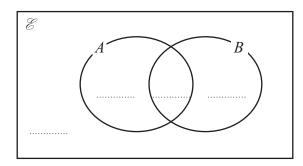
$$n(\mathscr{E}) = 37$$

$$n(A) = 22$$

$$n(A \cap B) = 12$$

$$n(A \cup B) = 30$$

(a) Complete the Venn Diagram to show the **numbers** of elements.



(2)

(b) Find (i)  $n(A \cap B')$ 



(ii)  $n(A' \cup B')$ 



(2)

P and Q are two sets. n(P) = 9 and n(Q) = 5

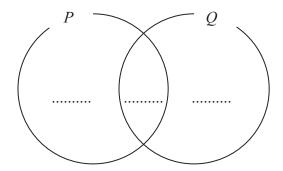
(a) Find the value of  $n(P \cup Q)$  when  $P \cap Q = \emptyset$ 

$$n(P \cup Q) = \dots$$
 (1)

(b) Find the value of  $n(P \cup Q)$  when  $Q \subset P$ 

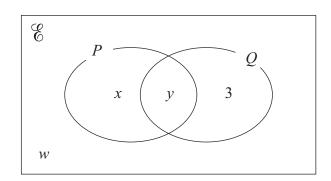
$$n(P \cup Q) = \dots$$
 (1)

(c) (i) Complete the Venn Diagram to show **numbers** of elements when  $n(P \cap Q) = 3$ 



(ii) Find the value of  $n(P \cup Q)$  when  $n(P \cap Q) = 3$ 

$$n(P \cup Q) = \dots$$



In the Venn diagram, 3, w, x and y represent the **numbers** of elements.

$$n(\mathscr{E}) = 24$$

$$n(P') = 8$$

$$n((P \cap Q)') = 15$$

- (a) Find the value of
- (i) w
- (ii) x
- (iii) y

(i) 
$$w = ....$$

(ii) 
$$x = ....$$

(iii) 
$$y = ....$$
 (3)

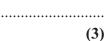
(b) (i) Find  $n(P' \cap Q)$ .

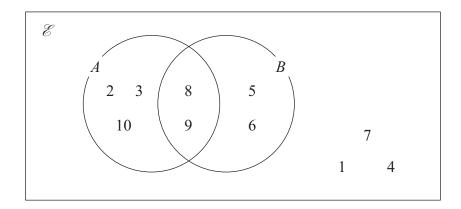


(ii) Find  $n(P' \cup Q')$ .



(iii) Find  $n(P \cap Q \cap P')$ .





The Venn diagram shows all of the elements in sets A, B and  $\mathcal{E}$ .

(a) Write down the elements in A'

(1)

(b) Find  $n(A \cap B)'$ 

(1)

(c) Find the elements in  $(A \cap B) \cup (A \cup B)'$ 

(1)

$$A \cap C = \emptyset$$
  
 $B \cup C = \{5, 6, 7, 8, 9\}$   
 $n(C) = 3$ 

(d) Write down the elements in C.

(1)

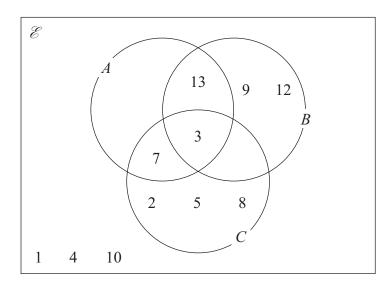
$$\mathcal{E}$$
= {1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13}

$$A = \{3, 7, 11, 13\}$$

$$B = \{3, 6, 9, 12, 13\}$$

$$C = \{2, 3, 5, 6, 7, 8\}$$

(a) Complete the Venn diagram.



(1)

(b) List the members of the set  $B' \cap C$ 



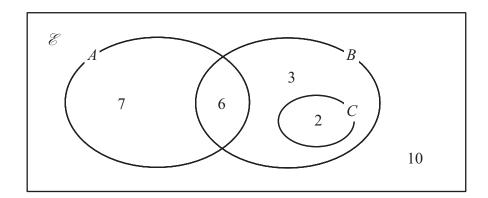
(c) List the members of the set  $(A \cup C)' \cap B$ 



(d) Find  $n(A' \cap B')$ 



The Venn diagram shows a universal set  $\mathscr{E}$  and three sets A, B and C.



7, 6, 3, 2 and 10 represent the **numbers** of elements.

Find

(i)  $n(A \cup B)$ 

.....

