CIRCLE THEOREMS

[ESTIMATED TIME: 60 minutes]



(+ IGCSE) EXAM QUESTION PRACTICE

1. [3 marks]

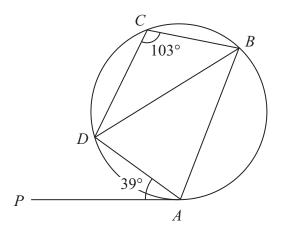


Diagram NOT accurately drawn

A, B, C and D are points on a circle.

PA is a tangent to the circle.

Angle $PAD = 39^{\circ}$

Angle $BCD = 103^{\circ}$

Calculate the size of angle ADB.



A, B, C and D are points on a circle.

Angle $BAC = 40^{\circ}$.

Angle $DBC = 55^{\circ}$.

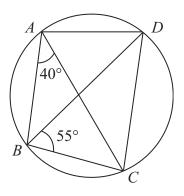


Diagram **NOT** accurately drawn

(i)	Find the size of angle <i>DAC</i> .	
(ii)	Give a reason for your answer.	. • •
(i)		(2
(ii)	Give reasons for your answer.	. • •
		•••
		•••
		(3
	(ii) (ii) Is <i>B</i>	(ii) Calculate the size of angle <i>DCB</i> . (iii) Give reasons for your answer. Is <i>BD</i> a diameter of the circle? Give a reason for your answer.

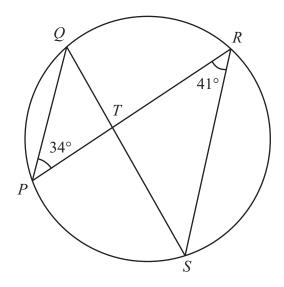


Diagram **NOT** accurately drawn

P, Q, R and S are points on the circumference of a circle. PR and QS intersect at T.

Angle $\widetilde{QPR} = 34^{\circ}$ and angle $PRS = 41^{\circ}$

(a) (i) Find the size of angle *PQS*.

(ii)	Give a reason for your answer.	
		(2)
(b) (i)	Find the size of angle <i>PTS</i> .	
(ii)	Explain why T cannot be the centre of the circle.	

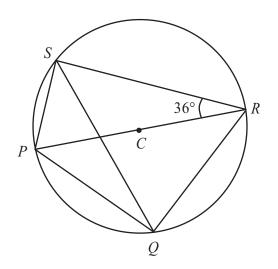


Diagram **NOT** accurately drawn

P, Q, R and S are points on a circle, centre C. PCR is a straight line. Angle $PRS = 36^{\circ}$.

Calculate the size of angle *RQS*. Give a reason for each step in your working.

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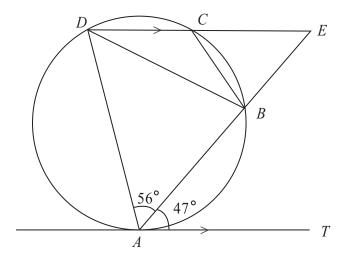


Diagram **NOT** accurately drawn

A, B, C and D are points on a circle. ABE and DCE are straight lines. AT is a tangent to the circle. DCE is parallel to AT. Angle $EAT = 47^{\circ}$. Angle $BAD = 56^{\circ}$.

(a)	(i)	Find	the	size	of	angle	AED.

			0
	(ii)	Give a reason for your answer.	
			(2)
(b)	Fin	nd the size of angle <i>BCD</i> .	()
			0
			(1)
(c)	(i)	Find the size of angle <i>ADB</i> .	
` /			0
	(ii)	Give a reason for your answer.	
			(2)

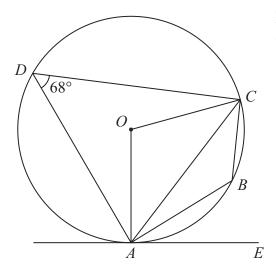


Diagram **NOT** accurately drawn

A, B, C and D are points on a circle, centre O. AE is a tangent to the circle. Angle $ADC = 68^{\circ}$

(a) (i) Find the size of angle ABC.

(ii) Give a reason for your answer.

(b) (i) Find the size of angle AOC.

(ii) Give a reason for your answer.

(c) Find the size of angle CAE.

(1)

(2)

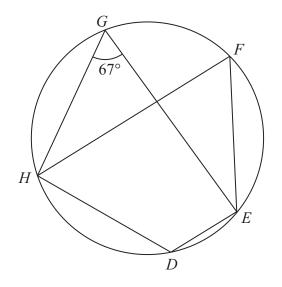


Diagram **NOT** accurately drawn

D, E, F, G and H are points on a circle. Angle $EGH = 67^{\circ}$

((a)	Find	the	size	of	angle	EFH.
	()		****		-	2010	

	(1)
(b) (i) Find the size of angle <i>EDH</i> .	
(ii) Give a reason for your answer.	

(2)

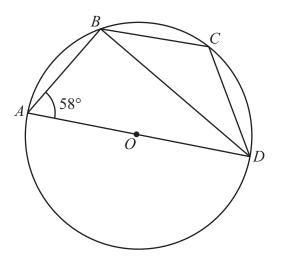


Diagram **NOT** accurately drawn

A, B, C and D are four points on a circle, centre O. AD is a diameter of the circle. Angle $BAD = 58^{\circ}$

(a) Calculate the size of angle ADB.

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(2)	

(b) (i) Calculate the size of angle BCD.