(ii) n(A')

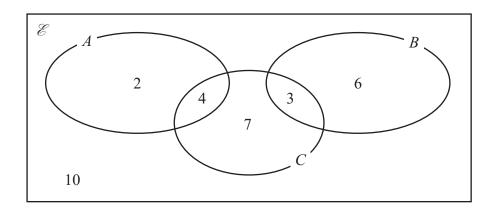
.....

(iii)  $n(B \cap C')$ 

.....

(iv)  $n(A' \cup B')$ 

The Venn diagram shows a universal set  $\mathscr{E}$  and 3 sets A, B and C.



2, 4, 7, 3, 6 and 10 represent **numbers** of elements.

Find

(i)  $n(A \cup B)$ 

(ii) n (B')

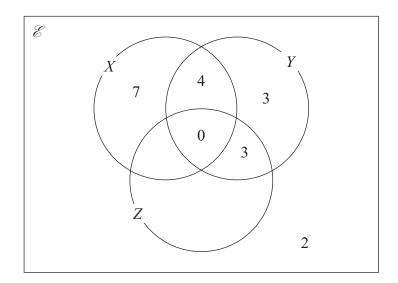
(iii) n  $(A \cap C')$ 

(iv) n  $(B' \cap C')$ 

.....

.....

The Venn diagram shows a universal set  $\mathcal{E}$  and three sets X, Y and Z.



The numbers shown represent **numbers** of elements.

$$n(X') = 14$$

$$n(Z) = 14$$

(a) Complete the Venn diagram.

**(2)** 

- (b) Find the value of
  - (i)  $n(X \cup \bullet Z)$

(ii)  $n(X \cap Y')$ 

**(2)** 

14. [3 marks

A garage tests cars for faults.

There are three types of fault – braking, steering and lighting.

A car fails the test if it has one or more of these three types of fault.

Last week, 11 cars had braking faults

9 cars had steering faults

7 cars had lighting faults

no car had both steering faults and lighting faults

2 cars had both braking faults and steering faults

3 cars had both braking faults and lighting faults.

By drawing a Venn Diagram, or otherwise, find the number of cars which failed the test last week.

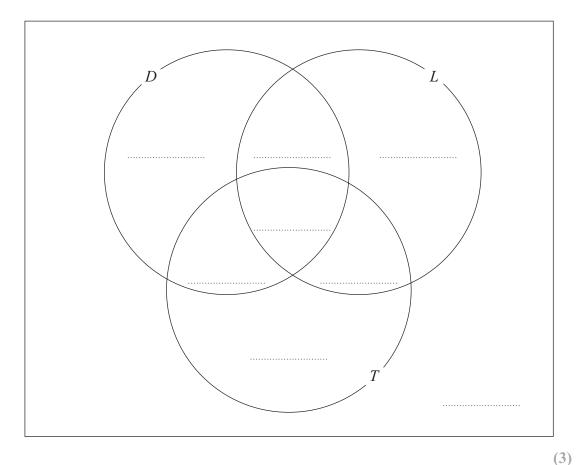
15. [4 marks]

Each student in a group of 32 students was asked the following question.

"Do you have a desktop computer (D), a laptop (L) or a tablet (T)?"

Their answers showed that

- 19 students have a desktop computer
- 17 students have a laptop
- 16 students have a tablet
- 9 students have both a desktop computer and a laptop
- 11 students have both a desktop computer and a tablet
- 7 students have both a laptop and a tablet
- 5 students have all three.
- (a) Using this information, complete the Venn diagram to show the number of students in each appropriate subset.



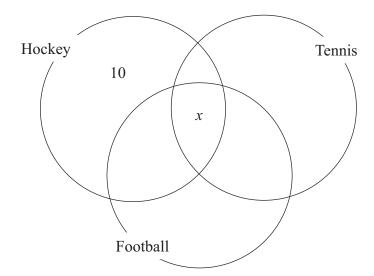
One of the students with both a desktop computer and a laptop is chosen at random.

(b) Find the probability that this student also has a tablet.



Each student in a group plays at least one of hockey, tennis and football.

- 10 students play hockey only
- 9 play football only.
- 13 play tennis only.
- 6 play hockey and football but not tennis.
- 7 play hockey and tennis.
- 8 play football and tennis.
- x play all three sports.



(a)	Write down an expression, in terms of x	, for the number of students who play hockey
	and tennis, but not football.	

.....(1)

There are 50 students in the group.

(b) Find the value of x.

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