<i>(</i>)		
(11)	Give a reason for your answer.	

(2)

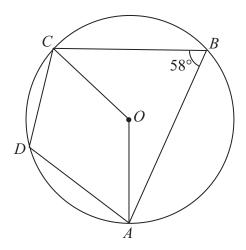


Diagram **NOT** accurately drawn

A, B, C and D are points on a circle, centre O. Angle $ABC = 58^{\circ}$.

(a) (i) Calculate the size of angle AOC.

	(ii)	Give a reason for your answer.	
			(2)
(b)	(i)	Calculate the size of angle <i>ADC</i> .	(-)
	(ii)	Give a reason for your answer.	
			(2)

10. [3 marks]

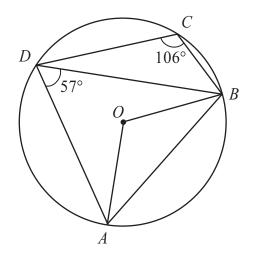


Diagram **NOT** accurately drawn

A, B, C and D are points	on a circle	e, centre O
Angle $ADB = 57^{\circ}$.		
Angle $BCD = 106^{\circ}$.		

(a) (i) Calculate the size of angle AOB.

(ii) Give a reason for your answer.	
	(2)
(b) Calculate the size of angle <i>RAD</i>	

	0
(1)	

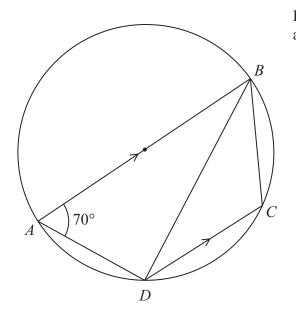


Diagram **NOT** accurately drawn

A, B, C and D are points on a circle. AB is a diameter of the circle. DC is parallel to AB. Angle $BAD = 70^{\circ}$

(a) Calculate the size of angle BDC.

(2)

The tangent to the circle at D meets the line BC extended at T.

(b) Calculate the size of angle BTD.

(3)

12. [6 marks]

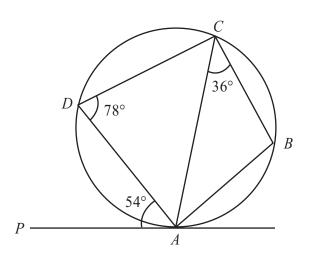


Diagram NOT accurately drawn

A, B, C and D are points on a circle. PA is the tangent to the circle at A. Angle $PAD = 54^{\circ}$, angle $ACB = 36^{\circ}$ and angle $ADC = 78^{\circ}$.

		(2)
	(ii)	Give a reason for your answer.
		•
(a)	(i)	Find the size of angle ACD.

(b)	Explain why BD is a diameter of the circle.								
	••••	•••••	••••••	•••••		•••••	•••••	 •••••	•••••
				• • • • • • • • • • • • • • • • • • • •				 	
									(2)
(c)	(i)	Work	out the s	size of an	gle <i>ABC</i> .				

		0
		••••
(ii)	Give a reason for your answer.	
()		
		•••••

(2)

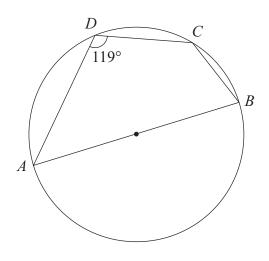


Diagram **NOT** accurately drawn

A, B, C and D are points on the circumference of a circle. AB is a diameter of the circle. Angle $ADC = 119^{\circ}$.

(a) (i) Work out the size of angle ABC.

(ii)	Give a reason for your answer.	
		(2)

(b) Work out the size of angle BAC.



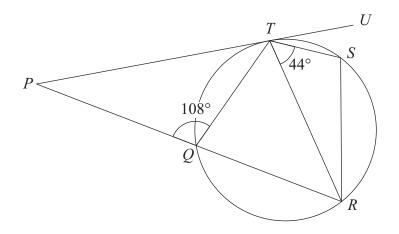


Diagram **NOT** accurately drawn

Q, R, S and T are points on the circumference of a circle.

PU is a tangent to the circle at T.

PQR is a straight line.

Angle $PQT = 108^{\circ}$.

Angle $STR = 44^{\circ}$.

Work out the size of angle STU.

You must give a reason for each step in your working.

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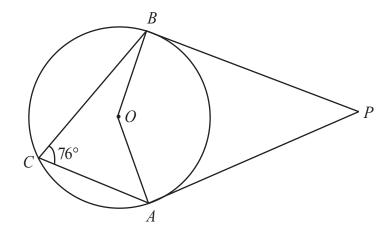


Diagram **NOT** accurately drawn

A, B and C are points on a circle, centre O.

Angle $ACB = 76^{\circ}$

PA and PB are tangents to the circle.

Calculate the size of angle APB.

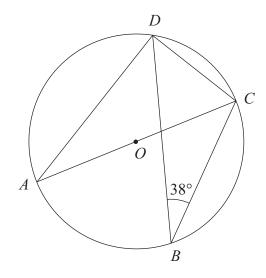


Diagram **NOT** accurately drawn

A, B, C and D are points on a circle, centre O. AC is a diameter of the circle. Angle $CBD = 38^{\circ}$.

(a) (i) Find the size of angle DAC.

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(ii) Give a reason for your answer.

(2)

(b) Find the size of angle ACD.